



Mathematical Model of Measuring Monitoring and Temperature Control of Growing Vegetables in Greenhouses

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ABSTRACT

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The main purpose of the article is to improve the mathematical model of the process of computerized measuring monitoring and adaptive fuzzy control of temperature modes of growing crops in greenhouse conditions. The results of the research were obtained using methods of physical and mathematical modelling, theory of differential equations of mathematical physics, theory of thermal conductivity, methods of structural-algorithmic synthesis of complex technical systems. The main purpose of the article was achieved by taking into account types and periods of vegetation of crops and factors of seasonality and engineering design of greenhouses, which allowed substantiating the functional diagram of the system of monitoring and control of temperature in the growing zone. The article establishes regularities of influence of natural sources and technical components of heat energy inputs and losses in greenhouses taking into account current requirements for technological modes of greenhouse operating, which allowed estimating the range of total specific heat energy sufficient for the production. Promising areas for further research of the developed model were proposed in order to increase the integral efficiency of greenhouse farms. The obtained research results can be used as a scientific and applied basis for substantiating ways to optimize energy consumption of industrial greenhouses.

1. INTRODUCTION

1.1 Relevance of the research topic

One of the prerequisites for ensuring good nutrition of the population is uniform introduction of fresh vegetables and fruits into the diet throughout the year [1]. Cost-effective and technically efficient functioning of industrial greenhouse complexes can contribute to the solution of the problem of seasonality of domestic vegetable production. In general, profitability of vegetable growing on protected grounds can be expressed in terms of energy intensity of production to the rate, quality, and volume of output greenhouse products. In order to ensure competitiveness of greenhouse enterprises in temperate and cold climates with a relatively high cost of energy, it is imperative to solve the problems of optimal and adaptive temperature control of cultivation using contemporary achievements in the field of digital, microprocessor, sensor, and information technology [2, 3]. Thus, conducting studies to justify the requirements for hardware and software for the subsystems of monitoring and control of greenhouse heating systems by mathematical modelling methods is an urgent scientific and applied task.

The scientific novelty of the obtained research results consists in the development of the nonlinear mathematical model of the process of measuring monitoring and adaptive control of temperature modes of cultivation by taking into account the types and periods of crops, as well as seasonality and climatic features of greenhouse locations. This fact allows to optimize plant growing modes in greenhouse conditions.

1.2 Analysis and generalization of known research results

At present, the problem of developing and substantiating mathematical models for monitoring and control of the temperature in the greenhouse growing area has been sufficiently addressed from theoretical and practical points of view. For example, the authors [4-8] propose to consider a greenhouse as a nonlinear system in which temperature is a dynamic characteristic and can be estimated on the basis of the energy balance equation. In the articles [9, 10] physical and mathematical foundations of forecasting the temperature dynamics in greenhouses are grounded on the basis of adaptive measuring monitoring of the greenhouse indoor microclimate and external climatic factors. In articles [11-13],

the basic approaches to the implementation of simulation models of fuzzy control of temperature modes of cultivation on the basis of differential equations of heat and mass transfer are presented. In articles [14-16] basic scientific and theoretical provisions concerning physical, mathematical and simulation modelling of industrial greenhouse microclimate with the use of modern hardware and software solutions to the construction of computerized systems of monitoring and control of technological modes of crop cultivation on the protected grounds are presented. The results of the development of dynamic models of influence of microclimate parameters on the quality of growing vegetable crops under greenhouse conditions are presented in articles [17-19], as well as the main algorithms and results of numerical solution of the proposed models.

The fact of a significant number of the studies of the greenhouse microclimate monitoring and control systems using IoT and GWT technologies [20, 21] has been established.

These developments allow to optimize the structural and software organizations of the monitoring and control systems of the growing crops regimes. These results can be used as a basis during development of the mathematical model of measuring monitoring and temperature control of growing vegetables in greenhouses.

Analysis and logical generalization of the known research results in the investigated subject area revealed lack of scientists' attention to the influence of types and periods of greenhouse crops vegetation, taking into account factors of climatic zones and seasonality of cultivation on technical and functional characteristics of monitoring and control of heating systems. This fact necessitates conducting research to justify the requirements for structural and algorithmic organization of such subsystems by mathematical modelling methods, which will increase economic and technical efficiency of the production process of growing vegetables in greenhouses.

1.3 Purpose, object and structure of the research

The main purpose of the article is to improve the mathematical model of the process of computerized measuring monitoring and adaptive temperature control of crop growing in greenhouse conditions by taking into account types and periods of crop vegetation and the seasonality factor, which will allow optimizing energy consumption of greenhouses.

The object of the study is regularities of the influence of informative parameters and destabilizing factors on the distribution of heat energy in the greenhouse growing zone.

Section 2 describes the basic materials and methods used in the development of the mathematical model; section 3 presents the basic quantitative and qualitative results of mathematical modelling of the process of temperature monitoring in greenhouses; section 4 outlines promising areas for further research; section 5 summarizes the main conclusions of the article.

2. MATERIALS AND METHODS OF THE RESEARCH

2.1 General research methods

Theoretical and experimental studies on the development

and justification of the mathematical model of the process of measuring monitoring and control of temperature modes of greenhouse crop cultivation were obtained using the provisions of physical and mathematical modelling, theory of differential equations of mathematical physics, theory of thermal conductivity, structural-synthetic algorithms. The main research results were obtained in the specialized laboratories "Information and Measurement Engineering and Metrology" and "Computer Technologies and Modelling" of the Department of Electronic Engineering of SHEE "Donetsk National Technical University" using certified and standardized equipment and software.

2.2 Basic research technique

Measuring temperature monitoring is a dynamic process, the characteristics of which are mainly determined by the exchange of energy between the indoor greenhouse growing area and the outside environment. In this case, the mathematical modelling of thermodynamic processes occurring in the greenhouse involves establishing and solving equations of mathematical physics.

Based on the analysis of the known research results on modelling temperature modes in greenhouses, it is established that the modern engineering design of industrial greenhouse complexes allows assuming during mathematical modelling of thermodynamic processes that the greenhouse is an object with a uniform temperature distribution in the cultivation zone. Therefore, the basic equation for mathematical modelling of measuring temperature monitoring is [22]:

$$\frac{\partial T_{air\ in}(t)}{\partial t} = \frac{Q_{total}(t)}{V_{in} \cdot \rho_{air} \cdot C_p} \quad (1)$$

where, $T_{air\ in}$ is temperature inside the greenhouse, °C; Q_{total} is total heat energy in the growing zone, W; t is time, h.; V_{in} is volume of the greenhouse growing zone, m³; ρ_{air} is air density, kg·m⁻³; C_p is specific heat of air, J·kg⁻¹·°C⁻¹.

Temperature dynamics in greenhouses is affected by different processes of heat and mass transfer. Therefore, in order to develop a relatively accurate and adequate model describing heat distribution in the greenhouse growing zone, it is important to investigate in detail the mechanisms of these processes. Thus, the basis of the developed mathematical model is the equation of the balance of mass and energy inside the greenhouse [11, 22]:

$$Q_{total} = Q_{gain} - Q_{loss} \quad (2)$$

where, Q_{gain} is amount of energy supplied to the greenhouse, W; Q_{loss} is amount of energy consumed in a greenhouse, W.

Tomatoes and cucumbers were selected as the basic types of greenhouse crops when designing the mathematical model. The study of the mathematical model was conducted for two typical growing seasons: before fruiting and during fruiting. The annual growing period was divided into two main cycles: autumn-winter and spring-summer.

