

Ingénierie des Systèmes d'Information

Vol. 26, No. 6, December, 2021, pp. 577-584

Journal homepage: http://iieta.org/journals/isi

A Modified Jellyfish Search Optimizer with Opposition Based Learning and Biased Passive Swarm Motion



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https://doi.org/10.18280/isi.260608

Received: 12 October 2021 **Accepted:** 3 December 2021

Keywords:

swarm intelligence, nature inspired optimization, metaheuristic algorithms

ABSTRACT

Jellyfish Search Optimizer (JSO) is one of the latest nature inspired optimization algorithms. This paper aims to improve the convergence speed of the algorithm. For the purpose, it identifies two modifications to form a proposed variant. First, it proposes improvement of initial population using Opposition based Learning (OBL). Then it introduces a probability-based replacement of passive swarm motion into moves biased towards the global best. OBL enables the algorithm to start with an improved set of population. Biased moves towards global best improve the exploitation capability of the algorithm. The proposed variant has been tested over 30 benchmark functions and the real world problem of 10-bar truss structure design optimization. The proposed variant has also been compared with other algorithms from the literature for the 10-bar truss structure design. The results show that the proposed variant provides fast convergence for benchmark functions and accuracy better than many algorithms for truss structure design.

1. INTRODUCTION

Optimization algorithms can be classified in several ways. On the basis of use of random numbers, there are Deterministic and Stochastic Algorithms. Deterministic algorithms provide exact optimum solution every time they run but they are not applicable to complex non-linear problems. Stochastic algorithms are solutions to such problems. Stochastic optimization algorithms deploy heuristic search methods. Based on the number of search particles deployed, they can be Single Solution based or Population based. They are also referred as Metaheuristic Algorithms as these algorithms do not require any information about the nature of the search space and can be implemented on any type of optimization problem. Search methods deployed in these algorithms are often inspired by one or more natural phenomenon or real life process giving them the popular identity as Nature Inspired Algorithms. Some salient features of nature inspired algorithms are listed below:

- (1) They use random numbers and thus may provide a different solution every time they execute.
- (2) The solution may not be the exact optimum but in most cases, it is an acceptable solution.
- (3) Information of the search space is not required. Only the objective function and feasible ranges of the variables are needed.
- (4) Search agents deployed in the feasible space move to improve their location.
- (5) Location of the global best agent is the output of the algorithm.

There is no fixed deterministic rule to move the agents in the space, so each algorithm uses algorithm specific methods to search better values. These search methods involve very high number of evaluations of the objective function and thus require computer based calculations. With the advance of computing capabilities, these algorithms have been able to adopt new sophisticated methods and the number of new nature inspired algorithms has increased many folds in the last few decades. Few popular latest algorithms are Grey Wolf Optimizer [1], Whale Optimization Algorithm [2], Water Strider Algorithm [3] and Black Widow Optimization Algorithm [4].

This paper proposes a modified variant of a recently introduced nature inspired algorithm i.e. Jellyfish Search Optimizer (JSO) [5]. Two modifications are proposed in the basic JSO to form the modified variant.

One of the modifications is Opposition based Learning (OBL). OBL is a learning operator widely used in nature inspired optimization algorithms and other computational intelligence methods. OBL generates a point that is opposite of the given point. The generated point is opposite with respect to the upper and lower limits of the variable. An opposite member O' for a point O with upper and lower limits UL and LL respectively is denoted in Eq. (1).

$$O' = LL + UL - O \tag{1}$$

OBL based learning methods vary on further use of the opposite members, but generally a selection is performed between O and O' to select the better one and drop the other one.

The proposed variant is then validated by solving 30 benchmark functions and the 10-bar truss structure design optimization problem. Rest of the article is structured as follows: Section 2 explains the basic steps of the working of JSO. Section 3 investigates the literature for similar modifications done on other algorithms. Section 4 explains the modifications and the proposed variant. Section 5 presents the experimental results over benchmark functions and discussion. Section 6 shows the proposed variant's implementation to

solve the 10-bar truss design problem. Finally, Section 7 concludes the paper while providing future direction of the work.

2. JELLYFISH SEARCH OPTIMIZER

JSO is inspired by the survival behavior exhibited by Jellyfish in the waters.

Like any other population based nature inspired optimization algorithm, JSO also has three basic steps of Initialization, Generations and Termination. All these steps are explained further.

