

Free Convection in a Caterpillar Shaped Triangular Enclosure Filled with Different Nanofluids

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ABSTRACT

A numerical work is conducted for the free convection in a right triangular cavity filled with water-based nanofluids. The bottom wall is in a caterpillar wavy shape which is assumed as a hot wall whereas the rest walls of the enclosure are considered as a cold wall. Governing equations of the problem are discretized through the finite volume method. The present study is undertaken to appraise the effect of the constrained parameters i.e. various types of nanofluids (TiO₂, CuO, and Al₂O₃), volume fractions of the nanoparticles and Rayleigh number ($Ra=10^5$ - 10^7). The higher augmentation in the rate of heat transfer is observed for the Al₂O₃-water-based nanofluid for each Rayleigh number.

1. INTRODUCTION

The exploration of the heat transfer through free convection in enclosures with irregular shapes play a prominent role in industrial applications and hence it has become a subject of interest in these present days. However, enclosures like triangular shaped have received a paramount attention in many practical appliances, for example, thermal environment of buildings, solar energy systems, cooling of electronics equipment, geophysics, nuclear power plant, heat exchanger and many other applications involving heat transfer due to its geometry [1-4]. Morsil and Sabeur-Bendehina [5] conducted numerical study for natural convection in a wavy square enclosure. It was reported that the Nusselt number was decreased with the undulations. Bhavnani and Bergles [6] reported the natural convection in the sinusoidal wavy surfaces. It was mentioned that the heat transfer rate was increased by 15 % at amplitude to wavelength ratio of 0.3. Rahman et al. [7] analyzed the effect of buoyancy ratio (Br) and Lewis number (Le) on the heat and mass transfer. On the same cavity, Rahman et al. [8] studied the heat transfer in a corrugated base surface triangular enclosure. Results revealed that both heat and mass transfer was enhanced with the increase of the wavelength and Rayleigh number.

The conventional fluids such as water, air, oil, and ethylene glycol are used as heat conveyance fluids, but it is quite challenging to use these fluids for momentous improvements in the heat transfer because of their inherently poor heat carrying capabilities. On the other hand, emerging applications like microelectronics, micro-electro-mechanical system (MEMS), and nanotechnology offered devices in miniaturized form exaggerates the thermal loads of the system. Hence, to overcome these challenges, the role of heat transport fluids becomes intrinsic in the management of enhanced thermal loads. An innovative technique where small solid nanoparticles which are suspended in the base or pure fluid generally called nanofluid was initially introduced by Choi [9] to reform the drawback of the base fluids. It was

assessed that the increment of the nanoparticles concentrations in base fluid enhances the thermal conductivity of the nanofluid and hence, substantially, the rate of heat transfer. Afterward, plenty of models have been developed to calculate the thermal conductivity of the nanofluid by various researchers [10] so that the heat transfer rate can be enhanced.

Aside from the individual study of the Irregular shapes and nanofluids, some researchers have studied the natural convection in an enclosure with these two parameters together. Esmaeilpour and Abdollahzadeh [11] examined the natural convection in an enclosure filled with nanofluid for different patterns of wavy walls. Shermet et al. [12] studied the natural convection in a wavy open porous cavity filled with nanofluid. Abu-Nada et al. [13] numerically investigated the natural convection in Al₂O₃-water nanofluid filled wavy enclosure. It was found that the adiabatic wavy wall influenced the heat transfer. Sheikholeslami [14] used CuO-water nanofluid in the sinusoidal cavity to investigate the natural convection. Cho et al. [15] numerically analyzed the natural convection in a wavy enclosure filled with water-based nanofluid. Ghasemi and Aminossadati [16] numerically solved a natural convection problem in a right triangular enclosure filled with CuO-water nanofluid. The Brownian motion effects of nanoparticles were considered in the study. They stated that the Brownian motion significantly participated in the thermal performance of the enclosure filled with nanofluid. Later on, Sheikhzadeh et al. [17] also emphasized that the Maxwell-Granet model is not much effective as it does not consider the Brownian motion of the nanoparticles and urged to use the model which consider the Brownian motion. Ghasemi and Aminossadati [18] again conducted a numerical study on mixed convection in right triangular cavity filled with nanofluid. Rahman et al. [19] studied the natural convection in a corrugated base wall triangular shape solar collector filled with different nanofluids. The heat transfer rate was augmented by 24.28 % with 0 to 10 % increment of the volume fraction for Cu-nanofluid at $Gr=10^6$.

The existing literature unveiled that both surface geometry and nanofluids play an essential role in the enhancement of the heat transfer rate. However, the amalgamation of these two i.e. irregular surface and nanofluid can enhance heat transfer process with the significant rate. The concise literature survey also stated that the Maxwell-Garnett (MG) model was used to seek the thermal conductivity [20] but afterward researchers considered the Brownian motion of the nanoparticles for assessment of nanofluid thermal conductivity [16, 18, 21-26]. Triveni and Panua [27] numerically investigated the natural convection in a water-filled the right-angled triangular cavity with caterpillar wavy shape heated base wall. They found that the average Nusselt number was enhanced with the increase of aspect ratio of the wavy shape and found the maximum for width (w) 0.50b and aspect ratio (d) 0.15. Hence, the present work is the extension of this study [27] at the reported width and aspect ratio where the cavity is filled with TiO₂, CuO and Al₂O₃-water based nanofluids. Patel et al. [28] model is espoused for the analysis of thermal conductivity of nanofluid.