2.3 Sources of heat energy

The amount of energy coming into the greenhouse is greatly influenced by the following physical processes and

phenomena: energy from solar radiation; energy from the heating system; thermal component of energy from artificial systems of additional lighting [10, 11, 22]. Thus, in general, the amount of the energy supplied to the greenhouse can be calculated by the formula:

$$Q_{gain} = Q_s + Q_h + Q_l \quad (3)$$

where, Q_s is useful solar energy supplied to the greenhouse, W; Q_h is heat energy from the heating system, W; Q_l is thermal component of energy from artificial systems of additional lighting, W.

One of the most important factors determining the input of heat energy to the greenhouse is solar radiation. The heat energy supplied to the greenhouse from the sun can be estimated by the following relation [23, 24]:

$$Q_s = A_g \cdot \gamma \cdot \tau \cdot I_{total} \quad (4)$$

where, A_g is the greenhouse surface area (roof and sidewalls), m^2 ; γ is the constant of the fraction of solar radiation entering the greenhouse and causing the temperature increase, relative units; τ is the greenhouse surface capacity, relative units; I_{total} is the solar energy falling on the greenhouse surface, $W \cdot m^{-2}$.

At present, there are several theoretical and empirical models that describe the dynamics of solar radiation. On the basis of the analysis of the obtained simulation data, the necessity of refining the model of solar radiation distribution with consideration of seasonal and daily dynamics of the solar radiation [25] for temperate continental climate was established. For the spring-summer period, the average value of daylight hours is equal to 13 hours (from 6 a.m. to 7 p.m.) and 9 hours for autumn-winter period (from 8 a.m. to 4 p.m.) for GMT+3 time zone. On this basis, the analytic expression for describing the daily dynamics of the solar radiation, taking into account the seasonality, is as follows:

– For the spring-summer cultivation cycle:

$$\begin{cases} I_{total} = \left| k_{decr} \left[I_{sc} \cdot (\sin(\omega t - \varphi) + \sin(\omega)) \right] \right|, & 6n \leq t \leq 19n; \\ I_{total} = 0, & otherwise, \end{cases} \quad (5)$$

– for the autumn-winter cultivation cycle:

$$\begin{cases} I_{total} = \left| k_{decr} \left[I_{sc} \cdot (\sin(\omega t - \varphi) + \sin(\omega)) \right] \right|, & 8n \leq t \leq 16n; \\ I_{total} = 0, & otherwise, \end{cases} \quad (6)$$

where, k_{decr} is the coefficient of the solar radiation attenuation, which varies in the range from 0.47 to 0.85, relative units; I_{sc} is the solar constant equal to $1367 \text{ W} \cdot m^{-2}$; ω is cyclic frequency of change in the solar radiation, defined as $2\pi/24$, rad.; φ is the argument of sinusoidal variation of solar radiation (for spring-summer period – 13 hours, for autumn-winter – 8 hours, (GMT+3)); n is the continuous number of the day in the calendar year.

When estimating the value of the useful solar energy supplied to the greenhouse, the numerical values of the parameters were assigned in accordance with Table 1. Typical sizes of greenhouses were selected based on current recommendations for modern engineering design.

The heat transfer rate from the stationary heating system to the air of the growing zone, depending on the structural

characteristics can be calculated by the formula [10, 23]:

$$Q_h = m_{h.c.} \cdot c_{h.c.} \cdot (T_{direct} - T_{back}) \quad (7)$$

where, $m_{h.c.}$ is heat carrier consumption, $kg \cdot s^{-1}$; $c_{h.c.}$ is specific heat capacity of the heat carrier, $J \cdot kg^{-1} \cdot ^\circ C^{-1}$; T_{direct} is the heat carrier supply temperature, $^\circ C$; T_{back} is the temperature of the heat carrier removed from the heating system, $^\circ C$.

During the estimation of the value of heat energy coming into the greenhouse from the stationary heating systems, the numerical values of the parameters were assigned in accordance with Table 2.

The thermal energy component of artificial light systems can be estimated by taking into account the existing recommendations [26] by the formula:

$$Q_l = E_l \cdot F_l \cdot q_l \cdot \eta_l \quad (8)$$

where, E_l is the required level of illumination of the growing zone, lx; F_l is the area of the greenhouse under lying surface, which ranges from 0.2 to 0.3 for greenhouses of different design, m^2 ; q_l is the specific heat release indicator, $W \cdot lx^{-1} \cdot m^{-2}$; η_l is the share of heat entering the growing zone, relative units.

In estimating the value of the heat energy supplied to the greenhouse from stationary specialized Phyto-LED artificial illumination systems, the numerical values of the parameters were assigned in accordance with Table 3.

Table 1. Assigned values of useful solar energy modelling

| Parameter | Accepted value | Units |
|--|----------------|------------|
| Surface area (A_g) (typical values for temperate continental climate) | 1500; 3000 | m^2 |
| Solar radiation fraction constant (γ) | 0.5 | rel. units |
| Greenhouse surface capacity (τ) | 0.7 | rel. units |
| Solar radiation attenuation coefficient (k_{decr}) | 0.65 | rel. units |

Table 2. Assigned values of modelling heat energy from greenhouse heating systems

| Parameter | Accepted value | Units |
|---|----------------|---------------------------------------|
| Consumption of heat carrier ($m_{h.c.}$) | 10 | $kg \cdot s^{-1}$ |
| Specific heat capacity of heat carrier ($c_{h.c.}$) | 4200 | $J \cdot kg^{-1} \cdot ^\circ C^{-1}$ |
| Permissible difference between temperatures of the forward and reverse branches of the heating system ($T_{direct} - T_{back}$) | 10 | $^\circ C$ |

Table 3. Assigned values of modelling heat energy from artificial light systems

| Parameter | Accepted value | Units |
|---|----------------|--------------------------------|
| Minimum required level of illumination (E_l) | 6 315 | lx |
| The area of the greenhouse underlying surface ($F_l = A_g/4$) | 375; 750 | m^2 |
| Specific heat release rate (q_l) | 0.018 | $W \cdot lx^{-1} \cdot m^{-2}$ |
| Share of heat entering the growing zone (η_l) | 1 | rel. units |

2.4 Sources that cause heat loss

Losses of heat energy in the greenhouse are largely due to the following processes and phenomena: heat loss due to thermal conductivity; heat loss due to soil absorption capacity; heat transfer due to ventilation and infiltration; condensation heat transfer [10, 11, 22]. Therefore, in general terms, the amount of energy lost in the greenhouse can be calculated as follows:

$$Q_{loss} = Q_k + Q_g + Q_v + Q_i + Q_c \quad (9)$$

where, Q_k is heat loss due to thermal conductivity, W; Q_g is heat loss due to soil absorption capacity, W; Q_v is heat transfer through ventilation, W; Q_i is heat transfer through infiltration, W; Q_c is condensation heat transfer, W.

Based on the analysis of the dependence (9), it can be seen that the loss of heat energy is caused by a considerable number of physical processes, one of which is the heat loss due to thermal conductivity. This component of the energy loss can be calculated using the following equation [22]:

$$Q_k = h \cdot A_g \cdot (T_{air\ in} - T_{air\ out}) \quad (10)$$

where, h is the heat transfer coefficient, $W \cdot m^{-2} \cdot ^\circ C^{-1}$; A_g is the greenhouse surface area, m^2 ; $T_{air\ in}$ is temperature in the greenhouse, $^\circ C$; $T_{air\ out}$ is ambient temperature, $^\circ C$.

The coefficient of heat transfer, which is a part of the Eq. (10), can be calculated depending on the speed of movement of air flows in the greenhouse [22] by the formula:

$$h = 2,8 + 1,2 \cdot v_{air\ in} \quad (11)$$

where, $v_{air\ in}$ is the velocity of air flow, $m \cdot s^{-1}$.