Step 1: Initialization

JSO uses logistic map to start with an improved set of population. A logistic sequence is generated using Eq. (2).

$$C_{j+1} = 4 \times C_j (1 - C_j) \tag{2}$$

where, j = 1 to ND indicates dimension of the problem and initial value for the sequence $C_0 = rand(0,1)$ but $C_0 \neq \{1|0.75|0.5|0.25\}$. Eq. (2) will create a sequence of ND numbers in the range (0,1).

Then the members of the population are initialized using Eq. (3).

$$X_{i,j} = LL_j + (UL_j - LL_j) \times C_j \tag{3}$$

where, i = 1 to NP the population size.

Step 2: Generation Loops

Each generation updates the location of each member by moving it in the space. A control function c(g) controls the type of movements. For each member, the value of c(g) is calculated by Eq. (4).

$$c(g) = \left| \left(1 - \frac{g}{G_{max}} \right) \times (2 \times rand - 1) \right| \tag{4}$$

where, g is the generation count, G_{max} is the maximum allowed generations and rand is a random number from (0,1).

Based upon the value of c(g), each jellyfish can have two types of movements i.e. ocean current movement and swarm motion.

A jellyfish observes ocean current movement if $c(g) \ge C_{in}$. Ocean currents contribute to exploration capabilities of the algorithm. C_{in} is the coefficient that controls the degree of exploration and exploitation of the algorithm. Eq. (5) expresses the ocean current movement.

$$\begin{aligned} x_i(g+1) &= x_i(g) \\ + rand \times (x_{best} - rand \times \beta \times \frac{\sum_{k=1}^{NP} x_k}{NP}) \end{aligned} \tag{5}$$

where, x_{best} is the member of the population with the best objective value and β is called the distribution coefficient.

If a jellyfish is not observing an ocean current movement, then it undergoes a swarm motion. Swarm motion provides the exploitation power to the algorithm. Swarm motion can be of either Active or Passive type.

If rand > (1 - c(g)) then it performs passive motion, otherwise active motion. Eq. (6) and Eq. (7) express these motions respectively.

$$x_i(g+1) = x_i(g) + (UL - LL) \times \gamma \times rand \tag{6}$$

where, $\gamma > 0$ is the motion coefficient. Passive swarm motion enables a jellyfish to exploit its surroundings for searching better locations.

$$x_{i}(g+1) = \begin{cases} x_{i}(g) + (x_{k} - x_{i}(g)) \times rand, & \text{if } f(x_{k}) \ge f(x_{i}(g)) \\ x_{i}(g) + (x_{i}(g) - x_{k}) \times rand & \text{Otherwise} \end{cases}$$
 (7)

where, k is a randomly chosen index between l to NP and f(x) denotes the objective function value of x. Active swarm motion depicts the movement of a jellyfish towards a better jellyfish in the population. Figure 1 shows the logical sequence of steps for each member in a generation loop.

The updated location of a jellyfish is checked for violation of limits UL and LL. In case of violation, the location is updated to fall inside the limits again. This update is done on the opposite side of the limit. If an updated member violates the upper limit UL_j by Δ_j and is located at $(UL_j + \Delta_j)$ then it is updated to a new location at $(LL_i + \Delta_j)$ in dimension j.

Step 3: Termination

A predefined termination condition is checked after each generation. In all the experiments of this paper, a maximum number of generations (G_{max}) is set as the termination condition.

3. LITERATURE REVIEW

This paper includes Opposition Based Learning (OBL) to improve the convergence speed of JSO. OBL provides an improved initial population to start the generation loops [6]. This initial advantage most of the times affects the quality of the ultimate solution. Literature is rich with the use of OBL as a tool to improve nature inspired algorithms. Most of the work in the literature suggests that OBL is implemented with one or more other tools for enhancement. A part of the literature is reviewed and the findings are presented in Table 1. Details of the additional tools with the OBL are also indicated.