2. PROBLEM STATEMENT

A two-dimensional isosceles triangular enclosure of base length b, height H is shown in Figure 1. The caterpillar shape base of the cavity is having a width (w) 0.50b and the height (h) is fixed at 0.075H, thus the caterpillar curve aspect ratio (d) is 0.15. The base wall is presumed at a higher temperature than the side and inclined walls i.e. T_h > T_c. Three different types of nano-scale particles namely TiO₂, CuO, and Al₂O₃ are used to mix with water. The thermo-physical properties of the nanoparticles and pure fluid are shown in Table 1.

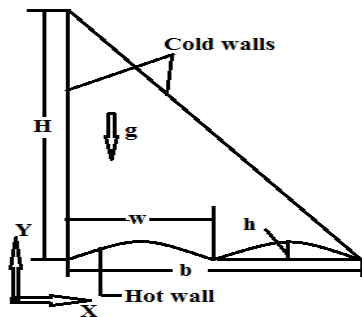


Figure 1. Schematic diagram of problem geometry with coordinate system

Table 1. Thermo-physical properties of nanoparticles and water at Pr=6.2 [21, 22]

Physical Properties	C _p (j/kg k)	ρ (kg/m ³)	k (W/m-k)	β×10 ⁻⁵ (1/k)
TiO ₂	686.2	4250	8.9538	0.9
CuO	540	6500	18	0.85
Al ₂ O ₃	765	3970	40	0.85
Water	4179	997.1	0.613	21

2.1 Mathematical formulation

There are some specific presumptions are formed to prompt the governing equations of the nanofluid. Each wall of the cavity is presumed as impervious. Heat transfer by radiation is efficaciously negligible among the walls. The

flow is assumed Newtonian, incompressible and steady. The nanoparticles and base fluid are presumed thermodynamically balance, no slip occurs between them and both of them are supposed to flow with the same velocity. The variation in the thermal properties of the fluid is assumed unchanged excluding the density variation in the y-direction (Boussinesq approximation). Under these assumptions, the two-dimensional mass, momentum, and energy equations are expressed as [29]:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (1)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial x} + \nu_{nf} \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) \quad (2)$$

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial y} + \nu_{nf} \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) + \frac{(\rho\beta)_{nf}}{\rho_{nf}} g(T - T_c) \quad (3)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha_{nf} \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) \quad (4)$$

where $\alpha_{nf} = k_{nf} / (\rho c_p)_{nf}$

The relative dimensionless parameters and numbers are:

$$X = \frac{x}{H}, Y = \frac{y}{H}, \theta = \frac{T - T_c}{T_h - T_c}, Ra = \frac{g\beta_f(T_h - T_c)H^3}{\alpha_f \theta} \quad (5)$$

The variation in the effective density of the nanofluid at defined Prandtl number and reference temperature can be calculated by:

$$\rho_{nf} = (1 - \varphi)\rho_f + \varphi\rho_{np} \quad (6)$$

in this φ , ρ_{np} , ρ_{nf} and ρ_f are denoted as nanoparticles volume fraction, the density of nanoparticles, the density of nanofluids density and density of the base fluid, respectively. Correspondingly, the coefficient of thermal expansion and heat capacitance can be analyzed by:

$$(\rho\beta)_{nf} = (1 - \varphi)(\rho\beta)_f + \varphi(\rho\beta)_{np} \quad (7)$$

$$(\rho C_p)_{nf} = (1 - \varphi)(\rho C_p)_f + \varphi(\rho C_p)_{np} \quad (8)$$

The effectual thermal conductivity of the nanofluid is calculated through the model proposed by the Patel et al. [24]:

$$\frac{k_{nf}}{k_f} = 1 + \frac{k_{np} A_{np}}{k_f A_f} + cPe \frac{k_{np} A_{np}}{k_f A_f} \quad (9)$$

where k_f is the coefficient of thermal conductivity of the pure fluid, k_{np} is the thermal conductivity of the dispersed nanoparticles and c is the experimental constant which value is to be c=25000. The Peclet number (Pe) and A_{np}/A_f are defined as:

$$Pe = \frac{u_b d_{np}}{\alpha_f}, \frac{A_{np}}{A_f} = \frac{d_{np}}{d_f} \frac{\varphi}{1 - \varphi} \quad (10)$$

u_b is the Brownian motion of the particles which is described by:

$$u_b = \frac{2Tk_b}{\pi\mu_f d_{np}^2} \quad (11)$$

where k_b is the Boltzman Constant ($k_b=1.3807 \times 10^{-23}$ J/K). d_{np} is the diameter of solid particles which taken as ($d_{np}=38$ nm)

and d_f is the size of molecule of the base fluid ($d_f=2A$) [18].

The nanofluid effective viscosity is determined by Brinkman model [30] as below,

$$\mu_{nf} = \frac{\mu_f}{(1-\phi)^{2.5}} \quad (12)$$

The dimensional boundary condition which is used to solve the governing equations is as follows:

$$\begin{aligned} T = T_h, u = v = 0 \text{ at } y = 0 \text{ and } 0 < x < b \text{ for base hot wall} \\ T = T_c, u = v = 0 \text{ at } x = 0 \text{ and } 0 < y < H \text{ for side cold wall} \end{aligned} \quad (13)$$

$$T = T_c, u = v = 0 \text{ at } 0 < x < b \text{ and } 0 < y < H \text{ for inclined cold wall}$$

