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Mass Transfer Effect on a Rotating MHD Transient Flow of Liquid Lead Through a Porous Medium in Presence of Hall and Ion Slip Current with Radiation

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https://doi.org/10.18280/mmep.080117	ABSTRACT
Received: 9 January 2020 Accepted: 14 November 2020	A problem of unsteady MHD convective flow of liquid lead through an impulsively started semi infinite vertical porous plate in presence of a transversely applied uniform
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Keywords:

hall current, ion slip current, heat and mass transfer

A problem of unsteady MHD convective flow of liquid lead through an impulsively started semi infinite vertical porous plate in presence of a transversely applied uniform magnetic field under the effects of Hall current, ion slip current and chemical reaction is investigated. The fluid is considered to be incompressible while the magnetic Reynolds number is assumed to be very small. An exact solution to the flow model is obtained adopting Laplace Transform Technique in closed form. The effects of the relevant physical parameters on the velocity field, temperature field and concentration field are displayed graphically and the effects on skin friction, Nusselt number and Sherwood number are presented in tabular form.

1. INTRODUCTION

Hall Effect is not considered in the generalized Ohm's law. But in a situation when the applied magnetic field is very strong, the inclusion of Hall Effect in the generalized Ohm's law is necessary. It is the deflection of the electric charges due to the electromagnetic force and so a new component of the current density vector needs to be considered. So the equation of the electric current density is derived from the diffusion velocity of electrons so as to include the Hall current rather than considering only the electromagnetic forces. Current research works in MHD trend towards a strong magnetic field which is to be addressed by considering Hall current. Cowling [1] first emphasized on the modification of Ohm's law to include Hall current when dealing with a strong magnetic field. Pop [2] analyzed the MHD convection flow near an accelerated plate incorporating the effects of Hall current. The importance of Hall Effect in the Hartmann channel flow has been indicated by Cramer and Pai [3]. Ahmed and Sarmah [4] have studied the unsteady MHD rotational flow past an impulsively started infinite horizontal porous plate with Hall current. Seth et al. [5] have investigated the effects of Hall current and rotation on the free convective MHD flow past a suddenly started moving vertical plate. Seth et al. [6] later studied the Hall current effects on unsteady MHD rotating natural convection free stream flow with exponential acceleration past a vertical plate.

Usually diffusion velocity of ions is neglected as it is much smaller than that of electrons when considering current density. But a strong electromagnetic force demands to consider the diffusion velocity of ions as well. The ion slip current is due to the diffusion velocity of ions. Mohanty [7] studied the hydromagnetic Rayleigh problem with Hall Effect. Soundalgekar et al. [8] have studied the Hall and ion slip effects on the MHD Couette flow with consideration of heat transfer phenomenon. Hall and ion slip current effects on MHD convective three dimensional flow of liquid metal with rotation was studied by Ghosh et al. [9]. Sheikh and Ahmed [10] have studied the effects of radiation, Hall current and ion slip current on the rotating MHD transient flow of liquid metal through a porous medium.

Study of combined heat and mass transfer has its own relevance since many industrial, scientific processes and natural events are associated with this phenomenon. Mass transfer process does have the impact on heat transfer. Diffusion of Chemical species affects the flow properties of the fluid also. Eckert and Drake [11] and some other researchers made significant contributions to the studies of heat and mass transfer problems. Because of its increasing relevance, further researches were carried out in the following years by many authors. Some names in this regard are Raptis et al. [12], Acharya et al. [13], Reddy et al. [14], Lavanya and Leela Ratnam [15].

Our objective in the present work is to study the mass transfer phenomenon on the unsteady MHD rotating convective flow under the effects of Hall and ion slip current in presence of thermal radiation.

2. MATHEMATICAL ANALYSIS

We consider the transient convective motion of an incompressible, viscous, partially ionized fluid past a semiinfinite plate through a porous medium. A rectangular Cartesian co-ordinate system is introduced so that the vertically upward direction along the plate becomes the X' axis, the perpendicular to the X' axis in the plate's plane becomes the Y axis and Z' axis is along the normal to the X'Y' plane directed towards the fluid region. The flow geometry is given below in Figure 1.