The optimum temperature inside the greenhouse depends on the types and periods of vegetation of the crops grown. Statistics on the temperature dynamics over the last calendar year in Ukraine were obtained according to the official data of the Ukrainian Hydrometeorological Centre: for the autumn-winter cycle it is $+3.77^\circ C$, for the spring-summer cycle it is $+15.6^\circ C$.

Therefore, the numerical values of the parameters in accordance with Table 4 are assigned when estimating the values of heat energy losses caused by the heat transfer effect.

The next physical process to be taken into account when estimating heat losses in the greenhouse is the soil absorbing capacity. The estimated value of the heat loss due to the soil absorption capacity can be calculated by the formula [11, 22]:

$$Q_g = \frac{k_g}{Z_g} \cdot F_l \cdot (T_{air\ in} - T_{soil}) \quad (12)$$

where, k_g is the coefficient of soil thermal conductivity, $W \cdot m^{-1} \cdot ^\circ C^{-1}$; Z_g is thickness of the soil layer, m; F_l is the area of the greenhouse underlying surface, m^2 ; $T_{air\ in}$ is greenhouse air temperature, $^\circ C$; T_{soil} is soil temperature, $^\circ C$.

The calculation of the heat losses was carried out taking into account the current requirements for temperature modes of the gas-air environment and the greenhouse soil, the thickness of the soil layer and typical sizes of industrial greenhouse complexes, as shown in Table 5.

Table 4. Assigned values of modelling heat energy losses due to thermal conductivity

| Parameter | Accepted value | Units |
|--|----------------|------------------|
| Velocity of the air flow ($v_{air\ in}$) | 1 | $m \cdot s^{-1}$ |
| Surface area (A_g) | 1500; 3000 | m^2 |
| Average ambient temperature ($T_{air\ out}$) | +3.77; +15.6 | $^\circ C$ |

Table 5. Assigned values of modelling heat energy losses due to soil absorption capacity

| Parameter | Accepted value | Units |
|---|----------------|--------------------------------------|
| Soil thermal conductivity coefficient (k_g) | 1.52 | $W \cdot m^{-1} \cdot ^\circ C^{-1}$ |
| Area of the greenhouse underlying surface (F_l) | 375; 750 | m^2 |
| Thickness of the soil layer (Z_g) | 0.5 | m |
| Permissible temperature difference ($T_{air\ in} - T_{soil}$) | 3 | $^\circ C$ |

The effects of heat loss from the crop growing zone under the influence of heat and wind pressure are ventilation (forced and natural) (Q_v) and infiltration (Q_i). Estimation of the heat loss through ventilation can be performed by the following formula [11, 27]:

$$Q_v = \frac{r_v \cdot V_g \cdot k_{air} \cdot (T_{air\ in} - T_{air\ out}) \cdot C_p \cdot \rho_{air}}{3600} \quad (13)$$

where, r_v is percentage of opening mechanisms of the ventilation system, relative units; V_g is greenhouse volume, m^3 ; k_{air} is multiplicity of air exchange, h^{-1} ; C_p is specific heat of air, $J \cdot kg^{-1} \cdot ^\circ C^{-1}$; $T_{air\ in}$ is greenhouse temperature, $^\circ C$; $T_{air\ out}$ is ambient temperature, $^\circ C$; ρ_{air} is air density, $kg \cdot m^{-3}$.

The numerical value of the heat loss indicator due to the infiltration process, which is caused by the greenhouse surface density, can be estimated by the following formula [11]:

$$Q_i = \frac{0,5 \cdot V_g \cdot k_{air} \cdot (T_{air\ in} - T_{air\ out})}{3600} \quad (14)$$

Thus, the total heat loss (Q_{v+i}) caused by the processes of ventilation and infiltration can be found by the formula:

$$Q_{v+i} = \frac{r_v \cdot V_g \cdot k_{air} \cdot (T_{air\ in} - T_{air\ out}) \cdot C_p \cdot \rho_{air}}{3600} + \frac{0,5 \cdot V_g \cdot k_{air} \cdot (T_{air\ in} - T_{air\ out})}{3600} \quad (15)$$

Numerous parameters were assigned during the simulation of the heat loss due to the processes of ventilation and infiltration of the greenhouse, including seasonal factors, climatic characteristics of the region, types and periods of crop vegetation, as well as the engineering design of greenhouses, as shown in Table 6.

The effect of condensation, which is caused by the constant release of moisture by plants, leads to the restriction of the supply of the heat energy to the greenhouse growing zone. The heat energy losses due to the effect of condensation on the greenhouse surface can be numerically estimated by taking into account the geometric characteristics

of greenhouses and the seasonality factor according to the following formula [23]:

$$Q_c = C_c \cdot L_v \cdot A_g \quad (16)$$

where, C_c is rate of condensation on the greenhouse surface, which is due to the difference between external and internal temperature and humidity, $\text{kg}\cdot\text{s}^{-1}\cdot\text{m}^{-2}$; L_v is enthalpy of saturated vapor, $\text{J}\cdot\text{kg}^{-1}$.

Table 6. Assigned values of modelling heat energy losses due to ventilation and infiltration

| Parameter | Accepted value | Units |
|--|----------------|---|
| Specific heat capacity of air (C_p) | 1010 | $\text{J}\cdot\text{kg}^{-1}\cdot\text{C}^{-1}$ |
| Average ambient temperature ($T_{air\ out}$) | +3.77; +15.6 | $^{\circ}\text{C}$ |
| Air density (ρ_{air}) | 1.292 | $\text{kg}\cdot\text{m}^{-3}$ |
| Multiplicity of air exchange (k_{air}) | 2 | h^{-1} |
| Greenhouse volume ($V_g=A_g\cdot h_g/4$) | 1875; 3750 | m^3 |
| Percentage of opening the mechanisms of the ventilation system (r_v) | 0.6 | rel. units |

Estimates of the rate of condensation on the greenhouse surface were obtained by the researchers [22] for a temperate continental climate, as shown in Table 7.

Table 7. Assigned values of modelling of heat energy losses due to condensation

| Parameter | Accepted value | Units |
|---------------------------------------|--------------------|---|
| Surface area (A_g) | 1500; 3000 | m^2 |
| Saturated vapor enthalpy (L_v) | $2.45\cdot 10^6$ | $\text{J}\cdot\text{kg}^{-1}$ |
| Condensation rate in winter (C_c) | $2.5\cdot 10^{-6}$ | $\text{kg}\cdot\text{s}^{-1}\cdot\text{m}^{-2}$ |

The authors of the study [22] also found that the energy losses due to condensation increase if the greenhouse surface temperature is lower than the dew point temperature of the indoor air. Therefore, taking into account this effect, we can assume that the condensation rate in the spring-summer growing cycle is zero.

3. RESEARCH RESULTS

3.1 Quantitative and qualitative modelling results

When estimating the value of the useful solar energy according to formulas (4)–(6), which enters the greenhouse, the results were obtained in the normalized to the maximum energy value (for greenhouses with the area of $1500\ \text{m}^2$ – $378.5\ \text{kW}$, for greenhouses with the area of $3000\ \text{m}^2$ – $757\ \text{kW}$), as shown in Figure 1. The obtained simulation results, which are shown in Figure 1, proved the need to take into account the seasonal and daily dynamics of the solar radiation when estimating the heat energy entering the greenhouse growing zone from the sun. The estimated value of the heat energy entering the greenhouse growing zone from stationary heat supply systems, which is calculated by formula (7), is $420\ \text{kW}$. The obtained results of calculations of heat energy component from the heat supply systems proved the necessity of their account during the research of the mathematical model of measurement monitoring of the growing zone temperature of industrial greenhouses.