3. NUMERICAL TECHNIQUES

Finite volume scheme is accompanied to solve the presented governing equations for the associated boundary conditions which are available in commercially obtainable software, FLUENT 6.3 [31]. SIMPLE algorithm and second order upwind technique are involved for pressure-velocity coupling and to discretize the momentum and energy equations. The locally varying heat transfer on the base hot wall can be calculated by local Nusselt number:

$$Nu_x = -\frac{k_{nf}}{k_f} \left(\frac{\partial T}{\partial y} \right)_{y=0} \quad (14)$$

where $\frac{k_{nf}}{k_f}$ is resolute using equation (8). However, the average Nusselt number is defined by:

$$Nu = \int_0^b Nu_x dX \quad (15)$$

The Nu (average) is determined from amended the Nusselt number which is recommended by Yesiloz and Aydin [32] to prevail on the singularity issue in a triangular enclosure:

$$Nu = \left(\int_0^b Nu_x dx \right) \frac{\pi}{2} \quad (16)$$

Relatively, the stream function is demarcated as:

$$u = \frac{\partial \psi}{\partial y}, v = -\frac{\partial \psi}{\partial x} \quad (17)$$

and the dimensionless stream function which is determined from:

$$\Psi = \psi/\alpha \quad (18)$$

3.1 Grid independence check and code validation

The wedge primitive grid shown in Figure 2 has been chosen for the study as this grid system is recommended by Triveni and Panua [27] and yesiloz and Aydin [32]. However, the grid system of 120 x 120 has been adopted for the present problem as Triveni and Panua [27] conducted the study at this grid size which is shown in Table 2.

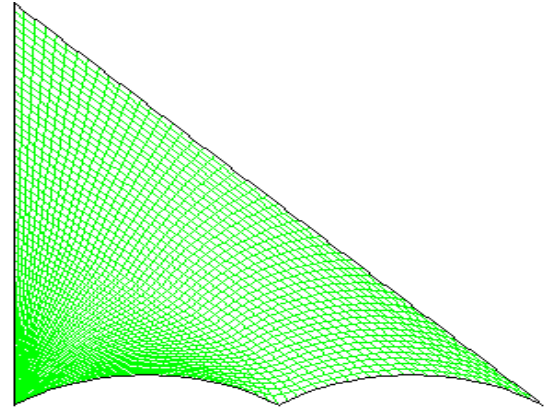


Figure 2. Suggested wedge primitive grid

Table 2. Result of grid independency test

No. of grids in X-Y	Ψ_{max}	Deviation (%)	Nu	Deviation (%)
60x60	36.04		14.95	
80x80	34.62	3.94	15.01	0.40
100x100	33.05	4.53	15.02	0.07
120x120	31.90	3.50	15.05	0.19

The present study is conducted for water filled right triangular cavity retaining the similar boundary conditions at $Ra=10^5$ and $Ra=5 \times 10^5$. The results are validated qualitatively by the available experimental and numerical outcomes of Yesiloz and Aydin [32] as shown in Figures 4 & 5. All the results are validated quantitatively shown in Figures 3, and 4 which unveiled relatively decent matching along with the published results.

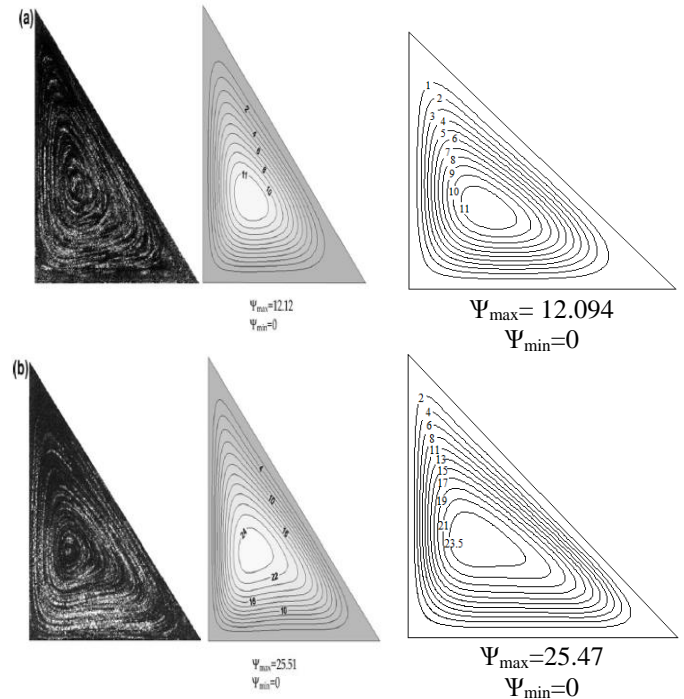


Figure 3. Experimental and Numerical streamlines (left and middle) from Yesiloz and Aydin and numerical simulation (right) from the present study for a) $Ra=10^5$ and b) $Ra=5 \times 10^5$

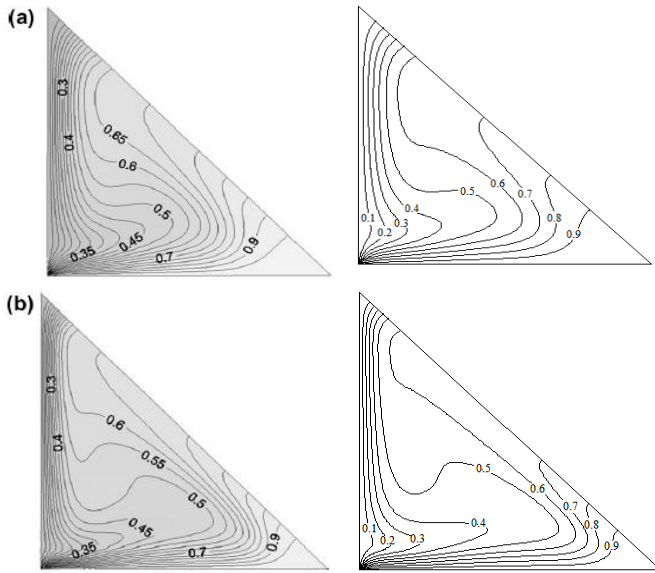


Figure 4. Experimental and Numerical isotherms (left column) from Yesiloz and Aydin and numerical isotherms (right column) from the present study for a) $Ra=10^5$ and b) $Ra=5 \times 10^5$

4. OUTCOMES AND DELIBERATIONS

The analysis of natural convection problem is executed within the right-triangular cavity for various types of nanoparticles (TiO_2 , CuO , and Al_2O_3) mixed with base fluids, a wide range of concentration of nanoparticles ($0.01=\phi=0.04$) and Rayleigh number ($10^5=Ra=10^7$). The flow of fluid is presented by streamlines and the isotherm contours show the heat flow while the rate of transfer of heat is quantitatively shown by means of Nusselt number (local and average).