It is assumed that the fluid as well as the plate is rotating about the Z' axis with uniform angular velocity $\vec{\omega}$. A strong magnetic field \vec{B} of intensity B_0 is applied to the system in the positive Z' direction that is transversely to the plane of the flow. At time *t*'=0, the plate temperature is same with the free stream fluid temperature T'_{∞} and concentration at the plate is assumed to be equal with the free stream fluid concentration C'_{∞} . At time *t*'>0, due to the application of an impulsive force, the plate velocity, temperature at the plate and the concentration at the plate rise suddenly to U_0, T'_w and C'_w respectively which remain constant throughout the motion.



Figure 1. Physical model of the problem

The magnetic Reynolds number in the problem is assumed to be very small. Due to this assumption, the induced magnetic field is ignored in this investigation. But in view of the relative motion of the particles in the partially ionized fluid, Hall current is considered in this study. With magnetic field \vec{B} and electrical field \vec{E} acting in directions perpendicular to each other, the electromagnetic Lorentz force acts in a direction perpendicular to both \vec{B} and \vec{E} , causing the charged particles to drift in that direction. Consequently, the current density vector \vec{J} will have a component in that direction, known as the Hall current. Further, the intensity B_0 of the applied magnetic field is strong enough to consider the diffusion velocity of the ions, causing the ion-slip current. Taking into account the Hall current and ion-slip effect, following Sherman and Sutton [16], the electric current density vector $\vec{J} = (J_{x'}, J_{y'}, J_{z'})$ is taken as:

$$J_{x'} = \left[\alpha_1 \left(E_{x'} + B_0 V' \right) - \beta_1 \left(E_{y'} - B_0 U' \right) \right] \sigma$$

$$J_{y'} = \left[\alpha_1 \left(E_{y'} - B_0 U' \right) + \beta_1 \left(E_{x'} + B_0 V' \right) \right] \sigma$$

$$J_{z'} = 0 \left(\begin{array}{c} \text{since the plate is taken electrically} \\ \text{non-conducting} \end{array} \right)$$

where, $\alpha_1 = \frac{1+\beta_i\beta_e}{(1+\beta_i\beta_e)^2+(\beta_e)^2}$ and $\beta_1 = \frac{\beta_e}{(1+\beta_i\beta_e)^2+(\beta_e)^2}$

The porous medium is assumed to be homogeneous and isotropic. This assumption allows us to use a single permeability for the porous medium in the simulation of hydrolic conductivity. The pressure gradient across the fluid medium is defined on the basis of Darcian drag force model as: $\nabla p = -\frac{\mu \vec{q}}{\kappa_p^*}$.

Due to the above assumptions, the Equations governing the flow and the heat and mass transfer characteristics can now be written as (neglecting the convective acceleration terms):

$$\rho\left(\frac{\partial U'}{\partial t'} - 2\omega V'\right) = \mu \frac{\partial^2 U'}{\partial z'^2} - \frac{\partial p}{\partial x'} + J_{y'} B_0 - \frac{\mu U'}{K_p^*} - \rho g \qquad (1)$$

$$\rho\left(\frac{\partial V'}{\partial t'} + 2\omega U'\right) = \mu \frac{\partial^2 V'}{\partial z'^2} - \frac{\partial p}{\partial y'} - J_{x'} B_0 - \frac{\mu V'}{K_p^*}$$
(2)

$$\frac{\partial T'}{\partial t'} = \frac{\kappa}{\rho C_p} \frac{\partial^2 T'}{\partial {z'}^2} - \frac{4I}{\rho C_p} \left(T' - T_{\infty}' \right) \tag{3}$$

$$\frac{\partial C'}{\partial t'} = D_M \frac{\partial^2 C'}{\partial z'^2} + K_1 \left(C'_{\infty} - C' \right) \tag{4}$$

In Eq. (3), $I = \int_0^\infty (a_\lambda)_w \left(\frac{\partial e_{\lambda h}}{\partial T'}\right) d\lambda$. In the free stream, U=V=0, $\rho = \rho_\infty$. Thus Eqns. (1) and (2)

In the free stream, U=V=0, $\rho = \rho_{\infty}$. Thus Eqns. (1) and (2) take the form:

$$\frac{\partial p}{\partial x'} = \left(\alpha_1 E_{y'} + \beta_1 E_{x'}\right) B_0 \sigma - \rho_\infty g \tag{5}$$

$$\frac{\partial p}{\partial y'} = \left(\beta_1 E_{y'} - \alpha_1 E_{x'}\right) B_0 \sigma \tag{6}$$

