



Integral Backstepping Control of Induction Machine

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ABSTRACT

The goal of this work is to propose a latest design of a rotor speed and rotor flux modulus control approach for an induction machine using a Backstepping corrector with an integral action. The advantage of the Backstepping Strategy is the ability to manage a nonlinear system. The Lyapunov theory has been used to ensure the system stability. To improve the controller robustness proprieties the integral action is used, despite the system uncertainties and the existence of external disturbances. The unavailable rotor flux is recovered by estimation of the rotor flux of the machine based on the integration of the stator voltage expressions. The simulation results illustrate the effectiveness of the proposed control scheme under load disturbances, rotor resistance variation and low and high speed.

1. INTRODUCTION

Compared to other electric machine types, the induction motor plays a crucial role in many industrial applications because of its excellent reliability, great robustness, less maintenance, robustness and low cost [1-3]. However, the control problem is more complex for induction motors, due to their multivariable and strongly nonlinear dynamics [4]. Also, physical parameter uncertainties, such as the variation of the rotor resistance with temperature, affect significantly the dynamics of the system, whereas the load torque strictly depends on the load type. In the majority of industrial applications, it is required to be able to control the speed of induction motor drives. Using linear system theory for controlling the induction machine can present limitations, especially in transient regimes [5]. On the other hand, using the PI controller induces many problems such as high overshoot, oscillation of speed and torque due to sudden load changes and external disturbances. This poor ability to manage the uncertainty of the system constitutes a major drawback which can lead to a degradation of the system performance.

A literature review shows that nonlinear pre-compensation can be used as a powerful method for controlling the induction machine based on the linearization technique [6, 7]. Nevertheless, the nonlinear part of the system must be neglected [5]. The first control techniques used for variable speeds are based on classical scalar control allows to ensure only basic performances [8]. In different applications, it is important to integrate new sophisticated controls as Field Oriented Control (FOC). This command, which was initiated in 1972, consists to make the behavior of the induction motor analogous to that of the DC motor [9, 10]. Its principle is based on the model of the asynchronous machine in a rotating reference frame and makes it possible to independently control the flux and the torque in a manner similar to the DC machine. In the literature, two types of vector control are possible: the first is called direct vector control, which requires the

estimation of the position of the vector rotor flux (modulus and phase). However, the next type is named indirect vector control, which is characterized only by the estimation of the rotor flux [10]. Nonetheless the drawbacks of this technique essentially reside in the sensitivity to motor parametric variations and external load disturbances, especially according to the rotor resistance variation [11]. Knowing the calculation of the flux orientation angle is based on this resistance.

A small variation in this resistance can cause an error in the orientation of the rotating frame. In addition, the consequences can influent on the decoupling [10].

To overcome these problems, various nonlinear command techniques have been examined. Among these nonlinear control techniques that ensure high performance and global decoupling between the outputs to control whatever the path profile imposed for the machine; we can cite the technique of input-output feedback linearization presented by Hill [12]. This technique focuses on the differential geometry principle to convert a non-linear system into a linear system using a linearization state feedback with input-output decoupling. From there, we can apply the theory of linear systems [13, 14].

The study presented in Refs. [15] and [16] shows that passivity based control method is incapable to eliminate the non-linearity terms. However, it allows guarantying the stability of system, taking into account a damping part of the global energy of the system. Also, this method ensures the robustness control under the parameter uncertainties. Nevertheless, this method has some drawbacks [17, 18].

- 1) The necessary and sufficient conditions used to linearize the system can't be permanently ensured during the time;
- 2) Existence of singular points;
- 3) Complexity of the controller and heavy computing of the load.

The sliding mode control represents another technique for controlling the systems. In fact, it has high robustness proprieties and its design is easy. The main disadvantage of this technique is the chattering phenomenon. Due to high

oscillations of frequency this phenomenon is appeared. The consequence of the chattering phenomenon is the dynamic instability of systems [6, 19].

Recently, the technique of Backstepping command has been extensively discussed and designed for the nonlinear control of nonlinear systems [11, 20, 21]. This technique is initiated by Fateh and Abdellatif [20]. In transient and steady state regimes, this technique accords good performances. It's considered more robust under the variations in parameter and presence of load torque perturbations. But it is relatively well in steady state regime. Indeed, the classical Backstepping control technique focuses on a proportional derivative, which provides a static error [20]. The conception of this method is realized by using Lyapunov stability tools. The modification of Backstepping approach of control by adding integral action is an interesting solution to improve the robustness of Backstepping control and eliminate residual errors [20].