4.1 The effect of concentration of nanoparticles

Figure 5 encapsulates the consequences of volume fractions in the fluid flow and temperature distributions at $Ra=1 \times 10^6$. It is noted from the figures that three vortices of streamlines are shaped within the cavity for all the volume fractions and out of them the bigger vortex is rotated in counterclockwise while smaller vortices in a clockwise direction. The inner cell of the bigger vortex is elliptic and widened in the case of pure fluid but once the nanoparticles are added to the base fluid, the width of the bigger cell is getting reduced. Similarly, the upper vortex is having two cells in case of pure fluid; the interior cell is becoming smaller and smaller with the intensification of volume fractions and finally, the cell vanishes at $\phi=0.04$. It happens because the viscosity of nanofluid is raised with the increment of nanoparticles concentrations into the base fluid. Nevertheless, the thermal conductivity of the nanofluid is increased with the increase of volume fractions of nanoparticles and therefore, the global heat transfer rate of the cavity is mounted. It is worthy to mention that the increase in viscosity does not signify the full domination of conduction over convection.

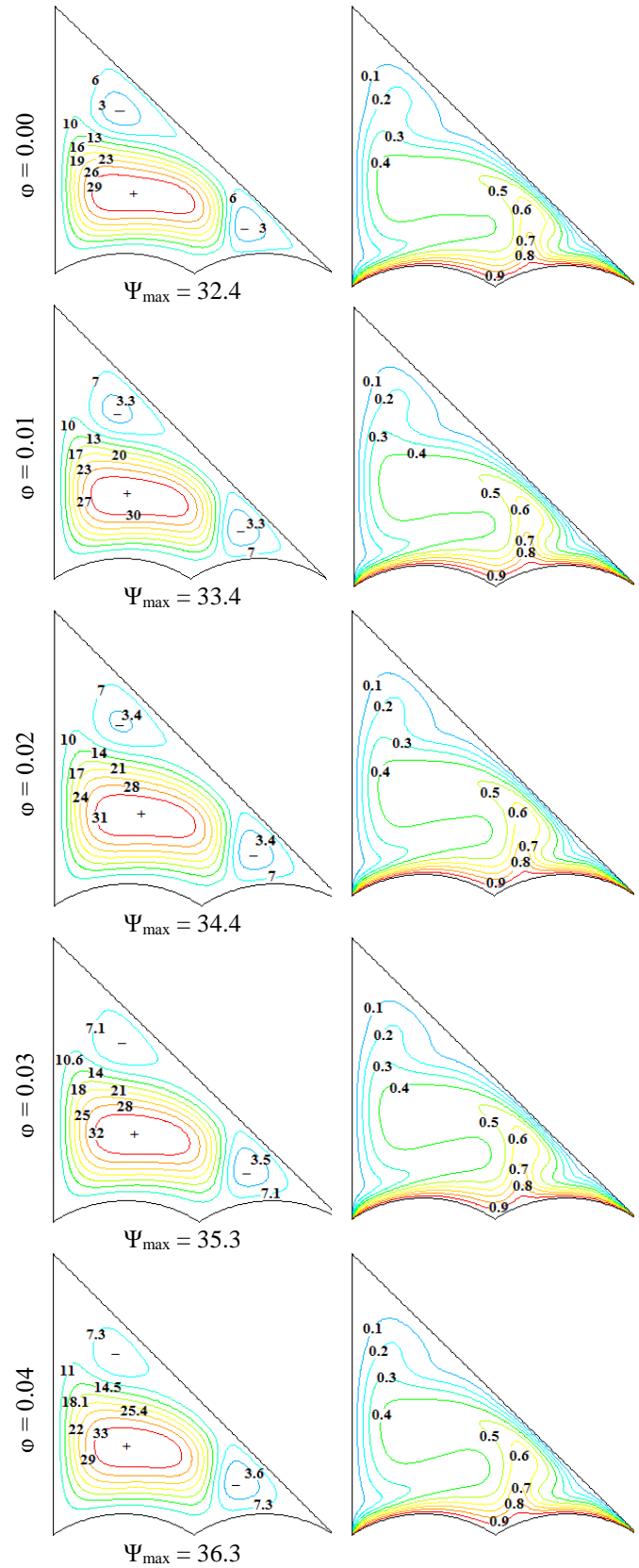


Figure 5. Streamlines (left) and isotherms (right) for different volume fractions of Al_2O_3 at $Ra = 1 \times 10^6$

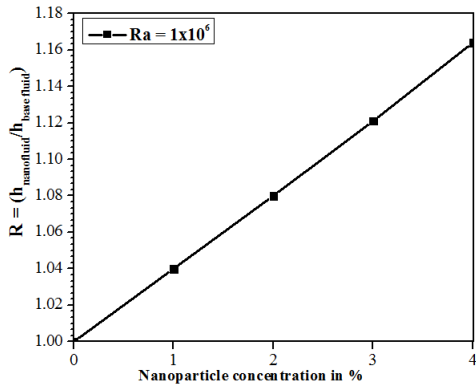


Figure 6. Variation in convection coefficient with nanoparticles concentration of Al_2O_3 at $Ra=10^6$