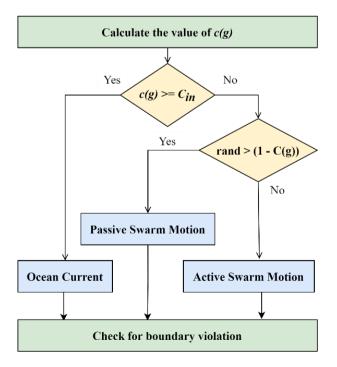


Figure 1. Types of movement inside generation loops

Table 1. Findings of the literature review

Year	Algorithm	Implementation Details	Reference
2021	Elephant Herding Optimization	To overcome the slow convergence of the algorithm due to lack of exploitation component, OBL and position update operator from Sine-cosine algorithm are implemented.	[7]
2021	Class Topper Optimization Along OBL, the paper uses fractional order to update positions. The provides a balance between exploitation and exploration.		[8]
2020	Firefly Algorithm	OBL along with three methods adopted from the working of Dragonfly Algorithm are used to modify Firefly Algorithm to avoid local optimum.	[9]
2020	Salp Swarm Algorithm	OBL and a new local search strategy are used to improve Salp Swarm algorithm for feature selection.	[10]
2020	Crow Search Algorithm	OBL is used to enhance initial population. A cosine function is used to accelerate exploration to avoid local optima.	[11]
2019	Monarch Butterfly Optimization Algorithm	OBL generates an opposite population. Better of the two opposite members is then selected to continue. A Random local Perturbation is then used to improve the migration operator.	[12]
2019	Multifactorial Evolutionary Algorithm	Integration of OBL and DE is used to improve the convergence of the algorithm. Different search territories of DE and OBL along with their complementary nature and the simulated binary crossover are the motivation for the algorithm.	[13]
2019	Dragonfly Algorithm	Selection between a member of the population and its opposite member is performed throughout the execution to continuously improve the solution. The variant has been implemented on multi-level thresholding image segmentation.	[14]
2019	Shuffled Complex Evolution	OBL with an improved competition complex evolution strategy is used to improve accuracy, efficiency and population diversity of the algorithm.	[15]
2018	Grasshopper Optimization Algorithm	First phase of the enhancement generates opposites of the initial population. Second phase improves half of the population in generation loops using OBL.	[16]

4. PROPOSED MODIFIED JSO (MJSO)

Following are two modifications proposed in the structure of basic JSO.

OBL in initialization

OBL is implemented as a tool to improve initial population. Summary of literature review in Table 1 is evident that OBL in initialization step is a proven method of improving convergence. After initialization, using Eq. (3), a set of opposite members X' is generated for the initial set of population X, temporarily having 2NP members. Best NP members are then selected from the set $(X \cup X')$. Figure 2 visualizes this update for 2- dimensional Rastrigin function with initial population size of 10. Figure 2(a) shows the initial population with red circled markers and the opposite member generated for each member as green circled markers. Figure 2(b) shows the best 10 members selected from the union of both the populations.

Improved Passive Swarm Motion

Ocean currents in JSO are aimed at exploration while swarm motion targets exploitation. Coefficient C_{in} trades off the degree of both these capabilities. The time control c(g) of Eq. (4) allows exploratory ocean currents during the initial phase of the execution. As the execution advances, ocean current movements are replaced by swarm motion to increase the degree of exploitation. Among swarm motion, active swarm motion moves keep on increasing with the generation count while passive motion keeps on suppressing. Figure 3 demonstrates the number of all the three types of moves for a typical run of 500 generations in a population of 100 for C_{in} =0.5. Exploitation aims to converge the algorithm.

The movement of jellyfish in passive swarm motion enables it to search its surrounding for better locations. This search is unbiased hence has a low probability of finding better values and thus contributing least to the whole purpose of exploitation. The proposed modification is to add a directional bias to passive swarm motion to enhance convergence. The direction of this bias is kept towards the global best jellyfish x_{best} .

Passive swarm motion is not removed completely but a probability-based method has been deployed to replace some passive swarm motion into biased moves towards global best. A coefficient called Convergence Bias *(CB)* is introduced to control the magnitude of the bias. Mathematically, the passive swarm motion of Eq. (6) is replaced by Eq. (8). Figure 4 demonstrates both these movements.

$$x_i(g+1) =$$

$$\{x_i(g+1) = x_i(g) + (x_{best} - x_i) \times rand, \text{ if } C_B > rand$$

$$\{x_i(g+1) = x_i(g) + (UL - LL) \times \gamma \times rand, \text{ Otherwise } \}$$

$$(8)$$

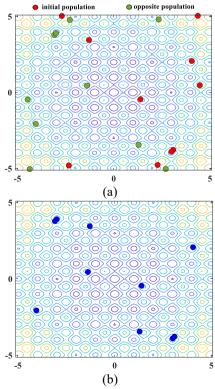


Figure 2. (a) initial population and its opposite population (b) best members from the union of both the population sets