Implementation of the equation of state according to Bousinnesq approximation gives:

$$\rho_{\infty} = \rho + \rho \beta \left(T' - T'_{\infty} \right) + \rho \beta^* \left(C' - C'_{\infty} \right) \tag{7}$$

Due to (5), (6) and (7); Eqns. (1) and (2) now can be written as:

$$\frac{\partial U'}{\partial t'} - 2\omega V' = \nu \frac{\partial^2 U'}{\partial z'^2} + \frac{B_0^2 \sigma}{\rho} (\beta_l V' - \alpha_l U') - \frac{\nu U'}{K_p^*} + \beta g (T' - T_{\infty}') + \beta^* g (C' - C_{\infty}')$$
(8)

$$\frac{\partial V'}{\partial t'} + 2\omega U' = \nu \frac{\partial^2 V'}{\partial z'^2} - \frac{B_0^2 \sigma}{\rho} \left(\beta_1 U' + \alpha_1 V'\right) - \frac{\nu V'}{K_p^*} \tag{9}$$

Now introducing two complex variables q'=U'+iV' and $\alpha_0 = \alpha_1 + i\beta_1$, momentum conservation equations represented by (8) and (9) are combined together to transform into a single equation given by (10):

$$\frac{\partial q'}{\partial t'} + 2i\omega q' = v \frac{\partial^2 q'}{\partial z'^2} - \frac{B_0^2 \sigma \alpha_0}{\rho} q' - \frac{v q'}{K_p^*} + \beta g \left(T' - T_{\infty}'\right) + \beta^* g \left(C' - C_{\infty}'\right)$$
(10)

The initial and boundary conditions for the momentum conservation Eq. (10), energy conservation Eq. (3) and the species continuity Eq. (4) are assumed as:

$$t' \le 0, z' = 0: q' = 0(U' = 0, V' = 0), T' = T'_{\infty}, C' = C'_{\infty}$$

$$t' > 0, z' = 0: q' = U_0 (U' = U_0, V' = 0), T' = T'_w, C' = C'_w$$

$$t' > 0, z' \to \infty: q' \to 0(U' \to 0, V' \to 0), T' \to T'_{\infty}, C' \to C'_{\infty}$$
(11)

For the sake of idealization of the problem, the following non-dimensional quantities are introduced:

$$U = \frac{U'}{U_{0}}, V = \frac{V'}{U_{0}}, q = \frac{q'}{U_{0}}, t = \frac{t'U_{0}^{2}}{v}, z = \frac{z'U_{0}}{v}$$

$$\theta = \frac{T' - T'_{\infty}}{T'_{w} - T'_{\infty}}, \phi = \frac{C' - C'_{\infty}}{C'_{w} - C'_{\infty}}$$

$$Gr = \frac{g\beta v (T' - T'_{\infty})}{U_{0}^{3}}, Gm = \frac{g\beta' v (C' - C'_{\infty})}{U_{0}^{3}}$$

$$Er = \frac{\omega v}{U_{0}^{2}}, Nm^{2} = \frac{B_{0}^{2} v \sigma}{\rho U_{0}^{2}}, Da = \frac{K_{p}^{*}}{L^{2}}, Re = \frac{U_{0}L}{v}$$

$$N = \frac{4Iv}{\rho C_{p} U_{0}^{2}}, Pr = \frac{\mu C_{p}}{\kappa}, K = \frac{K_{1}v}{U_{0}^{2}}, Sc = \frac{v}{D_{M}}$$
(12)

By the aid of (12), Eqns. (10), (3) and (4) are idealized as follow:

$$\frac{\partial q}{\partial t} = \frac{\partial^2 q}{\partial z^2} + \operatorname{Gr} \theta + \operatorname{Gm} \phi - aq$$
(13)

$$\frac{\partial \theta}{\partial t} = \frac{1}{\Pr} \frac{\partial^2 \theta}{\partial z^2} - N\theta \tag{14}$$

$$\frac{\partial \phi}{\partial t} = \frac{1}{\mathrm{Sc}} \frac{\partial^2 \phi}{\partial z^2} - K\phi \tag{15}$$

Corresponding idealized initial and boundary conditions are:

$$t \le 0, z = 0: q = 0, \theta = 0, \phi = 0$$

$$t > 0, z = 0: q = 1, \theta = 1, \phi = 1$$

$$t > 0, z \to \infty: q \to 0, \theta \to 0, \phi \to 0$$
(16)