The importance of the integral backstepping strategy in the control of induction motors by making a judicious choice of the Lyapunov function lies in the stability of the whole system [21]. The main advantages of this strategy of control are: robustness under parametric variation constraints and good tracking references [20].

In the present paper, the Backstepping approach control, robustness of speed-flux and torque ($\xi_1 = \frac{1}{j}T_e$) controllers have been improved by integrating new integral terms. The addition of the integral action makes it possible to significantly reduce the effect of the variation in resistance of the rotor as well as the disturbance due to the load torque and therefore eliminates the error in steady state.

The organization of this manuscript is given as follows: In section two the nonlinear induction motor model is presented. In section three, design of integral Back-stepping speed and flux controllers are developed. Estimator of rotor flux is presented in the section four. Finally, simulation results and interpretations are discussed.

2. IM NON-LINEAR MODELLING

To lower the multiplicity of the IM model, an equivalent representation of two phases has been used. This representation considers linearity assumptions of the magnetic circuit and neglects iron losses. The design of this model class is developed under the fixed (α, β) stator reference frame, by the following non-linear functions with the stator current, rotor flux and rotor speed as selected state variables of the motor. Under these conditions, the non-linear model of the IM can be formulated as follow [5]:

$$\dot{x} = f(x) + g(x)u \quad (1)$$

$$y = h(x) \quad (2)$$

With,

$$f(x) = \begin{bmatrix} -\gamma i_{s\alpha} + \frac{K}{T_r} \varphi_{r\alpha} + p\omega \varphi_{r\beta} \\ -\gamma i_{s\beta} - p\omega K \varphi_{r\alpha} + \frac{K}{T_r} \varphi_{r\beta} \\ \frac{M}{T_r} i_{s\alpha} - \frac{1}{T_r} \varphi_{r\alpha} + p\omega \varphi_{r\beta} \\ \frac{M}{T_r} i_{s\beta} - p\omega \varphi_{r\alpha} - \frac{1}{T_r} \varphi_{r\beta} \\ \frac{pM}{jL_r} (\varphi_{r\alpha} i_{s\beta} - \varphi_{r\beta} i_{s\alpha}) - \frac{f}{j} \Omega - \frac{T_l}{j} \end{bmatrix} \quad (3)$$

$$g(x) = \begin{bmatrix} \frac{1}{\sigma L_s} & 0 & 0 & 0 \\ 0 & \frac{1}{\sigma L_s} & 0 & 0 \end{bmatrix}^T \quad (4)$$

$$h(x) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \quad (5)$$

$$K = \frac{1}{M} \left(\frac{1-\sigma}{\sigma} \right), \sigma = 1 - \frac{M^2}{L_s L_r}, \gamma = \frac{1}{\sigma} \left(\frac{1}{T_s} + \frac{1-\sigma}{T_r} \right), k_f = \frac{f}{j},$$

$$k_l = \frac{p}{j}, \text{ and } \omega = p\Omega.$$

where,

- The indicators s and r are defined respectively for the stator and the rotor components.
- α and β symbols indicate respectively the direct and quadrature of the fixed stator reference frame components.
- $x = [i_{s\alpha}, i_{s\beta}, \varphi_{r\alpha}, \varphi_{r\beta}, \Omega]^T$ represents the state vector; $u = [u_{s\alpha}, u_{s\beta}]^T$ shows the input vector of control.
- R is the resistance, L is the inductance, M is the mutual inductance. T_s and T_r are the stator and the rotor time constant respectively.
- Ω is the rotor speed, f is the friction coefficient, j represents the moment of inertia coefficient, p is the number of pair poles, and finally T_l is the load torque.

3. DESIGN OF FLUX AND SPEED BACKSTEPPING CONTROLLER

3.1 Control objective

The goal of control is to design the virtual control (appropriate functions), to simplify a complex nonlinear control problem. The simplification has been done by dividing the control design into several steps. Each step deal with a single input-output design problem, and considered as a reference for the next step. To ensure global system stability and tracking objectives, the ELF is used step by step [21].

3.2 Step one

In this step, it is important to identify the target trajectories that the system must follow them. Also, to guarantee best tracking precision, the controllers must be designed.

The desired trajectories of rotor speed and rotor flux modulus are defined by Ω_d and φ_d^2 .

The speed tracking error e_1 and the flux modulus tracking error e_3 can be controlled using the auxiliary variables ξ_1^d and ξ_2^d respectively.

