Efficient Rectified Stator Currents Hysteresis Control of the Induction Motor Drive and Flux Optimization Using Fuzzy Logic

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ABSTRACT

The induction machine (IM) is a nonlinear, multivariable, strongly coupled system. Therefore, it is necessary to achieve a decoupling between flux and torque. The vector control technique is the one that gives better performance. To have high dynamic responses and better torque control, the machine must be supplied with sinusoidal currents. The present work contributes to improving the efficiency of a flux-oriented indirect control (IFOC) of an induction motor associated with a new hysteresis inverter. The Induction motors have good efficiencies when operating at full load. However, at lower than rated loads, which is a condition that many machines experience for significant portion of their service life, the efficiency is greatly reduced. To improve the efficiency of the existing motor it is important to regulate the flux of the motor in the desired operating range. This paper proposes the analytical approach of minimizing copper losses for an induction motor and energy efficient control strategy based on fuzzy logic using Matlab / Simulink®. This parameter is used to determine an optimal rotor flux reference it has the goal of maximizing the efficiency for each given load torque. The proposed fuzzy controller adjusts the electromagnetic torque, to give the optimized flux by minimizing losses.

1. INTRODUCTION

Currently, the research scientific around the world are engaged for the environment and energy conservation. The interest in the various problems posed firstly, push states to remodel their Energy and Environmental strategies, and secondly to put the inventors and the manufacturers of electrical systems in front of an important challenge which is Clean Energy.

The electrical energy is placed in the category of clean energy during its use but sometimes it’s not suitable during its production. Moreover, energy demand and the cost of its production and its operation are constantly increasing. This leads us to improving the efficiency of systems producing or consuming electrical energy [1].

Improving the efficiency of this large energy consumer will necessarily lead to significant savings in energy and money. Opting for an electric vehicle, it means choose an ecological automobile and less polluting in the use and also more silent to contribute for reducing disturbance noise… and improve our health grace to the absence of CO2 emissions.

Nowadays, a serious problem is mentioned by the industry, namely the high energy consumption in the face of increasingly limited energy sources. Several strategies and measures have been suggested to remedy this consumption which is growing [1].

Among these solutions, we can cite the reduction of electric energy consumption starting from the engines which generally constitute a large part of the high energy consumption equipment in the industry.

In the context of electric traction, the energy efficiency of the entire traction chain is essential. Indeed, asynchronous motors (our choice of study) that are included in this chain of traction have a good performance at the nominal point which degrades quickly outside this point of operation.

The efficiency of the induction motor can be improved by an optimal control of flux allowing the minimization of the machine losses. The induction motor losses can be classified into four types: Electrical losses, Magnetic losses, Mechanical losses, and supplementary losses. The effort is carried on the reduction of Electrical losses because they represent between 55% and 60% total losses of the machine and they are controllable. Many studies have identified several possible methods of minimizing machine losses [2, 3].

Several studies have participated improving the efficiency of asynchronous machines based on flux regulation because asynchronous motors operate at nominal flux even at low load by varying the load torque. Drid et al. [2] told about how to maximize engine efficiency for each value of load torque by genetic algorithm.

A loss model-based energy efficient control strategy for the IM using an optimal rotor flux reference has been accomplished by [3] which is determined using two advanced particle swarm optimization (PSO) algorithms, known as the dynamic particle swarm optimization (Dynamic PSO) and the chaos particle swarm optimization (Chaos PSO) algorithms.

The control schemes used in industry operate at constant flux at its nominal value. In this case, the engine operates at rated speed [4, 5], the increased losses lead to excessive consumption of electrical energy, due to the reduced load [6,
Adjusting the flux level of the motor using the IM loss model taking into account the variation of the parameters of the induction machine [8, 9], a genetic algorithm [10, 11] and a particle swarm [12] allowed the determination of the optimum flux level for efficient energy control using IM. Loss model.

If a losses model of the induction motor is available [13-15], the optimal flux by minimizing the losses can be calculated analytically. Although this method is characterized by its simplicity, the engine information must be known precisely.

The efficiency of the machine can be optimized, by finding the optimal values of the voltage and frequency of the drives based on the minimization of the induction motor losses. Many researches algorithms have been used. For induction motor efficiency optimization include Genetic Algorithm [8, 9], PSO, used to find the optimum values of the excitation voltage and frequency [10].