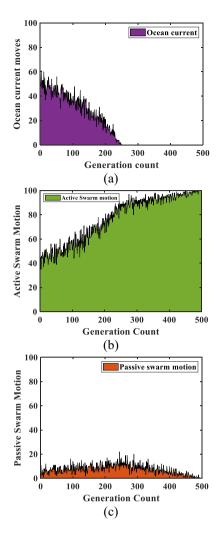


Figure 3. Number of (a) ocean current (b) active swarm and (c) passive swarm movements in a typical run of 500 generations for NP=100 and $C_{in}=0.5$

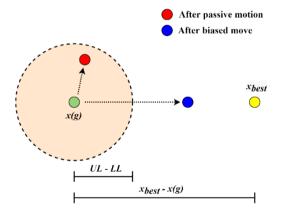


Figure 4. Movement of a jellyfish x(g) in passive swarm motion and proposed biased move

5. EXPERIMENTAL RESULT AND ANALYSIS FOR BENCHMARK FUNCTIONS

The proposed modified variant (MJSO) has been tested over a comprehensive set of 30 diverse benchmark minimization test functions [5]. The set includes both unimodal (f_1 to f_9) and multimodal (f_{10} to f_{30}) functions. Table 2 contains experimental environment details and parameter settings.

Table 2. Experimental environment and parameter settings

Experimental Environment						
Tool	MATLAB R2021a					
Рисседом	Intel(R) Core(TM) i7-8565U CPU					
Processor	@ 1.80GHz					
RAM	16 GB Windows 10					
Operating System						
Parameter Settings						
JSO coefficients C_{in} , γ , β	0.5, 0.1, 3					
Population size (NP)	50					
Maximum generations	500					
(G_{max})	500					
C_B for MJSO	0.25					

Due to the inherent property of randomization of the algorithms, all experiments were repeated for 30 runs. Best and mean objective function values obtained for f_1 to f_{30} along with the standard deviation are provided in Table 3. Necessary details about the functions are also included in Table 3. The source [5] can be referred for more details. Best values among the two algorithms are written in bold text. Mean values are used as the primary criteria for further analysis. Success Rate (SR) is defined as the percentage of functions for which the algorithm performs sole or the joint best. SR is calculated by Eq. (9).

$$= \frac{SR}{\frac{Number\ of\ functions\ the\ algorithm\ performs\ best}{Number\ of\ total\ functions}} \times 100}$$
(9)

JSO and MJSO succeed to be the best algorithms for 18 and 27 functions respectively obtaining SRs of 60% and 90%. For unimodal functions, the algorithms succeed for 4 and 8 functions respectively while for multimodal functions they succeed for 14 and 19 functions. Table 3 provides sufficient evidence to establish that MJSO outperforms JSO for unimodal as well as multimodal functions. Although for majority of functions, both algorithms are successful to find optimum and hence their difference is not visible in Table 3. To visualize convergence speeds, convergence graphs are plotted for all such functions f_1 , f_3 , f_4 , f_{10} , f_{11} , f_{12} , f_{15} , f_{18} , f_{19} , f_{20} , f_{21} , f_{22} , f_{23} , f_{24} and f_{25} in Figure 5. The figure manifests that MJSO provides faster convergence for most of the functions that could not be differentiated in Table 3.

6. 10-BAR TRUSS DESIGN OPTIMIZATION FOR CONTINUOUS DESIGN VARIABLES

Truss structures [17] are a rich class of optimization problems to act as benchmarks for algorithms. Literature has a good number of algorithms implemented to solve problems from the set. The 10-bar truss optimization problem has been optimized by Genetic Algorithm [17], Particle Swarm Optimization [18, 19], Harmony Search [20, 21], Artificial Bee Colony [22] and Teaching Learning based Optimization [23]. A truss is a combination of bars connected at a few joints and is designed to handle certain limits of deflection and stress. Weight of a bar in the truss is a function of its cross section area. After fixing the geometry of the truss, cross section areas of bars become the variables for the optimization problem. Objective of the optimization is to minimize total weight of all the bars put together while stress and deflection limits act as the constraints. Eq. (10) expresses the objective function.