The convection current of the nanofluid is also increased along with conduction with the increase of nanoparticles concentration as shown in Figure 6 and hence, the stream function of the nanofluid is more than the base fluid. The higher magnitude of stream function ($\Psi_{max}=36.3$) is found for volume fractions $\phi=0.04$ compare to the stream function ($\Psi_{max}=32.4$) of base fluid. Figure 5 shows the variation in the isotherms for different concentration of nanoparticles on the right side. The isotherms are upraised adjacent to the hot wall and concentrated more near the inclined cold wall rather than the side cold wall. It is happening due to the inclination of the wall of the cavity which brings the isothermal walls in closer contact in contrast to the side cold wall. It is remarkable to mention that any variation in the isotherms rarely occurs with the increase of volume fractions.

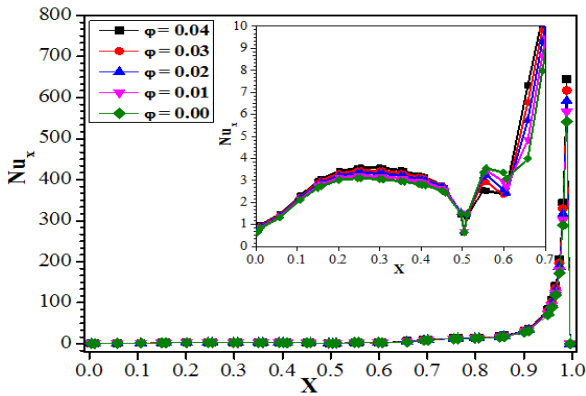


Figure 7. Variation of local Nusselt number with distance for different nanoparticle concentration of Al_2O_3 at $Ra=1 \times 10^6$

Figure 7 displays the variation of local Nusselt number against the bottom wall of the enclosure filled with Al_2O_3 -water nanofluid at $Ra = 1 \times 10^6$. It is observed from the figure that the local Nusselt number is improved with the increase of the nanoparticles concentrations. The increment in the local Nusselt number at the left side of the cavity is according to the shape of the bottom wall but a titanic increase is found at the right side. The peak value of the LNN is calculated 644.5, 617.1, 591.5, 565.9 and 541.8 at the right side edge of the cavity for $\phi=0.04, 0.03, 0.02, 0.01$ and 0.00 respectively. This emphasized that the LNN is enhanced with the escalation of nanoparticles concentrations and this phenomenon is remarkably substantial nearby the right side of the triangular enclosure.

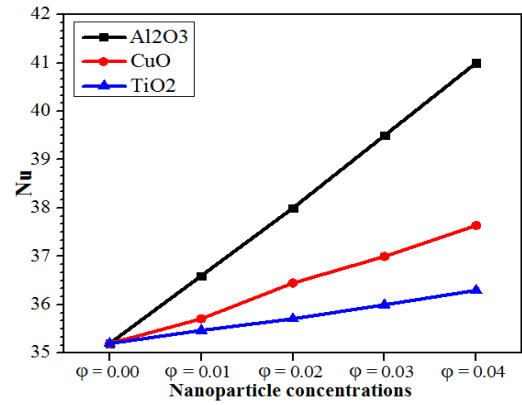


Figure 8. Variation in average Nusselt number variation with volume fraction for different types of nanofluid at $Ra=1 \times 10^6$

The variation of average Nusselt number is plotted against the volume fractions for different nanofluids at Rayleigh number 10^6 which is shown in Figure 8. From the plot, it is observed that the rate of heat transfer is significantly enhanced with the increment of volume fractions of the nanoparticles. However, the percentage variation in average Nusselt can be seen from the Table 3 and 4 which depicts the effect of different types of nanofluids and impact of different concentrations of nanoparticles. It becomes prominently clear that the Al_2O_3 -water nanofluid plays a momentous role in heat transfer compared to CuO and TiO_2 -water nanofluid.

Table 3. Percentage variation of average Nusselt number for different types of nanofluids

		Average Nusselt number		
		TiO_2	CuO	Al_2O_3
$Ra = 1 \times 10^6$	$\phi = 0.01$	35.47	35.71	36.60
	$\phi = 0.00$	35.20	35.20	35.20
	Difference (%)	0.8%	1.5%	4%
	$\phi = 0.02$	35.71	36.45	38.04
	$\phi = 0.00$	35.20	35.20	35.20
	Difference (%)	1.5%	3.6%	8.1%
	$\phi = 0.03$	35.96	37.00	39.45
	$\phi = 0.00$	35.20	35.20	35.20
	Difference (%)	2.2%	5.1%	12.1%
	$\phi = 0.04$	36.30	37.64	40.95
$\phi = 0.00$	35.20	35.20	35.20	
Difference (%)	3.1%	7%	16.3%	

Table 4. Percentage variation of average Nusselt number for different concentrations of nanoparticles

		Average Nusselt number			
		$\phi = 0.01$	$\phi = 0.02$	$\phi = 0.03$	$\phi = 0.04$
$Ra = 1 \times 10^6$	CuO	35.71	36.45	37.00	37.64
	TiO_2	35.47	35.71	35.96	36.3
	Difference (%)	0.7%	2.1%	2.9%	3.7%
	Al_2O_3	36.60	38.04	39.45	40.95
	CuO	35.71	36.45	37.00	37.64
	Difference (%)	2.5%	4.4%	6.6%	8.8%
	Al_2O_3	36.60	38.04	39.45	40.95
	TiO_2	35.47	35.71	35.96	36.3
	Difference (%)	3.2%	6.5%	9.7%	12.8%