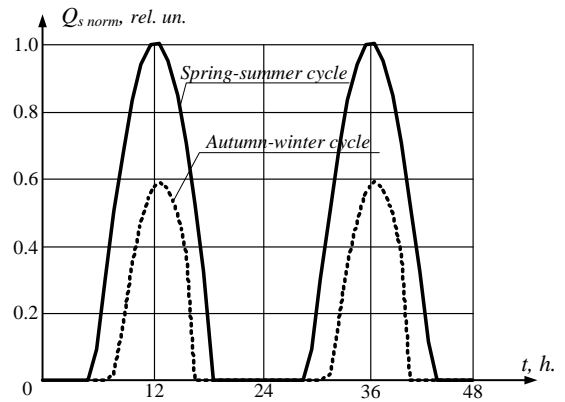


Figure 1. Normalized characteristics of the distribution of the useful solar energy

When estimating the value of the heat energy entering the greenhouse from the stationary artificial lighting systems using formula (8), the following numerical results were established: $42.6\ \text{kW}$ – for greenhouses with the area of $1,500\ \text{m}^2$; $85.2\ \text{kW}$ – for greenhouses with the area of $3,000\ \text{m}^2$.

Therefore, the total amount of the heat energy supplied to the greenhouse, taking into account the above components, which are calculated by formulas (4) – (8), can be estimated by formula (3). The simulation of the process of heat energy supply to greenhouses also takes into account the requirements for duration of the photoperiod of artificial lighting of greenhouse crops, which must be at least 16 hours. Thus, at the qualitative level, the heat input to the greenhouse is as follows: the useful solar energy – see Figure 1; the heat energy from the heating system – 24 hours a day; the heat energy from artificial lighting systems – from 4 a.m. to 8 p.m. (GMT+3). The obtained simulation results are normalized to the maximum energy value (for greenhouses with the area of $1500\ \text{m}^2$ is equal $Q_{gain\ max}=841.1\ \text{kW}$, for greenhouses with the area of $3000\ \text{m}^2$ – $Q_{gain\ max}=1262.2\ \text{kW}$). The normalized graph of energy distribution taking into account the areas of greenhouses is shown in Figure 2.

Based on the analysis of the simulation results shown in Figure 2, the estimated ranges of the total heat energy changes for greenhouses with typical sizes of 1500 and $3000\ \text{m}^2$, respectively, are: from 420 to $841.1\ \text{kW}$ and from $420\ \text{kW}$ to $1262.2\ \text{kW}$. The average rate of the heat energy increase / decrease was also established: for greenhouses with the area of $1500\ \text{m}^2$ it is $46.8\ \text{kW}\cdot\text{h}^{-1}$; for greenhouses with the area of $3000\ \text{m}^2$ – $93.6\ \text{kW}\cdot\text{h}^{-1}$.

The obtained graph of distribution of the estimated values of the heat energy losses on the basis of formulas (10) and (11) due to the heat transfer effect taking into account seasonality, geometric sizes of greenhouses and types and periods of vegetation of crops is shown in Figure 3.

The results of the calculations shown in Figure 3 prove the need to take into account the effect of the heat energy transfer from the growing zone to the environment during the mathematical modelling of the process of temperature monitoring.

The obtained results of the calculations of the heat energy losses due to the soil absorption capacity, which are estimated by formula (12), are as follows: for greenhouses with the area of $1500\ \text{m}^2$ it is $3.42\ \text{kW}$, for greenhouses with the area of $3000\ \text{m}^2$ – $6.84\ \text{kW}$, which is from 5 to 20% of energy losses due to the thermal conductivity of the

greenhouse surface and requires further consideration during the mathematical modelling of the temperature monitoring process.

The obtained graphical view of the distribution of estimated values of the total heat losses due to ventilation effects (natural and mechanical) and infiltration, taking into account seasonality, geometric sizes of greenhouses and types and periods of vegetation on the basis of formula (15) is shown in Figure 4.

The results of the numerical simulations shown in Fig. 4, prove the need to take into account the effect of heat losses

due to the ventilation and infiltration during the mathematical modelling of the process of temperature monitoring.

The results of calculations of the heat energy losses due to the effect of condensation based on formula (16) are as follows: for spring-summer cycle $Q_c = 0$ W, for autumn-winter – 12.7 kW (for greenhouses with the area of 1500 m²) and 25.7 kW (for greenhouses with the area of 3000 m²). The results of the calculations prove the need to take into account the effect of condensation during the mathematical modelling of the process of temperature monitoring of the greenhouse growing zone.

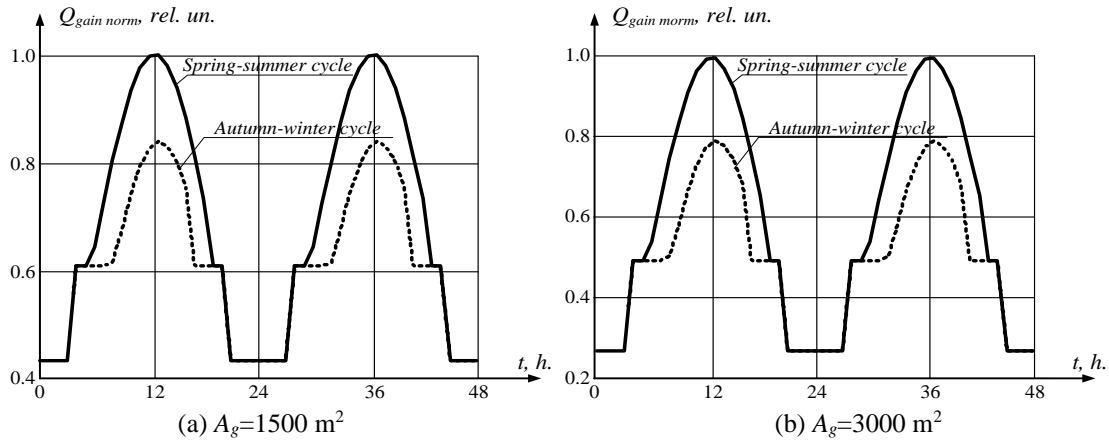


Figure 2. Normalized characteristics of the distribution of the heat energy entering the greenhouse