We define tracking errors as:

$$e_1 = \Omega_d - \Omega \quad (6)$$

$$e_3 = \psi_d - \psi_r \quad (7)$$

With $\psi_r = \varphi_{r\alpha}^2 + \varphi_{r\beta}^2$.

Their dynamics equations are given by:

$$\dot{e}_1 = \dot{\Omega}_d - \left[\frac{pM}{jL_r} (\varphi_{r\alpha} i_{s\beta} - \varphi_{r\beta} i_{s\alpha}) - \frac{T_l}{j} - \frac{f}{j} \Omega \right] \quad (8)$$

$$\dot{e}_3 = \psi_d - \left[\frac{2M}{T_r} (\varphi_{r\alpha} i_{s\alpha} + \varphi_{r\beta} i_{s\beta}) \right] + \frac{2}{T_r} \psi_r \quad (9)$$

The virtual control expressions are given as follow:

$$\xi_1 = \left[\frac{pM}{jL_r} (\varphi_{r\alpha} i_{s\beta} - \varphi_{r\beta} i_{s\alpha}) \right] \quad (10)$$

$$\xi_2 = \left[\frac{2M}{T_r} (\varphi_{r\alpha} i_{s\alpha} + \varphi_{r\beta} i_{s\beta}) \right] \quad (11)$$

Eqns. (8) and (9) can be formulated by the following expressions:

$$\dot{e}_1 = \dot{\Omega}_d - \xi_1 + \frac{T_l}{j} + \frac{f}{j} \Omega \quad (12)$$

$$\dot{e}_3 = \dot{\psi}_d - \xi_2 + \frac{2}{T_r} \varphi_r^2 \quad (13)$$

Checking of the tracking error dynamics stability is based on the following CLF:

$$v_1 = \frac{1}{2} [e_1^2 + e_3^2] \quad (14)$$

The mathematical expression given in (15) shows a derivative of (14) in a function of time.

$$\dot{v}_1 = e_1 \dot{e}_1 + e_3 \dot{e}_3 \quad (15)$$

The derivative error tracking has been chosen as follows.

$$\dot{e}_1 = -k_1 e_1 \quad (16)$$

$$\dot{e}_3 = -k_3 e_3 \quad (17)$$

The negative sign of (16) and (17) means that Lyapunov function is negative defined.

So, under these conditions, the virtual control extracted from expressions (12) and (13) can be written as follow:

$$\xi_1^* = k_1 e_1 + \dot{\Omega}_d + \frac{T_l}{j} + \frac{f}{j} \Omega \quad (18)$$

$$\xi_2^* = k_3 e_3 + \dot{\psi}_d + \frac{2}{T_r} (\psi_d - e_3) \quad (19)$$

where, coefficients k_1 and k_3 represent the positive design gains that define the dynamic of closed loop.

The derivative of the LF according to time is clearly negative definite. Then the tracking error e_1 and e_3 can reach a permanent regime.

Since the variables ξ_1 and ξ_2 are not a control inputs and only two variables of the system with its own dynamics. We will utilize it to insert the integral action, so the virtual controls ξ_1^* and ξ_2^* are used to guarantee the stability of the speed and modulus flux loops. The dynamics of the tracking errors are given by:

$$\xi_1^d = \xi_1^* + \lambda_1 \chi_1 \quad (20)$$

$$\xi_2^d = \xi_2^* + \lambda_2 \chi_2 \quad (21)$$

With λ_1 and λ_2 are positive constants and $\chi_i = \int_0^t e_i(\tau) d\tau$ $i = 1, 2$ are the integral actions brought in accordance with the following error. By introducing there in the virtual control, we insure the convergence of the error towards zero in steady state.

3.3 Step two

The control objective becomes: oblige the auxiliary variable ξ_1 to track ξ_1^d while ξ_2 must track ξ_2^d .

Last references have been chosen to guarantee a steady dynamic of velocity and flux modulus tracking error. Considering errors between them is important for virtual controls. The control objective becomes: force the auxiliary variable ξ_1 to track ξ_1^d while ξ_2 must track ξ_2^d .