4.2 The effects of Rayleigh number

This section, shown in Figure 9, exhibits the deviation of streamlines and isotherms for volume fractions $\phi=0.02$ of CuO at different Rayleigh number. It can be observed from the streamlines that two vortexes are formed inside the enclosure for first two Rayleigh number. The left cell is rotated in anticlockwise while the right cell in a clockwise direction. The flow rotation for the left vortex is higher than the right side vortex. It occurs due to the constriction between the hot and cold wall which restricts the flow motion of the fluid at the nook while this phenomenon is not befallen at the left side of the cavity. The convection current is not strong enough at low Rayleigh number since the buoyancy force is weak. But, as the Rayleigh number is increased, the fluid particles possess high heat energy from the hot wall which makes the buoyancy force stronger. Hence, the flow patterns are changed considerably with the increase of Rayleigh number. In the last three Rayleigh number, the streamlines get fragmented into three vortexes, and the value of stream function is increased accordingly. The extreme value of stream function ($\Psi_{\max}=75.6$) is found at higher Rayleigh number while at lower Ra, the stream function is calculated $\Psi_{\max}=21.7$. The corresponding isotherms are moved away from each other at lower Rayleigh number. These are not in fully touched with the cold walls and situated far away from the upper corner of the enclosure. The isotherms are analogous to each other near the hot wall, come closer to each other and grow up towards the upper edge of the triangular cavity with the increase of Rayleigh number. The isotherms with $\theta < 0.6$ are getting clustered near the cold walls as the Rayleigh number is increased, while, the isotherms with $\theta > 0.6$ are stick to the hot wall at higher Rayleigh number. This explicates that the fluid flow rate is being intensified along with the escalation of Rayleigh number and hence the rate of heat transfer is uplifted.

Figure 10 illustrates the effect of Rayleigh number on the local Nusselt number for $\phi=0.02$ of CuO. The local Nusselt number is varied according to the shape of the hot wall with the variation of Rayleigh number. It is conspicuous to indicate that the local Nusselt number is observed maximum at the crest of the caterpillar curve for higher Rayleigh number. At the right side of the cavity, heat transfer by conduction is well prevailed since some fluid particles get stuck due to the compactness at the corner while beside the corner, heat transfer is occurred due to the convection. That is why the local heat transfer rate is highly pronounced at the right corner of the cavity. The extreme value of local Nusselt number is obtained ($Nu_x=565.192$) at $Ra=1 \times 10^7$.

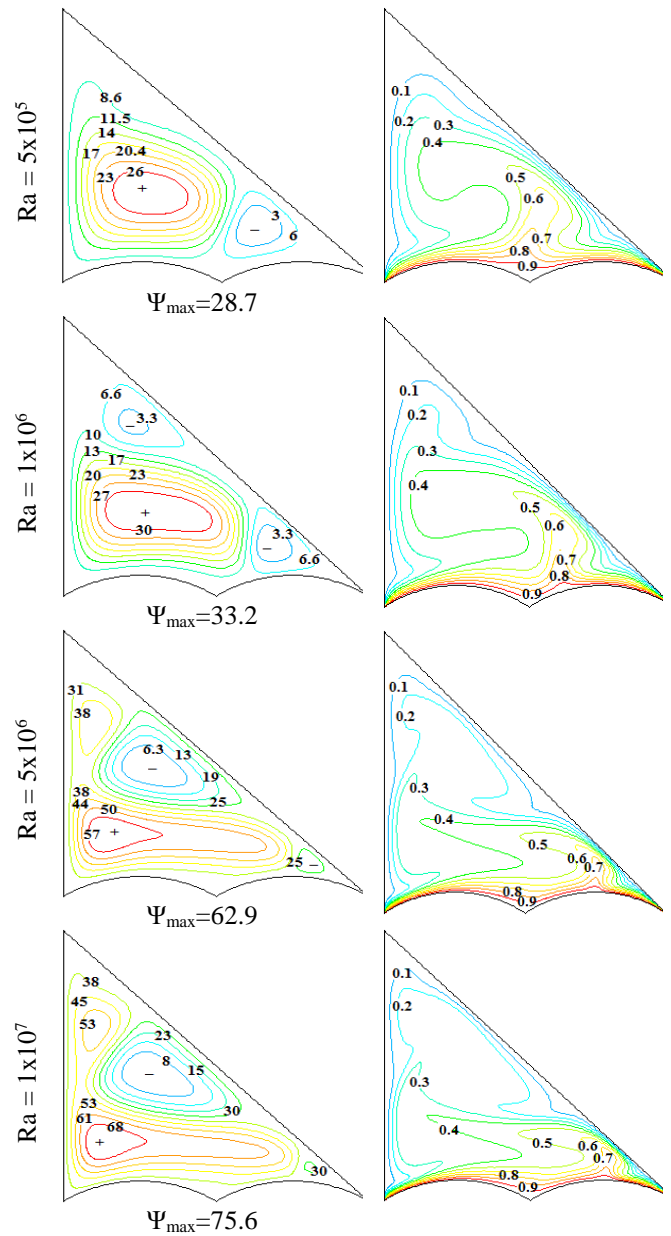
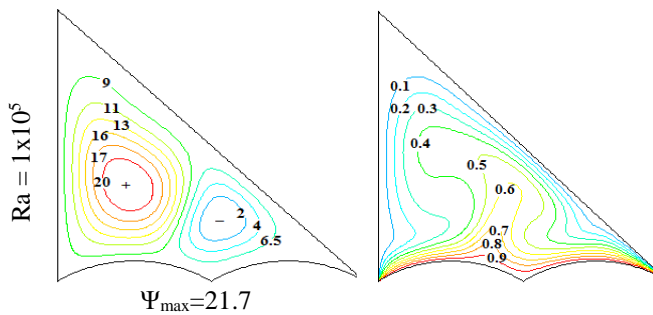