Improving efficiency by optimizing the waveforms provided by the inverter. Several strategies have been reported in the literature to reduce MI losses. Some algorithms use current [11], voltage [9], rotor flux [12] and other parameters.

At this point, we have studied the inverter machine association, where we use two types of inverter control, PWM and a new technique rectified currents hysteresis. However, this technique offers lower switching frequencies compared to PWM, giving us a non-rippled efficiency.

The induction machine (IM) is a nonlinear, multivariable, strongly coupled system. Therefore, it is necessary to achieve a decoupling between flux and torque. The vector control technique is the one that gives better performance. To have high dynamic responses and better torque control, the machine must be supplied with sinusoidal currents. However, some of these techniques deliver high switching frequencies and hysteresis band overshoots, and others have the disadvantage of phase current drift with respect to its reference [16-19].

In this work, we present a new hysteresis technique that provides a significant reduction in switching frequency and hysteresis band overshoots as well as the elimination of phase current drift from their references. Also we will propose a strategy Minimizing copper loss of the asynchronous machine by generating the optimal flux based on fuzzy logic.

This paper is organized into five sections. The mathematical model of IM and the principal of the inverter control with rectified currents hysteresis are introduced in section 2. In section 3, Analytical development of the optimal flux that ensures minimal losses is presented. Section 4 concerns flux optimization based on fuzzy logic. Finally, section 5 the simulation results are exposed and comparative illustration shows the performance of efficiency with flux optimization.

2. FLUX VECTOR ORIENTATION CONTROL

The vector control of the induction motor was invented by professor HASSE and professor BLASCHKE form university of Brunswick in 1968 [16, 17]. The main idea is to have the induction motor behavior be similar to that of a DC motor. Because it is well known that the induction motor model is nonlinear and strongly coupled (Flux-torque) unlike to the DC motor.

The vector control consists to keep the vector components of rotor flux as given in equation (1) and as illustrated on Figure 1 [18].

![Figure 1. Rotor flux orientation principle](image)

\[
\begin{align*}
\phi_{rd} &= \phi_r, \\
\phi_{rq} &= 0 \\
\end{align*}
\]

As a result of this orientation the flux and the torque will be decoupled equation (3) [18].

\[
\begin{align*}
\phi_r &= \frac{M}{T_s \omega_s + 1} I_{sd} \\
C_r &= p \frac{M}{L_r} \phi_r I_{sq} \\
\end{align*}
\]

We notice the rotor flux depends on the direct component of the stator current and the torque depends on quadratic component.

Stator, flux and speed control: The dynamics of stator currents rotor flux and mechanical speed are represented by (3), (4) and (6) respectively. Than the control of theses state variables is essay by using the placement poles technique [16-18].

\[
\begin{align*}
I_{sd} &= \frac{1}{\sigma L_{s} + R_s} (V_{sd} - e_d) \\
I_{sq} &= \frac{1}{\sigma L_{s} + R_s} (V_{sq} - e_q) \\
\end{align*}
\]

where electrical coupling terms are given as follows:
The mechanical equation is:

$$\Omega = \frac{1}{J} s f (C_c - C_r)$$  \hspace{1cm} (6)

The flux orientation vector control requires knowledge of the rotor module of the rotor flux. To do this, we can estimate the flux using the rotor equation (7) expressed in the stator reference frame, as shown on Figure 2 [18].

$$0 = -\frac{M}{T_r} I_{r\alpha} + \frac{1}{T_r} \phi_{r\alpha} + \frac{d \phi_{r\alpha}}{dt} + p \Omega \phi_{r\alpha}$$

$$0 = -\frac{M}{T_r} I_{r\beta} + \frac{1}{T_r} \phi_{r\beta} + \frac{d \phi_{r\beta}}{dt} - p \Omega \phi_{r\alpha}$$

$$\phi_r = \sqrt{\phi_{r\alpha}^2 + \phi_{r\beta}^2}$$

\[ \text{Equation (7)} \]

Figure 2. Rotor flux estimation

Sinusoidal PWM strategy

The SPWM is the widely strategy used to control the inverter. It consists to compartment the reference voltage (low frequency) with the triangular carrier signal (high-frequency), Figure 3.