3. METHOD OF SOLUTION

We have adopted Laplace transformation technique in closed form to find solutions for velocity field, temperature field and concentration field. Laplace transforms of the governing Eqns. (13), (14), (15) and the initial and boundary conditions (16) are as follow:

$$\frac{d^2 \bar{q}}{dz^2} - (s+a)\bar{q} = -\mathrm{Gr}\bar{\theta} - \mathrm{Gm}\bar{\phi}$$
(17)

$$\frac{d^2\bar{\theta}}{dz^2} - \Pr(s+N)\bar{\theta} = 0$$
(18)

$$\frac{d^2\bar{\phi}}{dz^2} - \operatorname{Sc}(s+K)\bar{\phi} = 0 \tag{19}$$

$$t \le 0, z = 0: \overline{q} = 0, \overline{\theta} = 0, \overline{\phi} = 0$$

$$t > 0, z = 0: \overline{q} = \frac{1}{s}, \overline{\theta} = \frac{1}{s}, \overline{\phi} = \frac{1}{s}$$

$$t > 0, z \to \infty: \overline{q} \to 0, \overline{\theta} \to 0, \overline{\phi} \to 0$$

$$(20)$$

Here $\overline{f}(z, s)$ denotes Laplace transform of f(z,t). Solving (17), (18) and (19) subject to (20), the following solutions are obtained:

$$\overline{q} = \left[\frac{1}{s} + \frac{1}{s}\left(\frac{B_1}{s - D_1} + \frac{E_1}{s - F_1}\right)\right] e^{-z\sqrt{s + a}} - \frac{1}{s}\left[\frac{B_1 e^{-z\sqrt{\Pr(s + N)}}}{s - D_1} + \frac{E_1 e^{-z\sqrt{\sec(s + K)}}}{s - F_1}\right]$$
(21)

$$\overline{\theta} = \frac{1}{s} e^{-z\sqrt{\Pr(s+N)}}$$
(22)

$$\overline{\phi} = \frac{1}{s} e^{-z\sqrt{\operatorname{Sc}(s+K)}}$$
(23)

Finally, inverse Laplace transformation is applied on Eqns. (21), (22) and (23) leading to the velocity, temperature and concentration distributions of this flow problem represented by Eqns. (24), (25) and (26) respectively as follow:

$$q = \left(1 - \frac{B_{1}}{D_{1}} - \frac{E_{1}}{F_{1}}\right) \psi(1, a, z, t) + \frac{B_{1}}{D_{1}} \psi(\operatorname{Pr}, N, z, t) + \frac{E_{1}}{F_{1}} \psi(\operatorname{Sc}, K, z, t) + \frac{B_{1}}{D_{1}} e^{D_{1}t} \left\{\psi(1, a + D_{1}, z, t) - \psi(\operatorname{Pr}, N + D_{1}, z, t)\right\} + \frac{E_{1}}{F_{1}} e^{F_{1}t} \left\{\psi(1, a + F_{1}, z, t) - \psi(\operatorname{Sc}, K + F_{1}, z, t)\right\}$$

$$(24)$$

$$\theta = \psi(\Pr, N, z, t) \tag{25}$$

$$\phi = \psi \left(\operatorname{Sc}, K, z, t \right) \tag{26}$$

4. SKIN FRICTION

Skin friction is defined by Newton's law of viscosity. The coefficient of skin friction, C_f at the plate is computed as follows:

$$C_{f} = -\frac{\partial q}{\partial z} \bigg|_{z=0}$$

$$= \left(1 - \frac{B_{1}}{D_{1}} - \frac{E_{1}}{F_{1}}\right) \psi'(1, a, t) + \frac{B_{1}}{D_{1}} \psi'(\Pr, N, t) + \frac{E_{1}}{F_{1}} \psi'(\operatorname{Sc}, K, t) + \frac{B_{1}}{D_{1}} e^{D_{1}t} \left\{ \psi'(1, a + D_{1}, t) - \psi'(\Pr, N + D_{1}, t) \right\} + \frac{E_{1}}{F_{1}} e^{F_{1}t} \left\{ \psi'(1, a + F_{1}, t) - \psi'(\operatorname{Sc}, K + F_{1}, t) \right\}$$
(27)