To this end, let us define the following errors:

$$e_2 = \xi_1^d - \xi_1 = \xi_1^* + \lambda_1 \chi_1 - \xi_1 \quad (22)$$

$$e_4 = \xi_2^d - \xi_2 = \xi_2^* + \lambda_2 \chi_2 - \xi_2 \quad (23)$$

The time derivative of (22) and (23) gives:

$$\dot{e}_2 = \dot{\xi}_1^d - \dot{\xi}_1 = \dot{\xi}_1^* + \lambda_1 e_1 - \dot{\xi}_1 \quad (24)$$

$$\dot{e}_4 = \dot{\xi}_2^d - \dot{\xi}_2 = \dot{\xi}_2^* + \lambda_2 e_3 - \dot{\xi}_2 \quad (25)$$

New formulation of equations (24) and (25) in function of new terms e_2 and e_4 are given as follow:

$$\dot{e}_1 = -k_1 e_1 + e_2 \quad (26)$$

$$\dot{e}_3 = -k_3 e_3 + e_4 \quad (27)$$

From (24) and (25), new formulations of error dynamics have been obtained.

$$\dot{e}_2 = \dot{\xi}_3 - \left[\frac{pK}{j} (\varphi_{r\alpha} u_{s\beta} - \varphi_{r\beta} u_{s\alpha}) \right] \quad (28)$$

$$\dot{e}_4 = \dot{\xi}_4 - [2KR_r (\varphi_{r\alpha} u_{s\alpha} + \varphi_{r\beta} u_{s\beta})] \quad (29)$$

where,

$$\begin{aligned} \xi_3 &= \xi_1^d + \frac{pM}{jL_r} \left[\left(\gamma + \frac{1}{T_r} \right) (\varphi_{r\alpha} i_{s\beta} - \varphi_{r\beta} i_{s\alpha}) \right] \\ &\quad + \frac{pM}{jL_r} [p\Omega (\varphi_{r\alpha} i_{s\alpha} + \varphi_{r\beta} i_{s\beta}) + K\varphi_r^2] \\ \xi_4 &= \xi_2^d + \frac{2M}{T_r} \left[\left(\gamma + \frac{1}{T_r} \right) (\varphi_{r\alpha} i_{s\alpha} + \varphi_{r\beta} i_{s\beta}) - \frac{K}{T_r} \varphi_r^2 \right] \\ &\quad - \frac{2M}{T_r} [p\Omega (\varphi_{r\alpha} i_{s\beta} - \varphi_{r\beta} i_{s\alpha}) \\ &\quad + \frac{M}{T_r} (i_{s\alpha}^2 + i_{s\beta}^2)] \end{aligned}$$

Expressions (28) and (29) show that the control term is included in the error dynamics formulations. So, the development of the augmented Lyapunov function is evident. Relation (30) shows this function.

$$v_2 = \frac{1}{2} [e_1^2 + e_2^2 + e_3^2 + e_4^2] \quad (30)$$

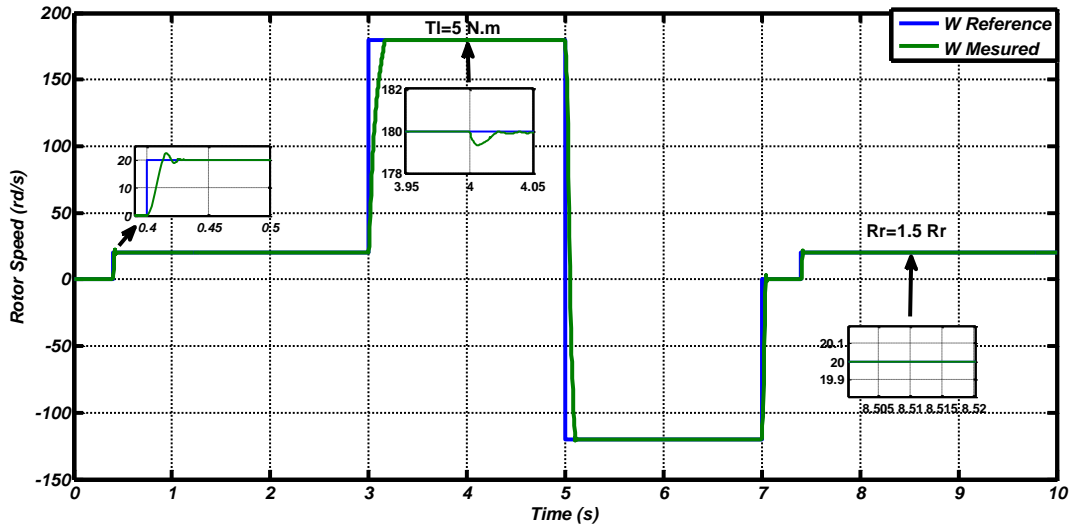


Figure 2. Reference and measured evolution of Rotor speed according to T_l and R_r variations