Figure 3. SPWM

Figure 4 presents the general diagram of the oriented vector for the induction motor. Also the Speed, Rotor flux, stator current control loops and the flux orientation blocks are presented.

To test the vector control, some simulations have been done to control the speed at 157 rd/s. After stating the motor without load, a torque load 20 Nm is applied at 0.5 s. The flux rotor is maintained to 1 web.

Simulation and results

The results show the performance of the vector control to tracking speed and flux to their references in transient state as well as in steady state, Figure 5 and 6. The parameters of IM are given in the appendix, Table 5. However, we notice the torque presents same oscillations due to the switching frequency, Figure 7. Also there is a distortion the current stator, Figures 8, 9, 10.

Figure 4. Vector control Block diagram of the induction motor using SPWM

Figure 5. Speed response versus time

Figure 6. Rotor flux response versus time

Figure 7. Torque response versus time

Figure 8. Phase (A) stator current response versus time
Our objective is to have torque response and currents not rippled, which gives us a good efficiency of the machine, the method used is to replace the PWM with rectified hysteresis regulators, this method has given us a great improvement in the levels currents, torque and speed.

3. HYSTERESIS CONTROL SYSTEM

This technique is derived from the principle hysteresis control, where the currents of the three phases of the machine are rectified before being controlled by the hysteresis comparator, allows operation at low switching frequency.

The principle of this method consists to define in the stator reference plan ($\alpha$, $\beta$), eight voltage vectors $U_i$ ($i=0-7$) corresponding to the possible positions of the inverter switches, these vectors define in turn six sectors, Figure 11.

In the middle of each sector we create a new variable reference plan $\alpha_i\beta_i$ ($i=1, 6$). For example, according to the reference voltage position, when the stator current error vector ($\Delta i=i_{st}-i$) is located in sector 2, the referential ($\alpha_2\beta_2$) is considered the current error vector is therefore decomposed into two components $\Delta i_\alpha$ and $\Delta i_\beta$ serving as input signals of the hysteresis controllers. The output signals ($h_\alpha$ and $h_\beta$) determine the switches state [19].

The synoptic diagram of this technique is mentioned in the Figure 12.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure12.png}
\caption{Block diagram of the control system by rectified currents}
\end{figure}

- From the information on the voltages control, the block "S" performs the identification of the sector by detecting the zero crossing of the stator voltages and giving the.
- Binary vector $V$ whose expression is the following [19]:

$$V = \begin{bmatrix} V1 \\ V2 \\ V3 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 1+\text{sgn}(U_{12\text{ref}}) \\ 1+\text{sgn}(U_{23\text{ref}}) \\ 1+\text{sgn}(U_{12\text{ref}}-U_{23\text{ref}}) \end{bmatrix}$$

(8)

- The rectified current error vectors $\Delta i_\alpha$ and $\Delta i_\beta$ are obtained from Information available at the input of the "RC" block which is $V$ and $AI$ as shown in Figure 2 The vectors $\Delta i_\alpha$ and $\Delta i_\beta$ are defined by the following expressions and mentioned in Table 1 [19]:

$$\begin{cases} 
\Delta i_\alpha = \bar{r}_\alpha^T \bar{i}_\alpha \\
\Delta i_\beta = \bar{r}_\beta^T \bar{i}_\beta 
\end{cases}$$

(9)

With

$$\bar{i}_\alpha = \begin{bmatrix} i_1 & i_2 \end{bmatrix}^T; \bar{i}_\beta = \frac{1}{\sqrt{3}} \begin{bmatrix} i_1 & -i_2 \end{bmatrix}^T$$

$$\bar{r}_\alpha = \begin{bmatrix} 0 & 1 & -1 \\ 1 & 0 & -1 \end{bmatrix} V; \bar{r}_\beta = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \end{bmatrix} V$$