5. NUSSELT NUMBER

Heat flux is determined from the Fourier law of conduction. The coefficient of rate of heat transfer or Nusselt number is specified by:

$$\operatorname{Nu} = -\frac{\partial \theta}{\partial z} \bigg|_{z=0} = \psi'(\operatorname{Pr}, N, t)$$
(28)

6. SHERWOOD NUMBER

Fick's law of mass diffusion defines the mass flux. The coefficient of rate of mass transfer in terms of Sherwood number is deduced as:

$$\operatorname{Sh} = -\frac{\partial \phi}{\partial z} \bigg|_{z=0} = \psi'(\operatorname{Sc}, K, t)$$
⁽²⁹⁾

7. RESULTS AND DISCUSSION

Computational software Matlab has been used to do calculations for temperature. numerical velocity. concentration, skin friction, Nusselt number and Sherwood number from their exact solutions obtained in Eqns. (24), (25), (26), (27), (28) and (29) by assigning admissible specific values to the parameters present in our study. The value assigned to the parameter Reynolds number Re is 0.5. The reason for choosing a small Reynolds number is because the flow under consideration is laminar. For the parameter Prandtl number Pr, the value chosen is 0.021, which is the Prandtl number of liquid lead at about 470 K temperature. Small Prandtl number indicates the high thermal conductivity of liquid lead. With Mercury as solute and liquid lead as solvent, two values for the parameter Schmidt number Sc have been considered. The value 816.87 corresponds to temperature of 470 K while 2305.245 is the value of Sc at 450 K temperature. Very high value of Sc signifies the prominence of convective mass transfer over molecular mass transfer. The results of the numerical calculations are presented graphically for velocity (both the primary and secondary velocity), temperature and concentration fields and the effects of specific parameters are analyzed. For the three transport properties the results and the effects of relevant parameters have been displayed in tabular form.

Figures 2-13 represent the influence of radiation parameter N, rotational parameter Er, hydromagnetic parameter Nm, Hall parameter β_e , ion-slip parameter β_i and the Darcy number Da on the flow characteristics of the problem with respect to the normal co-ordinate z. Figures 2, 4, 6, 8, 10 and 12 exhibit the primary velocity field U and Figures 3, 5, 7, 9, 11 and 13 show the variation of the secondary velocity field V. As depicted in the figures, primary velocity is boosted with increase in β_e , β_i and Da while *N*,*Er* and *Nm* decelerate the primary velocity. The parameters β_e , N, Nm and Da cause similar effects on the magnitude of the secondary velocity. But due to Er, the magnitude of the secondary velocity is enhanced and β_i retards the magnitude in contrast to their effects on the primary velocity. Observed effects of the radiation parameter, hydromagnetic parameter, rotational parameter and the Darcy number are well on the expected lines. Increase in the radiation parameter causes the fluid particles to lose their kinetic energy resulting in the fall of fluid velocity. The Lorentz force developed due to the interaction of the applied magnetic field and the moving electrically conducting fluid is acting in direction opposite to the fluid velocity. So increase in the hydromagnetic parameter means greater resistance to the fluid velocity. Due to rotation the system loses translational kinetic energy. So primary velocity is reduced with increase in Er but as due to rotation the motion is diverted a bit from the primary direction to the secondary direction, secondary velocity increases with Er. Again with increase in the Darcy number, permeability of the medium is enhanced allowing the fluid particles to have a better free movement through the medium. In Figure 14, temperature distribution has been demonstrated versus z under the influence of N. As can be realized from the Figure that temperature drops with increase in N. The reason for this behavior is the fact that the fluid loses thermal energy through radiation.



Figure 2. Primary velocity versus z for Gr=5,Gm=3, Re=0.5,Da=1,Sc=816.87,Er=0.02,Nm=5,t=0.2, Pr=0.021,K=0.2, $\beta_i = 0.2$, $\beta_e = 0.5$



Figure 3. Secondary velocity versus z for Gr=5,Gm=3, Re=0.5,Da=1,Sc=816.87,Er=0.02,Nm=5,t=0.2,Pr=0.021, K=0.2, β_i =0.2, β_e =0.5



Figure 4. Primary velocity versus z for Gr=5,Gm=3, Re=0.5,Da=1,Sc=816.87,N=5,Nm=5,t=0.2, Pr=0.021,K=0.2, $\beta_i = 0.2, \beta_e = 0.5$



Figure 5. Secondary velocity versus z for Gr=5,Gm=3, Re=0.5,Da=1,Sc=816.87,N=5,Nm=5,t=0.2, Pr=0.021,K=0.2, $\beta_i = 0.2, \beta_e = 0.5$