Figure 9. Streamlines (left) and isotherms (right) for different Rayleigh number at $\phi=0.02$ of CuO

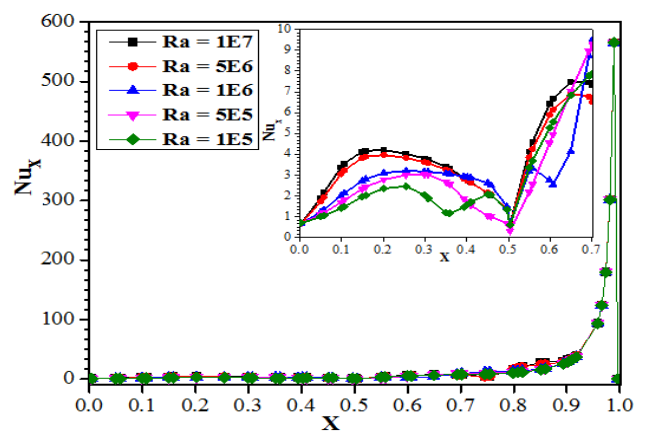


Figure 10. Local Nusselt number along with hot wall for different Rayleigh number for $\phi=0.02$ of CuO

Figure 11 (a, b and c) depicts the plot of Nu against Ra for various nanofluids. In the case of TiO_2 -water nanofluid, the

heat transfer rate is increased with Ra but the rate of heat transfer is not augmented in considerable amount with the increase of the percentage of nanoparticles volume fractions. But, the considerable improvement in average Nusselt number is found for Al₂O₃-water nanofluid. The variation can also be observed from the Table 5-7. From the data, it is clear that the average Nusselt number is enhanced with the increase of Rayleigh number but the percentage increment in heat transfer rate is decreased with the increase of Rayleigh number.

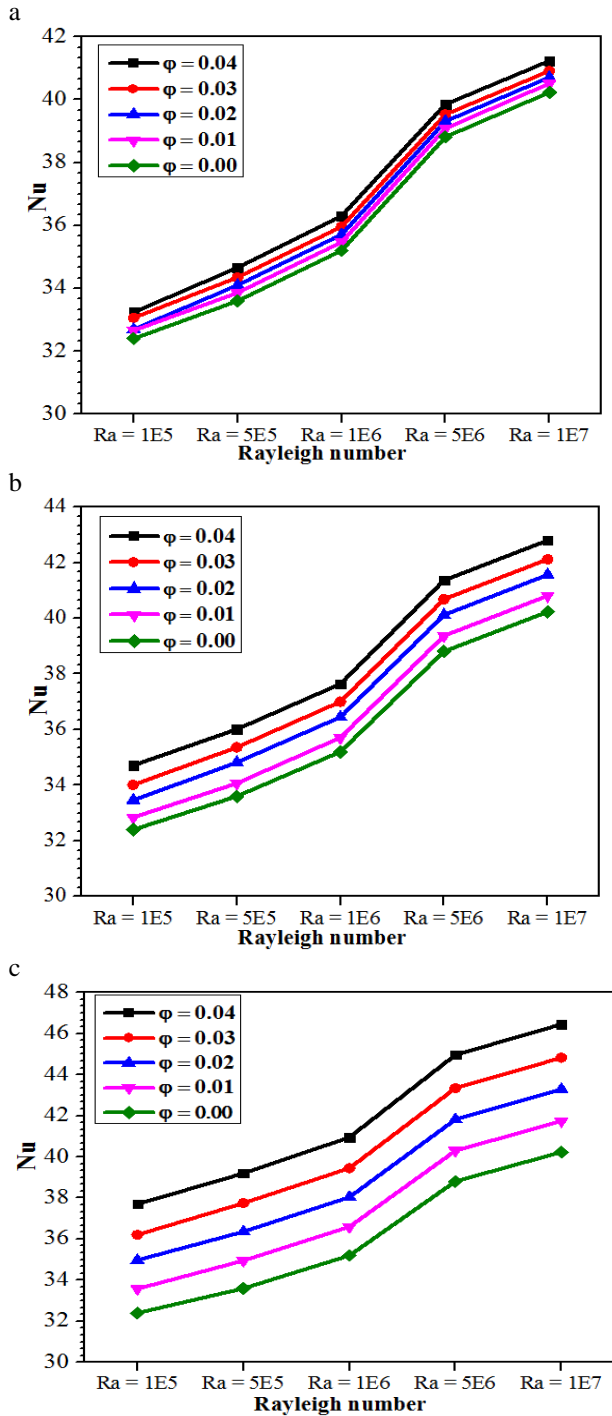


Figure 11. Average Nusselt number with Rayleigh number for a) TiO₂, b) CuO and c) Al₂O₃

Table 5. Percentage variation of average Nusselt number for TiO₂-water nanofluids