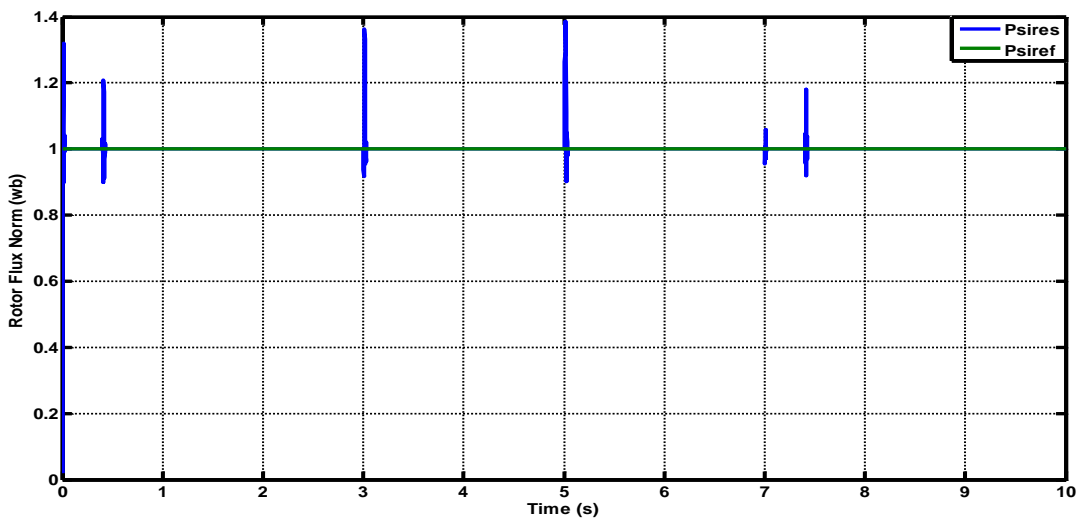


Figure 3. Reference and measured of the rotor flux norm under T_l and R_r variations