Figure 6. Primary velocity versus z for Gr=5,Gm=3, Re=0.5,Da=1,Sc=816.87,N=5,Er=0.02,t=0.2,



Figure 7. Secondary velocity versus z for Gr=5,Gm=3, Re=0.5,Da=1,Sc=816.87,N=5,Er=0.02,t=0.2, Pr=0.021,K=0.2, $\beta_i = 0.2, \beta_e = 0.5$



Figure 8. Primary velocity versus z for Gr=5, Gm=3, Re=0.5, Da=1, Sc=816.87, N=5, Er=0.02, t=0.2, Pr=0.021, K=0.2, Nm=5, $\beta_e = 0.5$



Figure 9. Secondary velocity versus z for Gr=5, Gm=3, Re=0.5, Da=1, Sc=816.87, N=5, Er=0.02,t=0.2, Pr=0.021, K=0.2, Nm=5, $\beta_a = 0.5$



Figure 10. Primary velocity versus z for Gr=5, Gm=3, Re=0.5, Da=1, Sc=816.87, N=5, Er=0.02, t=0.2, Pr=0.021, K=0.2, β_i =0.2, Nm=5



Figure 11. Secondary velocity versus z for Gr=5, Gm=3, Re=0.5,Da=1,Sc=816.87,N=5, Er=0.02, t=0.2, Pr=0.021, K=0.2, β_i=0.2, Nm=5



Figure 12. Primary velocity versus z for Gr=5, Gm=3, Re=0.5, Nm=5, Sc=816.87, N=5, Er=0.02, t=0.2, Pr=0.021, K=0.2, β_i =0.2, β_e =0.5



Figure 13. Secondary velocity versus z for Gr=5, Gm=3, Re=0.5, Nm=5, Sc=816.87, N=5, Er=0.02, t=0.2, Pr=0.021, K=0.2, β_i =0.2, β_a =0.5



Figure 14. Temperature versus z for Pr=0.021, t=0.2



Figure 15. Concentration versus z for Sc=816.87, t=0.2



Figure 16. Concentration versus z for K=0.2, t=0.2

Figures 15 and 16 represent the concentration profile versus the normal co-ordinate under the effects of chemical reaction parameter K and Schmidt number Sc respectively. Both the parameters reduce the concentration level of the fluid but their effects are realized only in a thin area adjacent to the plate. Physical justification for this behavior of fluid concentration is attributed to the very high value of Schmidt number. Very high value of Sc means very low mass diffusivity which results in a comprehensive fall in the concentration boundary layer.

Table 1. Variation of primary C_f with respect to Nm

Nm	Primary C _f
0	0.3825
0.5	0.4352
1	0.5891
1.5	0.8262
2	1.1426
2.5	1.5239
3	1.9509
3.5	2.4082
4	2.8837

Skin friction for z=0,Gr=5,Gm=3,Re=0.5,Da=1,Sc=816.87,N=5,Er=0.02,t=0.2,Pr=0.02 1,K=0.2, $\beta_i = 0.2, \beta_a = 0.5$

Table 2. Variation of primary C_f and Nu with respect to N

Ν	Primary C_f	Nu
0	3.8062	0.1828
0.5	3.8126	0.2008
1	3.8186	0.2182
1.5	3.8242	0.2351
2	3.8294	0.2514
2.5	3.8344	0.2673
3	3.8390	0.2827
3.5	3.8434	0.2977
4	3.8475	0.3123

Skin friction for

z=0,Gr=5,Gm=3,Re=0.5,Da=1,Sc=816.87,Nm=5,Er=0.02,t=0.2,Pr=0.02 1,K=0.2, β_i =0.2, β_{ρ} =0.5

Nusselt number for z=0,Pr=0.021,t=0.2

Table 3. Variation of primary C_f and Sh with respect to K

K	Primary C_f	Sh
0	3.8557	36.0567
0.1	3.8555	36.7755
0.3	3.8551	38.1988
0.5	3.8556	39.6035
0.8	3.8565	41.6768
1	3.8570	43.0370
1.5	3.8583	46.3637
2	3.8596	49.5897
3	3.8620	55.7616