Table 3. Best, mean and standard deviation values of benchmark test functions for JSO and MJSO

unction symbol	Function name			JSO			MJSO	
<u>-</u>	r unction name	Dimension	Best	Mean	Std	Best	Mean	Std
f_1	Stepint	5	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+
f_2	Quartic	30	4.68E-05	3.33E-04	1.67E-04	8.99E-05	3.51E-04	1.78E-0
f_3	Beale	2	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E +
f_4	Easom	2	-1.00E+00	-1.00E+00	0.00E+00	-1.00E+00	-1.00E+00	0.00E+
f_5	Colville	4	1.88E-11	1.34E-06	2.26E-06	1.49E-15	2.19E-08	9.35E-0
J ₅								
f_6	Trid6	6	9.54E-20	2.52E-15	9.36E-15	4.36E-25	2.14E-19	9.07E-1
f_7	Powell	24	1.76E-26	7.50E-08	2.97E-07	2.67E-32	5.87E-10	1.90E-0
f_8	Rosenbrock	30	3.85E-04	1.19E-01	2.55E-01	1.44E-04	6.97E-03	1.24E-0
f_9	Dixon-Price	30	6.26E-03	4.51E-02	4.06E-02	1.66E-03	2.92E-02	3.72E-
f_{10}	Foxholes	2	9.98E-01	9.98E-01	8.25E-17	9.98E-01	9.98E-01	4.12E-
f_{11}	Branin	2	3.98E-01	3.98E-01	0.00E+00	3.98E-01	3.98E-01	0.00E+
	Booth	2	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+
f_{12}								
f_{13}	Rastrigin	30	1.13E-06	3.61E-02	1.90E-01	1.07E-07	1.22E-04	3.64E-
f_{14}	Schwefel	30	-1.16E+04	-8.98E+03	1.44E+03	-1.21E+04	-1.06E+04	1.06E+
f_{15}	Michalewicz2	2	-1.80E+00	-1.80E+00	9.03E-16	-1.80E+00	-1.80E+00	9.03E-
f_{16}	Michalewicz5	5	-4.69E+00	-4.67E+00	1.93E-02	-4.69E+00	-4.65E+00	5.84E-
f_{17}	Michalewicz 10	10	-9.62E+00	-9.50E+00	1.21E-01	-9.66E+00	-9.41E+00	1.83E-
	Shubert	2	-1.87E+02	-1.87E+02	3.68E-11	-1.87E+02	-1.87E+02	2.11E-
f_{18}								
f_{19}	GoldStein-Price	2	3.00E+00	3.00E+00	1.35E-15	3.00E+00	3.00E+00	1.49E-
f_{20}	Kowalik	4	3.07E-04	3.07E-04	8.52E-09	3.07E-04	3.07E-04	2.48E-
f_{21}	Shekel5	4	-1.02E+01	-1.02E+01	1.78E-11	-1.02E+01	-1.02E+01	5.96E-
f_{22}	Shekel7	4	-1.04E+01	-1.04E+01	4.66E-16	-1.04E+01	-1.04E+01	6.60E-
f_{23}	Shekel10	4	-1.05E+01	-1.05E+01	1.55E-15	-1.05E+01	-1.05E+01	9.90E-
f_{24}	Powersum	4	3.89E+00	3.89E+00	2.81E-15	3.89E+00	3.89E+00	1.91E-
f_{25}	Hartman6	6	-3.32E+00	-3.32E+00	1.46E-11	-3.32E+00	-3.32E+00	8.08E-
	Penalized	30	1.45E-11	3.81E-10	6.44E-10	6.35E-12	2.40E-10	4.67E-
f_{26}								
f_{27}	Penalized2	30	6.80E-11	8.13E-09	1.05E-08	2.74E-11	7.12E-09	2.36E-
f_{28}	Fletcher Powell2	2	0.00E+00	1.97E-17	7.59E-17	0.00E+00	5.38E-26	2.37E-
f_{29}	Fletcher Powell5	5	2.09E-13	2.39E+01	1.24E+02	1.54E-18	5.95E+00	1.82E +
f_{30}	FletcherPowell10	10	1.82E-10	4.04E+01	1.30E+02	5.14E-17	1.41E+01	5.09E +
, 50	SR			60%			90%	
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\		0.45					2	1
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10	Generation Count	0.4	Generat	tion Count		Gene	eration Count	400
10	Generation Count $(d)f_{10}$	50 0.4		tion Count 11	30	Gene	eration Count $f)f_{12}$	
10	Generation Count	50 0.4	Generat	tion Count	30	Gene	eration Count () f_{12}	Jso
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10	Generation Count	50 0.4	Generat	tion Count	30 SO 25	Gene	eration Count () f_{12}	Jso
-1.2 -1.3 -1.4	Generation Count	0.4 -100 -120	Generat	tion Count	30 SO 25 20	Gene	eration Count () f_{12}	Jso
-1.2 -1.3	Generation Count	0.4	Generat	tion Count	30 SO 25	Gene	eration Count () f_{12}	Jso
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10 -1.2 -1.3 -1.4 \mathfrak{Z} -1.5 -1.6 -1.7	Generation Count $(d)f_{10}$	-100 -120 -140 -160 -	General (e)f	tion Count 11 JSG MJ	30 25 20 20 21 15	Geno (f	eration Count) f_{12}	JSO MJSO
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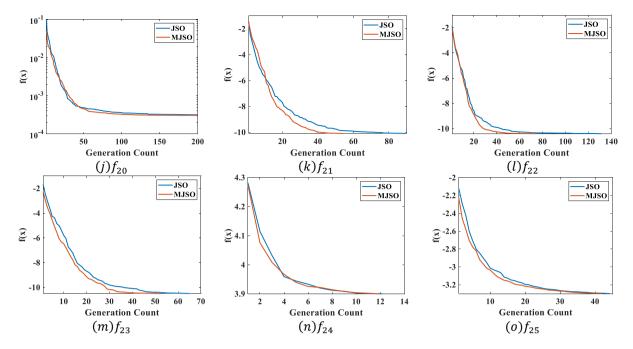