\begin{table}[h]
\centering
\caption{Definition the control variables}
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Sector N & V1 & V2 & V3 & $\Delta i_\alpha$ & $\Delta i_\beta$ \\
\hline
1 & 1 & 1 & 0 & (1-i3)/$\sqrt{3}$ & -i2 \\
2 & 0 & 1 & 0 & (i2-i3)/$\sqrt{3}$ & i1 \\
3 & 0 & 0 & 1 & (i2-i1)/$\sqrt{3}$ & -i3 \\
4 & 0 & 0 & 1 & (i3-i1)/$\sqrt{3}$ & i2 \\
5 & 1 & 0 & 1 & (i3-i2)/$\sqrt{3}$ & -i1 \\
6 & 1 & 0 & 0 & (i1-i2)/$\sqrt{3}$ & i3 \\
\hline
\end{tabular}
\end{table}
• The vectors $\Delta i_x$ and $\Delta i_y$ are the input variables of two hysteresis comparators. At the output of these comparators two bands are delivered $h_x$ along axis $x$ and $h_y$ along axis $y$.

• The switching states of the inverter switches Sa, Sb and Sc are obtained from Table 2 as a function of the values $V$, $h_x$ and $h_y$ [19].

The switching sequences (Table 2) $U_i$ ($i=0-7$), depend on $(h_x, h_y)$ the output of hysteresis controllers of $\Delta i_x$ and $\Delta i_y$.

<table>
<thead>
<tr>
<th>Sector N°</th>
<th>$(h_x, h_y)$</th>
<th>00</th>
<th>01</th>
<th>10</th>
<th>11</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>U7</td>
<td>U0</td>
<td>U2</td>
<td>U1</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>U0</td>
<td>U7</td>
<td>U3</td>
<td>U2</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>U7</td>
<td>U0</td>
<td>U4</td>
<td>U3</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>U0</td>
<td>U7</td>
<td>U5</td>
<td>U4</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>U7</td>
<td>U0</td>
<td>U6</td>
<td>U5</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>U0</td>
<td>U7</td>
<td>U1</td>
<td>U6</td>
<td></td>
</tr>
</tbody>
</table>

Table 2. Switching sequences

![Vector control Block diagram of the induction motor using RSCHC](image)

Figure 13. Vector control Block diagram of the induction motor using RSCHC

The simulations of the Vector control using RSCHC (Figure 13) is done with the same condition as with SPWM.

**Simulation and results**

The results are organized as follow:

![Speed response versus time](image)

Figure 14. Speed response versus time

![Rotor flux response versus time](image)

Figure 15. Rotor flux response versus time

![Torque response versus time](image)

Figure 16. Torque response versus time

![Phase (A) stator current response versus time (unloaded motor)](image)

Figure 17. Phase (A) stator current response versus time

![Zoom of Phase (A) stator current (unloaded motor)](image)

Figure 18. Zoom of Phase (A) stator current (unloaded motor)

![Zoom of Phase (A) stator current (Loaded motor 20Nm)](image)

Figure 19. Zoom of Phase (A) stator current (Loaded motor 20Nm)

The results show the performance of the vector control to tracking speed and flux to their references in dynamics as well as in steady state, Figure 14 and 15. However, we notice that the torque oscillations (Figure 16) are reduced compared with Figure 7. Also we can observe that the stator current is sinusoidal, Figures 17, 18, 19.

With SPWM the switching frequency is fixed thus and the distribution of the harmonics cannot be changed, in order to allow efficient operation of the motor operating at variable speed.
4. METHODS OF COPPER LOSS REDUCTION

We have chosen a simplified loss model which takes account only the copper losses. The joule losses of the induction motor are divided into two: the stator joule losses and the rotor joule losses. So the sum of the two losses gives us [20-24]:

\[ P_j = R_s (I_{st}^2 + I_{sq}^2) + R_r (I_{r}^2 + I_{rd}^2) \] (10)

In the steady state, the first equation of (3) can be written:

\[ I_{st} = \frac{\phi}{M} \] (11)

Due to its no accessibility, the rotor current is expressed as a function of the stator current as follows:

\[ \begin{cases} I_{st} = \frac{\phi}{L_r} - \frac{M}{L_r} I_{st} \\ I_{sq} = -\frac{M}{L_r} I_{sq} \end{cases} \] (12)

The second equation of (3) can be written:

\[ I_{sq} = \frac{C_e}{M} \frac{1}{p} \frac{1}{L_r} \phi_r \] (13)

By remplacing (11), (12) and (13) in (10), we obtain:

\[ P_j = K_1 \phi_r^2 + K_2 \frac{C_e^2}{\phi_r^2} \] (14)

where, \( K_1 = \frac{R_s}{M^2} \) and \( K_2 = \frac{R_r L_r^2}{p^2 M^2} + \frac{R_s}{p^2} \).