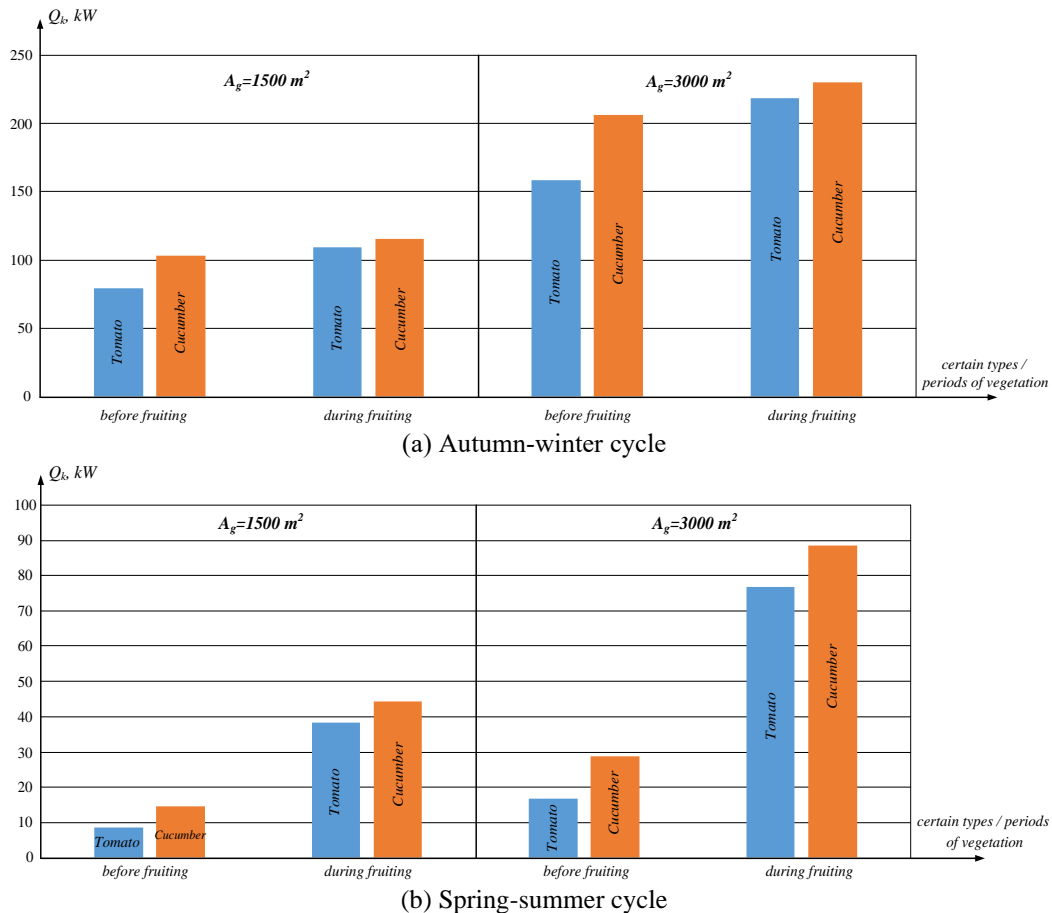


Figure 3. Heat energy losses due to the heat transfer effect

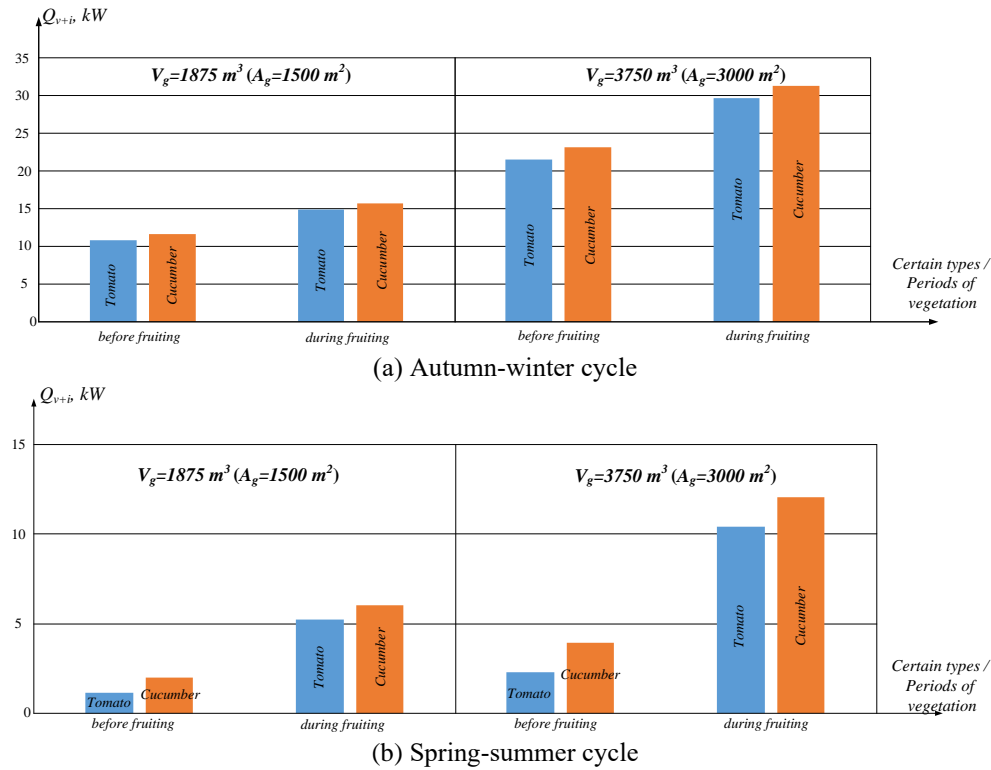


Figure 4. Heat energy losses due to the effects of ventilation and infiltration

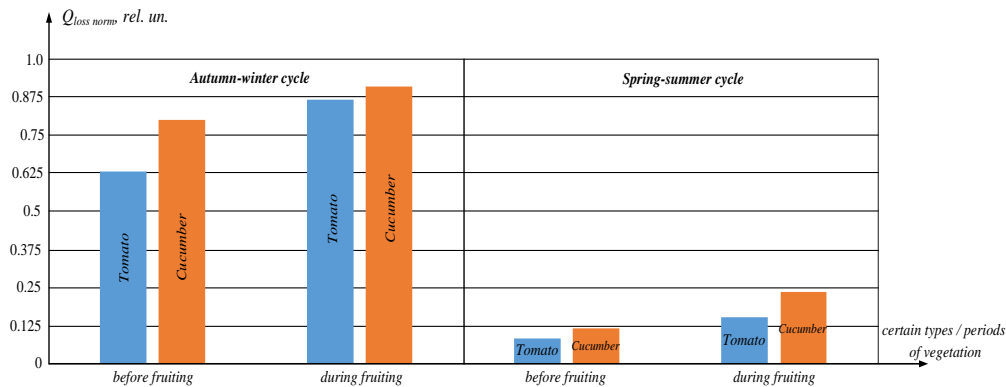


Figure 5. Total heat energy losses

Therefore, the total amount of the heat energy lost in the greenhouse due to the effects of soil thermal conductivity, soil absorption capacity, ventilation, infiltration and condensation can be estimated by formula (9) based on the results of calculations by formulas (10) – (16). While modelling the process of heat energy losses from the greenhouse, the regulated requirements for the engineering design of greenhouses, the temperature-humidity modes of growing greenhouse crops and the seasonality factor were taken into account. The obtained results of modelling the distribution of total heat losses in the normalized graphical form (for greenhouses with the area of 1500 m^2 it is equal to $Q_{loss \text{ max}}=160 \text{ kW}$, for greenhouses with the area of 3000 m^2 – $Q_{loss \text{ max}}=320 \text{ kW}$) are shown in Figure 5.

Based on the analysis of the modelling results shown in Figure 5, the estimated ranges of changes in total heat loss for greenhouses with typical sizes of 1500 and 3000 m^2 , respectively, are: from 13.1 to 145.8 kW and from 26.2 to 291.6 kW , taking into account the seasonality factors and types and vegetation periods of growing crops.

Thus, taking into account the obtained values of the

components of the input and losses of the heat energy in the greenhouse, the total heat energy (2) in the growing zone can be calculated. The estimated range of changes in the heat energy in the growing zone is obtained taking into account the following factors: seasonality, daily dynamics of solar radiation intensity, current requirements for temperature and humidity of certain types and periods of vegetation, engineering design of industrial greenhouses. The obtained results of mathematical modelling of heat energy dynamics in the graphical form are shown in Figures 6 and 7.

Based on the obtained data, which are shown in Figures 6 and 7, the dynamics of temperature in greenhouses by formula (1) can be estimated.

The differential equation is solved analytically under the following initial conditions: $T_{air \text{ in}}(0) = +3.77^\circ\text{C}$ – for the autumn-winter cycle and $T_{air \text{ in}}(0) = +15.6^\circ\text{C}$ – for the spring-summer cycle. The obtained results of modelling the temperature dynamics in the growing zone for cucumbers and tomatoes, taking into account the vegetation periods and seasonality are shown in Figures 8 and 9.