Figure 5. (a)-(o) Comparison of convergence speeds of JSO and MJSO for selected functions

$$Minimize W = \sum_{b=1}^{n} c_b l_b d_b$$
 (10)

Subject to:

$$\sigma_{LL} \le \sigma_h \le \sigma_{HH}$$
 (10.1)

$$\delta_{LL} \le \delta_j \le \delta_{HH} \tag{10.2}$$

$$c_{LL} \le c_b \le c_{HH} \tag{10.3}$$

where, b denotes the bar identifier and b=1 to n. Cross section area, length and density of the material of bar b are denoted by c_b , l_b , and d_b respectively. Stress of bar b and deflection at a joint j are denoted by σ_b and δ_j while σ_{LL} and σ_{HH} represent lower and upper limits of the allowed ranges of all the three constraints in Eqns. (10.1)-(10.3).

Stress penalty for a bar b is computed by Eq. (11).

$$\varphi_{\sigma}^{b} = \begin{cases} 0 & if \ \sigma_{LL} \leq \sigma_{b} \leq \sigma_{HH} \\ \left| \frac{(\sigma_{HH} - \sigma_{LL}) - \sigma_{b}}{(\sigma_{HH} - \sigma_{LL})} \right| & otherwise \end{cases}$$
(11)

Cumulative stress penalty for a design d is calculated by Eq. (12).

$$\varphi_{\sigma}^{d} = \sum_{b=1}^{n} \varphi_{\sigma}^{b} \tag{12}$$

Deflection penalty in each direction x, y and z at a joint j is calculated by Eq. (13).

$$\varphi_{\delta(x,y,z)}^{j} = \begin{cases} 0 & \text{if } \delta_{LL} \leq \delta_{j(x,y,z)} \leq \delta_{HH} \\ \left| \frac{(\delta_{HH} - \delta_{LL}) - \delta_{j(x,y,z)}}{(\delta_{HH} - \delta_{LL})} \right| & \text{otherwise} \end{cases}$$
(13)

Cumulative deflection penalty for a design d of the

structure with m joints is given by Eq. (14).

$$\varphi_{\delta}^{d} = \sum_{i=1}^{m} (\varphi_{\sigma x}^{m} + \varphi_{\sigma y}^{m} + \varphi_{\sigma z}^{m})$$
 (14)

Cumulative penalty for a design d is expressed as given in Eq. (15).

$$P^d = (1 + \varphi_\sigma^d + \varphi_\delta^d)^\varepsilon \tag{15}$$

where, ε is the penalty exponent. The penalized objective function for minimum weight for a design d now becomes as expressed in Eq. (16).

$$F^d = W \times P^d \tag{16}$$

10-bar truss is a cantilever truss with 6 joints. Figure 6 shows geometry of a 10-bar truss structure. The figure shows 10 bars A-J each of length 360 inches. The cross section area for each bar is between 0.1 in^2 and 35 in^2 . The material density (weight/volume) and elasticity are 0.1 lb/in^3 and 107 psi respectively. Maximum allowed stress violation for a bar is $\pm 25 \text{ ksi}$ and maximum allowed deflection at a joint is $\pm 2 \text{ in}$.