Skin friction for

z=0,Gr=5,Gm=3,Re=0.5,Da=1,Sc=816.87,Nm=5,Er=0.02,t=0.2,Pr=0.02

$$1,N=5, r^{e_{l}}=0.2, r^{e_{l}}=0.5$$

Sherwood number for z=0, Sc=816.87, t=0.2

In Table 1, primary skin friction has been analyzed under the effect of hydro-magnetic parameter, in Table 2, primary skin friction and Nusselt number have been presented corresponding to various values of radiation parameter and in Table 3 effects of chemical reaction parameter on primary skin friction and Sherwood number have been studied. It is found that as the applied magnetic field is made stronger the primary skin friction at the plate also grows up. The radiation parameter speeds up the heat transfer from the plate to the fluid and also increases the viscous drag at the plate. Chemical reaction parameter enhances the rate of mass transfer from the plate remarkably. However, no significant variation of primary skin friction at the plate is noticed under the effect of chemical reaction parameter.

8. CONCLUSIONS

The investigation leads to the following conclusions:

-Hall parameter, ion-slip parameter and Darcy parameter accelerate and radiation parameter, rotation parameter and hydromagnetic parameter decelerate the primary velocity. On the contrary, secondary velocity is accelerated by the rotation parameter and decelerated by the ion-slip parameter.

-Temperature decreases with radiation parameter.

-Chemical reaction parameter and Schmidt number reduce the concentration level but the effects are only limited to a thin area adjacent to the plate.

-Magnetic parameter and radiation parameter increase the primary skin friction at the plate.

-Heat transfer becomes faster under the effect of radiation parameter and chemical reaction parameter enhances the rate of mass transfer.

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NOMENCLATURE

\vec{B}	Magnetic induction vector
B_0	Magnitude of applied magnetic field
C'	Fluid concentration
C_{f}	Skin friction coefficient
C_P	Specific heat at constant pressure
Da	Darcy number
D_{M}	Mass diffusivity
E_r	Rotational parameter
\vec{g}	Acceleration due to gravity
Gm	Solutal Grashof number
Gr	Grashof number
$ec{J}$	Current density vector
Κ	Chemical reaction parameter
K_1	Chemical reaction constant
K_p	Permeability parameter
K_p^*	Permeability constant
L	Characteristic length
Ν	Radiation parameter
Nm	Hydromagnetic parameter
Nu	Nusselt number
р	Fluid pressure
Pr	Prandtl number
\vec{q}	Fluid velocity

Sc Schmidt number

Sh Sherwood number

- t' Time
- *T'* Fluid temperature

Greek symbols

β	Volume	expansion	coefficient	for	heat
	transfer			_	
eta^*	Volume	expansion	coefficient	for	mass
0					
β_e	Hall para	imeter			
eta_i	Ion slip p	arameter			
К	Thermal conductivity				
λ	Wave ler	ngth			
$(a_{\lambda})_{w}$	Absorptio	on coefficie	nt at the plate	;	
$e_{\lambda h}$	Planck's	function			
μ	Coefficie	ent of viscos	ity		
ν	Kinemati	c viscosity			

ρ	Fluid density
σ	Electrical conductivity
$ec{\omega}$	Angular velocity

APPENDIX

$$(H_0)^2 = (Nm)^2 \alpha_0 M_1 = 2i \, Er + (H_0)^2$$

$$a = M_1 + \frac{1}{Da(\operatorname{Re})^2} B_1 = \frac{\operatorname{Gr}}{\operatorname{Pr} - 1} D_1 = \frac{a - \operatorname{Pr} N}{\operatorname{Pr} - 1}$$

$$E_1 = \frac{\operatorname{Gm}}{\operatorname{Sc} - 1} \qquad F_1 = \frac{a - \operatorname{Sc} K}{\operatorname{Sc} - 1}$$

$$\psi(\xi, \eta, y, t) = \frac{1}{2} \left[e^{\sqrt{\zeta \eta} y} \operatorname{erfc} \left(\frac{\sqrt{\xi} y}{2\sqrt{t}} + \sqrt{\eta t} \right) + e^{-\sqrt{\xi \eta} y} \operatorname{erfc} \left(\frac{\sqrt{\xi} y}{2\sqrt{t}} - \sqrt{\eta t} \right) \right]$$

$$\psi'(\xi, \eta, t) = \sqrt{\xi \eta} \operatorname{erf} \left(\sqrt{\eta t} \right) + e^{-\eta t} \sqrt{\frac{\xi}{\pi t}}$$