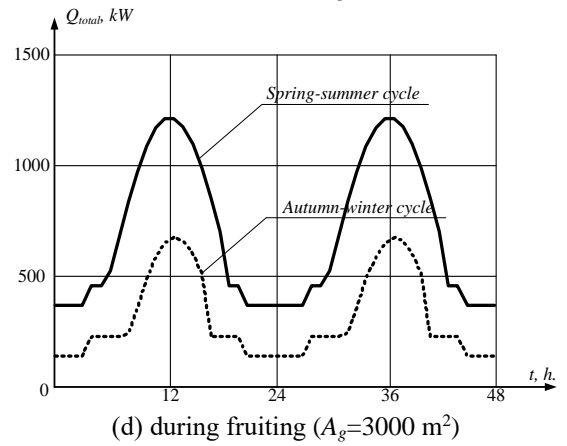
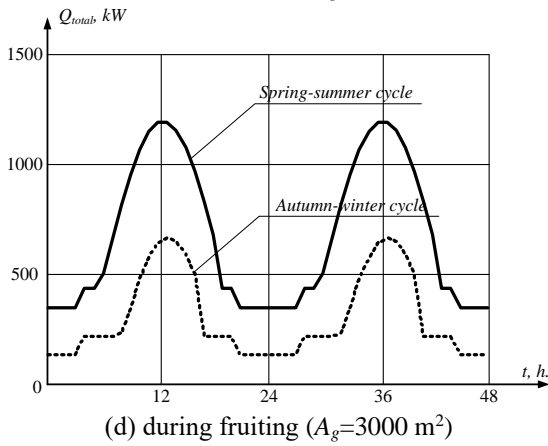
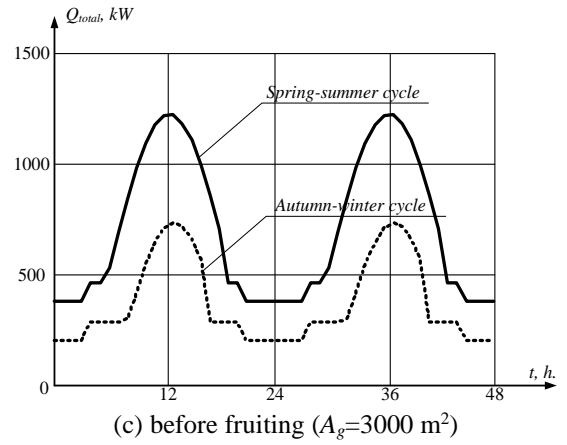
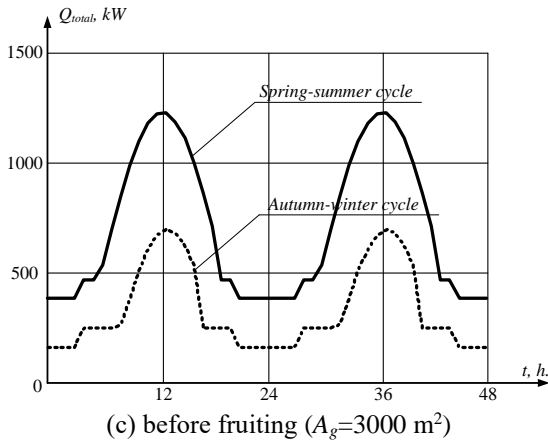
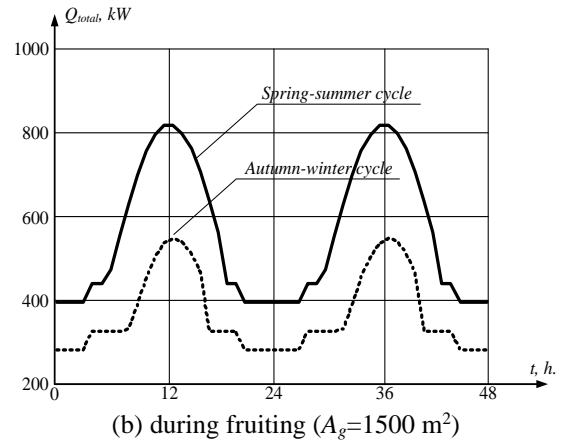
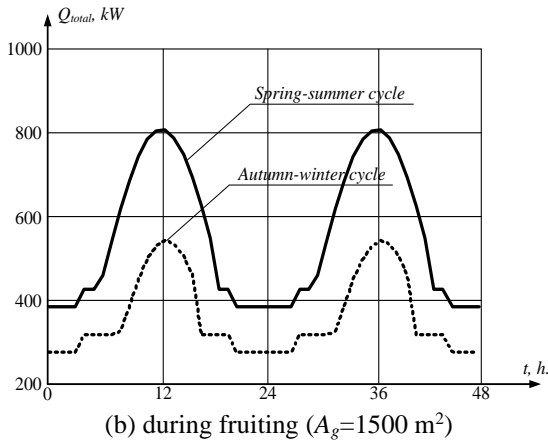
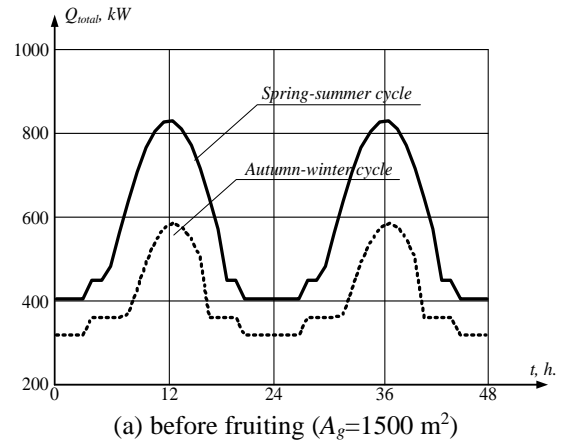
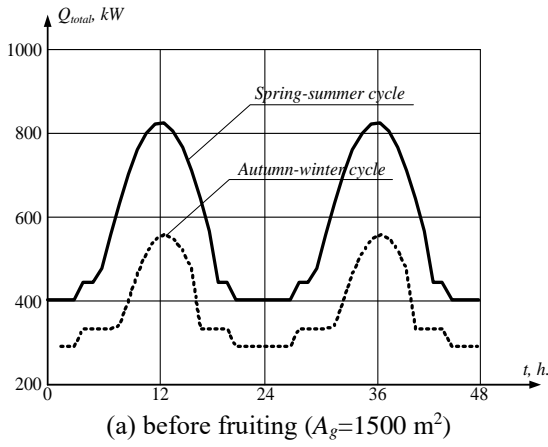


Figure 6. Dependences of heat energy distribution in the greenhouse during cucumber growing

Figure 7. Dependences of heat energy distribution in the greenhouse during tomato growing

By analysing the results of modelling the temperature dynamics in the greenhouse growing zone, which are shown in Figures 8 and 9, the following is established:

- During the cultivation of crops in the autumn-winter cycle under the condition of the heat energy input from the sun, the heating systems and the artificial lighting systems in the amount obtained under the above climatic conditions and source parameters is insufficient, which necessitates increasing the capacity of the heating systems and prompt control of them according to the results of measuring monitoring of internal and external influencing physical and chemical parameters;

- During the cultivation of crops in the spring-summer cycle under the condition of the heat energy input from the sun, the heating systems and the artificial lighting systems, as well as total energy losses in the amount obtained by the above of parameters is overestimated, which necessitates prompt control of ventilation and shading according to the results of measuring monitoring of internal and external influential physical and chemical parameters;

- The estimated values of the constant of the total specific heat energy, which is sufficient to ensure the regulated modes of cultivation of typical greenhouse crops [28], are as follows: for cucumbers before fruiting – $24.7 \text{ kW}\cdot\text{m}^{-2}$, during fruiting – $25.9 \text{ kW}\cdot\text{m}^{-2}$; for tomatoes before fruiting – $29.6 \text{ kW}\cdot\text{m}^{-2}$, during fruiting – $22.2 \text{ kW}\cdot\text{m}^{-2}$;

- Taking into account the types and periods of vegetation, seasonality and geometric dimensions of greenhouses leads to a complex function of the temperature dynamics, which makes it virtually impossible to implement control systems for growing temperatures using the classical laws of automatic control, and therefore there is a need to build subsystems for monitoring and control of air temperature in the greenhouse based on Fuzzy-logic.