	Average Nusselt number				
	water	TiO ₂			
	$\phi = 0.00$	$\phi = 0.01$	$\phi = 0.02$	$\phi = 0.03$	$\phi = 0.04$
Ra = 5x10 ⁵	33.60	33.86	34.10	34.35	34.66
Ra = 1x10 ⁵	32.40	32.66	32.70	33.06	33.24
Difference (%)	3.7%	3.7%	4.3%	4%	4.3%
Ra = 1x10 ⁶	35.20	35.47	35.71	35.96	36.30
Ra = 1x10 ⁵	32.40	32.66	32.70	33.06	33.24
Difference (%)	8.6%	8.6%	9.2%	8.8%	9.2%
Ra = 5x10 ⁶	38.81	39.1	39.31	39.53	39.85
Ra = 1x10 ⁵	32.40	32.66	32.70	33.06	33.24
Difference (%)	19.8%	19.7%	20.2%	19.6%	20%
Ra = 1x10 ⁷	40.23	40.51	40.71	40.91	41.23
Ra = 1x10 ⁵	32.40	32.66	32.70	33.06	33.24
Difference (%)	24.2%	24%	24.5%	23.7%	24%

Table 6. Percentage variation of average Nusselt number for CuO-water nanofluids

	Average Nusselt number				
	water	CuO			
	$\phi = 0.00$	$\phi = 0.01$	$\phi = 0.02$	$\phi = 0.03$	$\phi = 0.04$
Ra = 5x10 ⁵	33.60	34.07	34.82	35.36	36.10
Ra = 1x10 ⁵	32.40	32.84	33.46	34.01	34.72
Difference (%)	3.7%	3.7%	4%	4%	4%
Ra = 1x10 ⁶	35.20	35.71	36.45	37.00	37.64
Ra = 1x10 ⁵	32.40	32.84	33.46	34.01	34.72
Difference (%)	8.6%	8.7%	9%	8.8%	8.4%
Ra = 5x10 ⁶	38.81	39.38	40.12	40.70	41.37
Ra = 1x10 ⁵	32.40	32.84	33.46	34.01	34.72
Difference (%)	19.8%	19.9%	19.9%	19.7%	19.2%
Ra = 1x10 ⁷	40.23	40.81	41.56	42.12	42.80
Ra = 1x10 ⁵	32.40	32.84	33.46	34.01	34.72
Difference (%)	24.2%	24.3%	24.2%	23.8%	23.3%

Table 7. Percentage variation of average Nusselt number for Al₂O₃-water nanofluids

	Average Nusselt number				
	water	Al ₂ O ₃			
	$\phi = 0.00$	$\phi = 0.01$	$\phi = 0.02$	$\phi = 0.03$	$\phi = 0.04$
Ra = 5x10 ⁵	33.60	34.95	36.36	37.75	39.20
Ra = 1x10 ⁵	32.40	33.58	34.97	36.21	37.70
Difference (%)	3.7%	4%	4%	4.3%	4%
Ra = 1x10 ⁶	35.20	36.60	38.04	39.45	40.95
Ra = 1x10 ⁵	32.40	33.58	34.97	36.21	37.70
Difference (%)	8.6%	9%	8.8%	8.9%	8.6%
Ra = 5x10 ⁶	38.81	40.30	41.82	43.34	44.96
Ra = 1x10 ⁵	32.40	33.58	34.97	36.21	37.70
Difference (%)	19.8%	20%	19.6%	19.7%	19.3%
Ra = 1x10 ⁷	40.23	41.74	43.28	44.82	46.45
Ra = 1x10 ⁵	32.40	33.58	34.97	36.21	37.70
Difference (%)	24.2%	24.3%	23.8%	23.8%	23.2%

5. CONCLUSIONS

A detailed study of free convection has been conducted numerically in caterpillar shape right triangular cavity filled with pure fluid water and different type nanofluids. The aspect ratio (d) of the caterpillar curvature is maintained at 0.15 for the present study. Three different types of nanoparticles such as TiO_2 , CuO , and Al_2O_3 , the different volume fraction of the nanoparticles and different Rayleigh number have been used to emphasize the effect of the parametric study.

- The fluid flow is diminutively changed with the variation of the volume fraction of the nanoparticles.
- The fluid flow is followed the same flow pattern for all three nanofluids at fixed Rayleigh number.
- The augmentation in the rate of heat transfer occurs with the increment of volume fraction for all nanofluids.
- The Nu is obtained higher for Al_2O_3 –water nanofluid followed by CuO and TiO_2 respectively. The percentage rate of heat transfer is found very less for TiO_2 –water nanofluid.
- The rate of heat transfer for nanofluids is very much significant at a lower value of Rayleigh number than the higher Rayleigh number.
- The heat transfer rate is enhanced for all Rayleigh number.

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NOMENCLATURE

g	acceleration due to gravity in m/s ²
H	vertical length in m
b	horizontal length in m
s	inclination extent in m
h	apex of the caterpillar curve in m
w	breadth of the curvature in m
n	perpendicular direction to the plane
A	area in m ²
d	diameter in m
p	pressure in N/m ²
u,v	velocity components in m/s
u _b	Brownian motion velocity in m/s
x,y	Cartesian co-ordinates system
T	temperature in K
T _h	temperature of hot wall in K
T _c	temperature of cold wall in K
Pr	Prandtl number
Gr	Grashof number
Pe	Peclet number
Nu _x	Nusselt number (Local)
Nu	Nusselt number (Average)

Greek symbols

α	thermal diffusivity in m ² /s
β	coefficient of thermal expansion in 1/K
k	conduction coefficient in w/mK
ρ	density in Kg/m ³
μ	dynamic viscosity in N-s/m ²
ν	kinematic viscosity in m ² /s
ψ	stream function in Kg/s
δ	curvature aspect ratio (h/w)
Ψ	dimensionless stream function

Subscripts

h	hot wall
c	cold wall
f	basefluid
np	nanoparticle
nf	nanofluid