We obtain a loss equation as a function of the IM parameters, the electromagnetic torque and the rotor flux. The resolution of equation (14) allows us to obtain the optimum flux which ensures minimum losses. To solve this equation, derivative action equation (15), it is also called the sensitivity of the input power [20-24]:

\[ \frac{dP_j}{d\phi_r} = 2K_1 \phi_r - 2K_2 \frac{C_e^2}{\phi_r^3} \] (15)

Finally, the minimization of stator and rotor losses is obtained from the optimized rotor flux \( \phi_{r, opt} \):

\[ \phi_{r, opt} = \left( \frac{K_2}{K_1} \right) \sqrt{C_e} \] (16)

5. FUZZY LOGIC

Most complex industrial systems are difficult to control automatically. These problems are due to nonlinearity and to the variation of the parameters of these systems as well as the quality of the measurable variables. In order to provide a solution to these problems, a new control strategy based on “Fuzzy logic theory” has been developed the origin of the development of this theory was process control based on the expertise of the operator [19, 20]. In a control loop, human reacts like nonlinear robust controller whose parameters vary during the time. This control strategy “Human” needs to know process to order fuzzy controllers can be seen as a case of expert control characterized by the use of a mechanism representing the judgment of the human being [19, 24].

6. DESIGN OF THE FUZZY CONTROLLER

The proposed diagram Figure 20, explains the input and output variables used for optimization system.

The input variables are the torque component \( C_e \) and its variation \( \Delta C \), the output is the Flux component \( \phi_{opt} \) which has the goal of minimizing the copper losses [23, 24]. The Control rules are summarized in Table 3.

<table>
<thead>
<tr>
<th>( C_e )</th>
<th>NH</th>
<th>NM</th>
<th>NS</th>
<th>ZE</th>
<th>PS</th>
<th>PM</th>
<th>PH</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>N</td>
<td>N</td>
<td>NS</td>
<td>ZE</td>
<td>PS</td>
<td>PS</td>
<td>P</td>
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<tr>
<td>ZE</td>
<td>N</td>
<td>N</td>
<td>NS</td>
<td>ZE</td>
<td>PS</td>
<td>P</td>
<td>P</td>
</tr>
<tr>
<td>P</td>
<td>N</td>
<td>NS</td>
<td>NS</td>
<td>ZE</td>
<td>PS</td>
<td>P</td>
<td>P</td>
</tr>
</tbody>
</table>

**Table 3. Fuzzy rules**

As well as the simulation block diagram of this technique which is shown by the Figure 21:

**Figure 20. Membership functions for proposed scheme**

**Figure 21. Flux optimization scheme**
Figure 22. Block diagram of proposed control scheme

To test the efficiency of the proposed scheme (Figures 21, 22), simulations have been done to control the speed at 157rd/s. The induction motor is started with 1Nm, after which a torque load is changed to 7Nm at 0.5s (see Figure 23). The flux is generated by a fuzzy optimiser according to the torque load in order to reduce the losses. The results are compared to those when the flux is maintained to 1. Figure 24, 25, 26, 27, 28, 29, 30 and 31.

Figure 23. Torque profile

Figure 24. Speed response versus time

Figure 25. Torque response versus time

Figure 26. Rotor flux response versus time

Figure 27. Rotor flux response versus time

Figure 28. Phase a stator current response versus time

Figure 29. Phase (A) stator current response versus time

Figure 30. Zoom of Phase (A) stator current (without optimization)
The simulation which gives an optimized efficiency based on the fuzzy logic is performed using Matlab/Simulink®; the parameters of the machine used are given in appendix Table 4. And the results of the simulation are given in figures below.

We start with the evaluation of the efficiency as a function of the load torque for different loads Figure 32 clearly shows the performance efficiency with flux optimization based on fuzzy logic compared to the efficiency without optimization.

Figure 31. Zoom of Phase (A) stator current (with optimization)

Figure 32. Efficiencies for several Loads

The results of Table 4 show us that the efficiency of the machine increases up to 0.9233 for the system with optimization but in the system without optimization it stops at 0.8923. This observation allows us to say that the flux optimization of the machine based on fuzzy logic gave us a good improved efficiency.