3.2 Improved functional diagram

On the basis of the conducted research on the development of the mathematical model of measuring monitoring of air temperature in the greenhouse growing zone, the functional diagram of the measuring monitoring procedure for temperature modes of cultivation was refined, as specified in Figure 10.

Thus, the proposed functional diagram, which is shown in Figure 10, allows implementing the function of control of technological modes of cultivation, which is adaptive to types and periods of vegetation, taking into account seasonal factors and engineering design of greenhouses based on non-destructive measurement monitoring of basic characteristics of internal microclimate of greenhouses and external atmospheric parameters on a real-time basis.

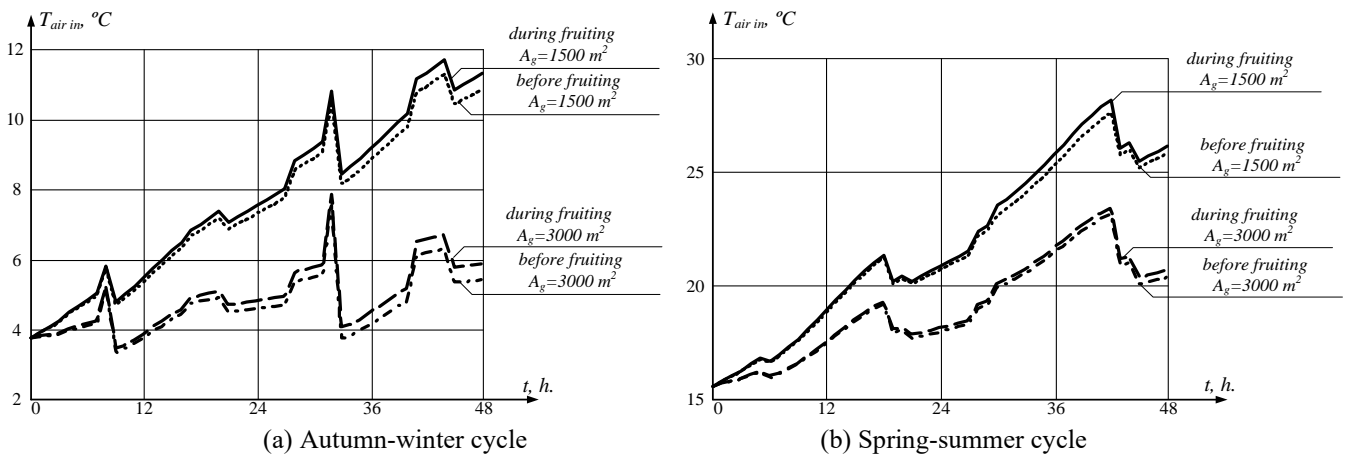


Figure 8. Temperature dynamics during cucumber growing in industrial greenhouses

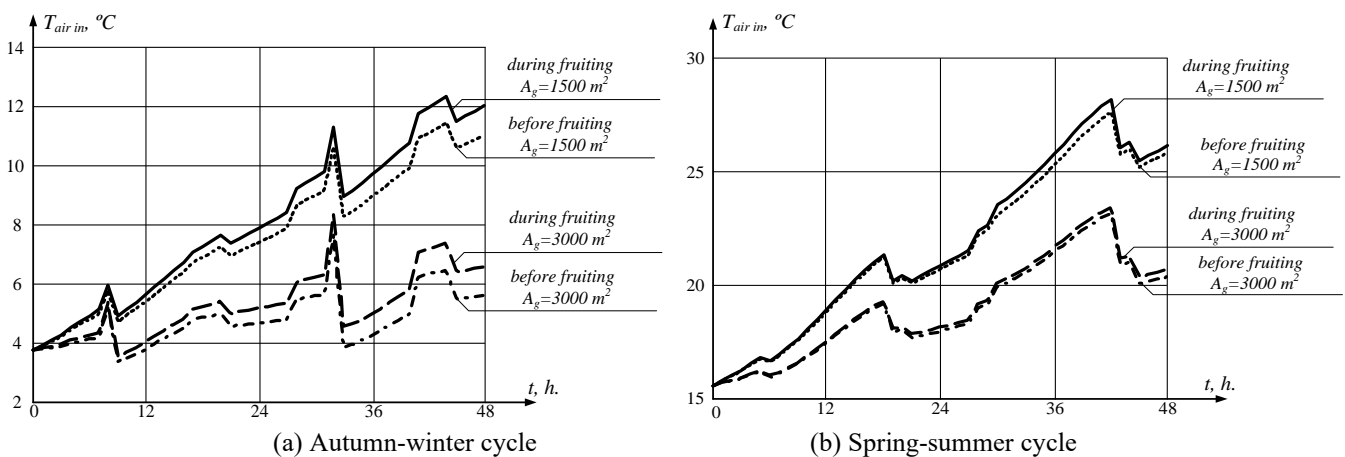


Figure 9. Temperature dynamics during tomato growing in industrial greenhouses

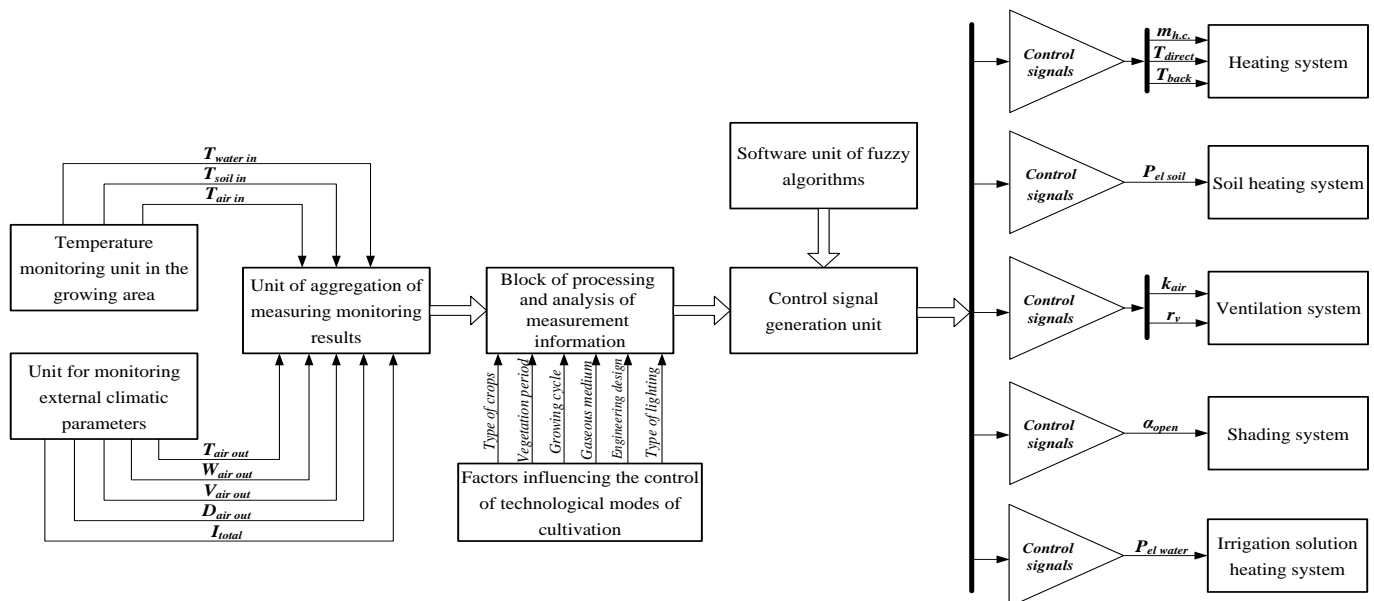


Figure 10. Refined functional diagram of measuring monitoring of the temperature modes of cultivation

4. DISCUSSION AND SUGGESTIONS FOR FUTURE INVESTIGATIONS

The scientific novelty of the obtained research results consists in the development of the mathematical model of the process of measuring monitoring and adaptive control of temperature modes of cultivation by taking into account the types and periods of crops, as well as seasonality and climatic features of greenhouse locations.