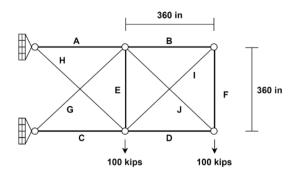


Figure 6. Geometry of 10-bar truss structure

The experiments for 10-bar truss design optimization were conducted for JSO and MJSO for 1000 generations and with all other parameter settings of Table 2. Table 4 contains the results. The table displays the best weight W_{best} obtained and

the cross section areas of all the 10 bars for W_{best} for JSO and MJSO. It also contains average weight W_{avg} , standard deviation of weights W_{std} and the number of objective function evaluation NFE. The table also inherits the results for the same problem from the literature as reported in the reference [23]. It can be observed that on the criterion of W_{best} MJSO outperforms GA, HPSO, SAHS and TLBO. Average weight is given for only three algorithms in the literature and MJSO outperforms PSO.

A comparative convergence graph containing average values of penalized weights for JSO and MJSO is shown in Figure 7. It is evident from the figure that MJSO continuously provides better values than JSO making it a variant that is capable of providing better results at every stage of execution.

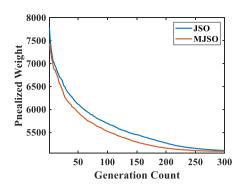


Figure 7. Convergence graph for penalized weight of 10-bar truss design for JSO and MJSO

Table 4. Comparative results for 10-bar truss design optimization for JSO, MJSO and literature

Variable		A	В	С	D	E	F	G
	JSO	30.5030	0.1005	23.1995	15.1241	0.1000	0.5468	21.2243
	MJSO	30.5821	0.1000	23.0505	15.1876	0.1000	0.5528	21.0851
	GA [17]	28.920	0.100	24.070	13.960	0.100	0.560	21.950
	PSO [18]	29.999	0.100	23.268	15.129	0.100	0.554	21.232
Cross section area	HS [20]	30.150	0.102	22.710	15.270	0.102	0.544	21.560
	HPSO [19]	30.704	0.100	23.167	15.183	0.100	0.551	20.978
	ABC [22]	30.548	0.100	23.180	15.218	0.100	0.551	21.058
	SAHS [21]	30.394	0.100	23.098	15.491	0.100	0.529	21.189
-	TLBO [23]	30.6684	0.1000	23.1584	15.2226	0.1000	0.5421	21.0255
Variable		H	I	J	W_{best}	W_{avg}	W_{std}	NFE(×10 ³)
	JSO	7.4820	0.1000	21.4063	5061.0814	5065.1659	7.0011	50
	MJSO	7.4775	0.1000	21.5475	5060.9112	5064.9284	6.5316	50
	GA [17]	7.690	0.100	22.090	5,076.31	-	-	15
	PSO [18]	7.454	0.100	21.670	5,059.85	5067.51	17.509	10.19
Cross section area	HS [20]	7.541	0.100	21.450	5,057.88	-	-	20
	HPSO [19]	7.460	0.100	21.508	5,060.92	-	-	12.5
	ABC [22]	7.463	0.100	21.501	5,060.88	-	-	500
	SAHS [21]	7.488	0.100	21.342	5,061.42	5061.95	0.71	7.081
	TLBO [23]	7.4654	0.1000	21.4660	5,060.973	5064.808	6.3707	13.767

7. CONCLUSION AND FUTURE WORK

The experiments conducted for JSO and the proposed MJSO are sufficient to establish that MJSO outperforms JSO for unimodal, multimodal and truss design optimization. Opposition based learning is a proven tool to improve the efficiency of population based algorithms. Any bias towards global best is expected to improve convergence for unimodal functions but the proposed variant identifies passive swarm motion that can be replaced for biased movements without affecting the convergence for multimodal functions as well. Furthermore, few directions for future work are suggested below:

- (1) To check and possibly improve the performance of JSO on multi-objective problems.
- (2) The proposed work tests biased moves in the passive swarm motion step of JSO. Similar bias can be tested in active swarm motion and the ocean current.
- (3) JSO can be hybridized with other nature-inspired algorithms to develop a hybrid variant that is more efficient.
- (4) Novel real world optimization problems can be identified and JSO can be modified to efficiently solve specific problems.

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