Table 4. Efficiency values with optimization and without optimization

<table>
<thead>
<tr>
<th>Load</th>
<th>Without Optimization</th>
<th>With Optimization</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0.5</td>
<td>0.5272</td>
<td>0.9237</td>
</tr>
<tr>
<td>0.9</td>
<td>0.6663</td>
<td>0.9242</td>
</tr>
<tr>
<td>1</td>
<td>0.6889</td>
<td>0.9242</td>
</tr>
<tr>
<td>5</td>
<td>0.9018</td>
<td>0.9233</td>
</tr>
<tr>
<td>20</td>
<td>0.9029</td>
<td>0.9029</td>
</tr>
<tr>
<td>30</td>
<td>0.8923</td>
<td>0.8923</td>
</tr>
</tbody>
</table>

The results clearly show the contribution of the optimized control in the copper losses, the stator currents of the machine evolve around their reference with a much slower dynamic.

The SPWM technique has a high and fixed switching frequency, which is not the case with the technique with hysteresis of the rectified currents. In the proposed technique the switching frequency inverter is optimized and lower than the SPWM. The advantages are a reduction of the electromagnetic torque ripples, reduction of the inverter switching losses and the stator current with optimization with low distortions.

8. CONCLUSIONS

In this paper, a rotor flux oriented vector control of the induction motor is presented. The motor is supplied through two level inverter using a new technique of rectified hysteresis current control. This technique is based on the hysteresis control principle, where the currents of the three phases of the machine are rectified before being controlled by the hysteresis comparator, allowing a low switching frequency operation.

Also, an analytical approach is exposed to minimizing the copper losses of the induction motor. This approach has been addressed and applied to improve the effectiveness of induction motor using a fuzzy logic. The strategy adopted consists to adjust the rotor flux according the value of the load torque to reduce the stator current, thus the optimizing Efficiency.

The results show the utility of efficiency optimization used fuzzy logic, when the machine is associated with rectified currents hysteresis control and confirm largely the effectiveness of the proposed control scheme.

Future research will be oriented towards the implementation of the proposed control on an electric vehicle.

REFERENCES

International Conference on Electronic Measurement & Instruments, pp. 3-866. https://doi.org/10.1109/ICEMI.2009.5274194


**APPENDIX**

<table>
<thead>
<tr>
<th>Table 5. Parameters of induction motor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rate values</td>
</tr>
<tr>
<td>Power  P=4 kW</td>
</tr>
<tr>
<td>Torque Cn=25Nm</td>
</tr>
<tr>
<td>Speed N=1440 rpm</td>
</tr>
<tr>
<td>Current In= 15/8.6A</td>
</tr>
<tr>
<td>Voltage Vs=220/380V</td>
</tr>
</tbody>
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<table>
<thead>
<tr>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stator resistance Rs=1.2Ω</td>
</tr>
<tr>
<td>Rotor resistance Rr=1.8Ω</td>
</tr>
<tr>
<td>Mutual inductance M=0.15H</td>
</tr>
<tr>
<td>Stator inductance Ls=0.1568H</td>
</tr>
<tr>
<td>Rotor inductance Lr=0.1568H</td>
</tr>
<tr>
<td>Inertia J= 0.05kgm²</td>
</tr>
<tr>
<td>Pole pair p=2</td>
</tr>
</tbody>
</table>

**NOMENCLATURE**

| s, r | Rotor and stator indices. |
| d, q | Direct and quadrate indices (synchronous reference) |
| α, β | Direct and quadrate indices (stator reference) |
| Is, Ir | Stator and rotor currents |
| Vs | Stator voltage |
| Rs, Re | Stator and rotor resistances |
| Lo, Lr | Stator and rotor inductances |
| Ts, Tr | Stator and rotor time-constants |
| σ | Leakage flux total coefficient |
| M | Mutual inductance |
| P | Number of pole pairs |
| Ω | Rotor speed (rd/s) |
| ωh | Stator current frequency (rd/s) |
| ωsl | Induced rotor current frequency (rd/s) |
| J | Inertia |
| f | Coefficient of viscous force |
| Cm, Cr | Electromagnetic torque and maximal torque |
| IM | Induction Motor |