The practical significance of the obtained research results lies in the substantiation of the functional diagram of the process of measuring monitoring and adaptive control of the main technological processes of growing greenhouse crops.

Promising areas for further research of the developed mathematical model are: development and testing in laboratory and field conditions of hardware and software of the measuring system, which implements the proposed mathematical model; developing the control unit of technological modes of cultivation and integrating it into the system on the basis of Fuzzy-logic; comprehensive assessment of technical and economic efficiency of the implementation of research results to the production conditions of industrial greenhouse complexes.

5. CONCLUSIONS

The article solves the topical scientific and applied problem of improving the mathematical model of computerized measuring monitoring and control of temperature modes of cultivation in greenhouse conditions taking into account the types and periods of crop vegetation and the seasonality factor, which allowed substantiating scientific and practical provisions of greenhouse energy consumption. The main quantitative and qualitative results of the research are:

- The regularities of the influence of energy from solar radiation, energy coming from the heating system and the thermal component of energy from artificial lighting systems on the total amount of heat energy generated in the greenhouse were established;

- The possible ranges of change of the total heat energy for greenhouses with typical sizes of 1500 and 3000 m², respectively, were estimated: from 420 to 841.1 kW and from 420 kW to 1262.2 kW. The average rate of increase / decrease of the heat energy was also established: for the greenhouses with the area of 1500 m² it is 46.8 kW·h⁻¹; for the greenhouses with the area of 3000 m² it is 93.6 kW·h⁻¹.

- The regularities of the influence of heat losses due to the soil thermal conductivity, due to the soil absorptive capacity, heat transfer due to ventilation and infiltration and heat transfer by condensation on the total amount of the heat energy removed from the growing zone of greenhouses;

- The possible range of change in the loss of total heat energy for greenhouses with typical sizes of 1500 and 3000 m², respectively, is: from 13.1 to 145.8 kW and from 26.2 kW to 291.6 kW;

- The estimated ranges of constant total specific heat energy are obtained, which is sufficient to ensure the regulated modes of cultivation of typical greenhouse crops: for cucumbers before fruiting – 24.7 kW·m⁻², during fruiting – 25.9 kW·m⁻²; for tomatoes before fruiting – 29.6 kW·m⁻², during fruiting – 22.2 kW·m⁻²;

- The functional diagram of the measurement monitoring process was developed, which allows implementing the function of adaptive control of the technological modes of cultivation depending on the types and periods of crop vegetation, taking into account the seasonality factors and engineering design of greenhouses on a real-time basis;

- The promising areas of research on hardware and software of non-destructive computerized monitoring and control of technological modes of cultivation using methods of physical and mathematical and simulation modelling are substantiated.

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NOMENCLATURE

| | |
|-----------------|--|
| A_g | greenhouse surface area (roof and side walls), m^2 |
| C_c | condensation rate on the surface of the greenhouse, $kg \cdot s^{-1} \cdot m^{-2}$ |
| $c_{h.c.}$ | specific heat of the heat carrier, $J \cdot kg^{-1} \cdot ^\circ C^{-1}$ |
| C_ρ | specific heat of air, $J \cdot kg^{-1} \cdot ^\circ C^{-1}$ |
| $D_{air\ out}$ | ambient air flow velocity, dimensionless |
| E_l | required level of illumination of the growing area, lx |
| F_l | area of the greenhouse underlying surface, m^2 |
| F_v | air flow due to ventilation, $m^3 \cdot s^{-1}$ |
| h | heat transfer coefficient, $W \cdot m^{-2} \cdot ^\circ C^{-1}$ |
| I_{sc} | solar constant, $W \cdot m^{-2}$ |
| I_{total} | solar energy falling on the greenhouse surface, $W \cdot m^{-2}$ |
| k_{air} | multiplicity of air exchange, h^{-1} |
| k_{decr} | coefficient of attenuation of solar radiation, dimensionless |
| k_g | soil thermal conductivity coefficient, $W \cdot m^{-1} \cdot ^\circ C^{-1}$ |
| L_v | enthalpy of saturated steam, $J \cdot kg^{-1}$ |
| $m_{h.c.}$ | Heat carrier consumption, $kg \cdot s^{-1}$ |
| n | continuous number of the day in the calendar year, dimensionless |
| $P_{el\ soil}$ | electric power consumption by the ground heating system, W |
| $P_{el\ water}$ | electric power consumption by heating the solution of the heating system, W |
| Q_c | heat transfer through condensation, W |
| Q_g | heat loss due to the soil absorptive capacity, W |
| Q_{gain} | amount of energy entering the greenhouse, W |
| Q_h | heat energy coming from the heating system, W |
| Q_i | heat transfer due to infiltration, W |

| | |
|-----------------|---|
| Q_k | heat loss due to thermal conductivity, W |
| Q_l | thermal component of energy from the artificial lighting systems, W |
| q_l | specific heat release indicator, $W \cdot lx^{-1} \cdot m^{-2}$ |
| Q_{loss} | amount of energy consumed in the greenhouse, W |
| Q_s | useful solar energy entering the greenhouse, W |
| Q_{total} | total heat energy in the growing area, W |
| Q_v | heat transfer through ventilation, W |
| Q_{v+i} | total heat transfer due to condensation and infiltration, W |
| r_v | percentage of opening of mechanisms of ventilation system, dimensionless |
| t | time, h. |
| $T_{air\ in}$ | temperature inside the greenhouse, $^\circ C$ |
| $T_{air\ ou}$ | ambient temperature, $^\circ C$ |
| T_{back} | temperature of the heat carrier removed from the heating system, $^\circ C$ |
| T_{direct} | heat carrier supply temperature, $^\circ C$ |
| T_{soil} | soil temperature, $^\circ C$ |
| $T_{water\ in}$ | temperature of irrigation solution, $^\circ C$ |
| V_g | greenhouse volume, m^3 |
| V_{in} | volume of the greenhouse growing zone, m^3 |
| $v_{air\ in}$ | air flow velocity, $m \cdot s^{-1}$ |
| $v_{air\ out}$ | ambient air velocity, $m \cdot s^{-1}$ |
| $W_{air\ out}$ | ambient humidity, % |
| Z_g | thickness of the soil layer, m |

Greek symbols

| | |
|-----------------|--|
| α_{open} | angle of opening of the mechanisms of the shading system, degree |
| γ | constant of the share of solar radiation entering the greenhouse and causing an increase in temperature, dimensionless |
| η_l | share of the heat entering the room, dimensionless |
| ρ_{air} | air density, $kg \cdot m^{-3}$ |
| τ | greenhouse surface capacity, dimensionless |
| ω | cyclic frequency of solar radiation change, rad. |

Subscripts

| | |
|--------|---|
| max | maximum value of the physical quantity |
| $norm$ | physical quantity normalized to the maximum value |