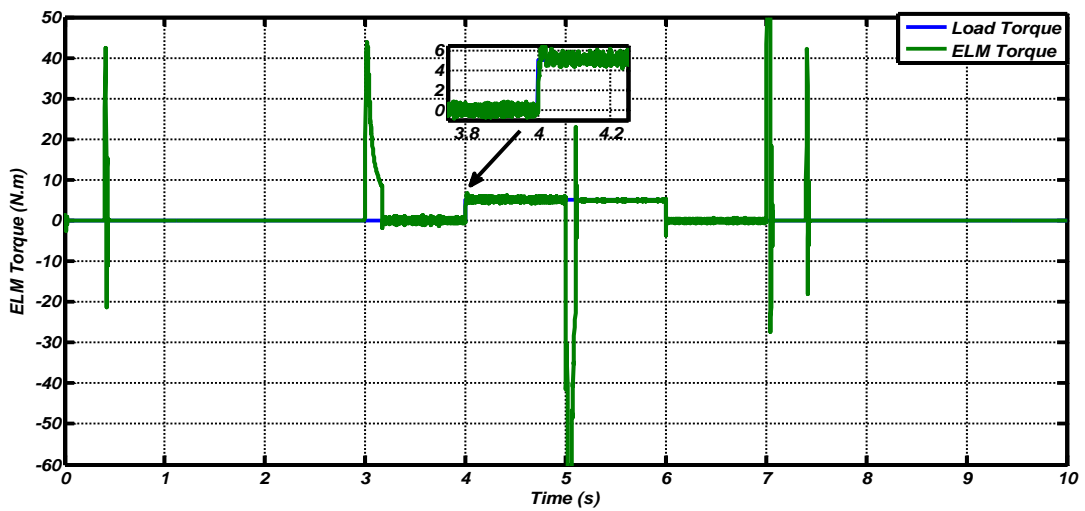


Figure 4. Variation of load and measured electromechanical torque

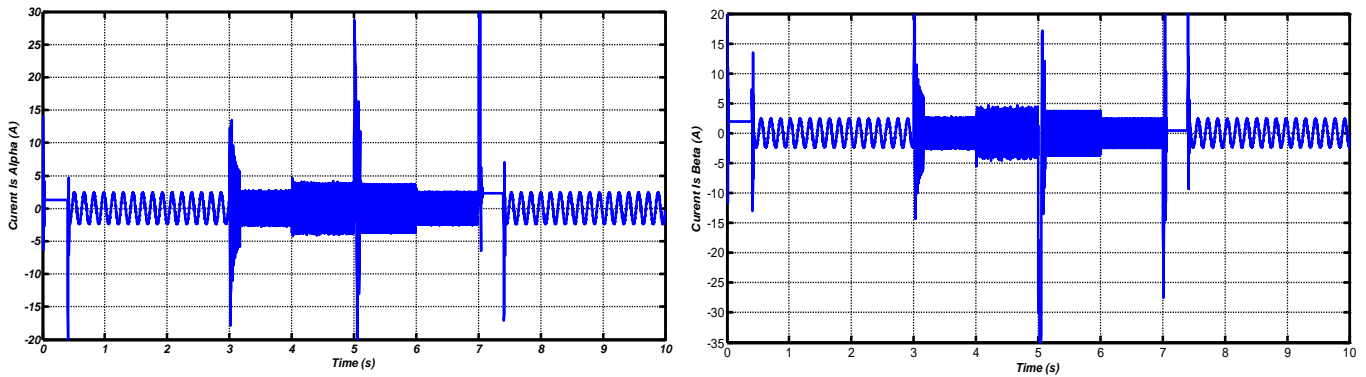


Figure 5. Measured $(\alpha - \beta)$ stator currents

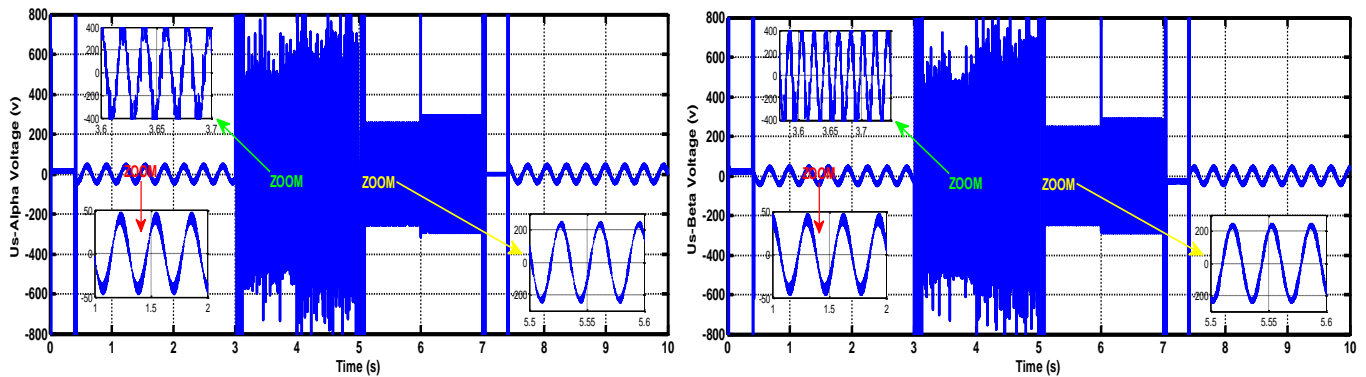


Figure 6. $(\alpha - \beta)$ stator voltage control inputs

Figure 3 illustrates that measured rotor flux norm follows the imposed flux with some disruption (peaks) when the speed change, the load and electromechanically torque of the motor are portrayed in Figure 4. A better tracking with negligible steady state error and a quick convergence, Figures 5-6 show respectively the measured stator currents and stator voltage components. Also, the simulation tests demonstrates that a remarkable decoupling impact of flux and torque components under rotor velocity, torque of load and rotor resistance variations, but the curves of rotor flux modulus, stator currents, torque and stator voltage present a peak when the speed change. This peak appeared because the specific action of the PWM inverter.

5. CONCLUSION

A new control scheme has been proposed in this manuscript. The proposed technique based on Backstepping control strategy with integration of integral action. The presented control combined with estimator have been tested via simulation under different operating conditions of the motor, specifically under conditions of load and speed variations, at low and high speed with a dynamic variation in rotor resistance of the motor.

The obtained results demonstrate that the proposed approach of control has high performances and ensures a perfect decoupling between the torque and flux. In fact, the machine operates permanently under these performances. Furthermore, by considering online parameter estimation the proposed approach can be improved.

Moreover, the obtained simulation results explain that the developed approach able to improve the performance of trajectory tracking under different conditions. In the case of

nonlinear control, the use of estimator considered efficient tool to estimate the states of unmeasurable variables (rotor flux). As perspectives for future works, experimental tests are envisaged.

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