

NUMERICAL STUDY OF MHD, THERMAL RADIATION FREE CONVECTION HEAT AND MASS TRANSFER FROM VERTICAL SURFACES IN POROUS MEDIA CONSIDERING SORET AND DUFOUR EFFECTS

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ABSTRACT

In the present approach, a two dimensional steady MHD, thermal radiation free convection flow of heat and mass transfer from a vertical surface in porous media has been analyzed numerically by considering Soret and Dufour effects. The governing non linear partial differential equations have been transformed by a similar transformation into a system of ordinary differential equations, which are solved numerically by using implicit finite difference scheme. The dimensionless velocity, temperature and concentration profiles are displayed graphically showing the effects for the different values of the Lewis number, Soret number, magnetic number and radiation parameter.

Keywords: free convection, porous medium, MHD, Dufour, Soret, thermal radiation and finite difference method.

1. INTRODUCTION

Several studies have been found to analyze the influence of the combined heat and mass transfer process by natural convection in a thermal and/or mass stratified porous medium, owing to its wide applications, such as development of advanced technologies for nuclear waste management, hot dike complexes in volcanic regions for heating of ground water, separation process in chemical engineering, etc. Here stratified porous medium means that the ambient concentration of dissolved constituent and/or ambient temperature is not uniform and varies as a linear function of vertical distance from the origin.

When heat and mass transfer occur simultaneously in a moving fluid, the relation between the fluxes and the driving potentials are of more intricate nature. It has been found that an energy flux can be generated not only by temperature gradients but by composition gradients as well. The energy flux caused by a composition gradient is called the Dufour or diffusion-thermo effect. On the other hand, mass fluxes can also be created by temperature gradient and this is the Soret or thermal-diffusion effect. These effects are considered as second-order phenomena, on the basis that they are of smaller order of magnitude than the effects described by Fourier's and Fick's laws, but they may become significant in areas such as geosciences or hydrology.

The study of magneto hydrodynamics (MHD) flows have stimulated extensive attention due to its significant applications in three different subject areas, such as astrophysical, geophysical and engineering problems. Free convection in electrically conducting fluids through an

external magnetic field has been a subject of considerable research interest of a large number of scholars for a long time due to its diverse applications in the fields such as nuclear reactors, geothermal engineering, liquid metals and plasma flows, among the others. Fluid flow control under magnetic force is also applicable in magneto hydrodynamics generators and a host of magnetic devices used in industries. Steady and transient free convection Coupled heat and mass transfer by natural convection in a fluid-saturated porous medium has attracted considerable attention in the last years, due to many important engineering and geophysical applications. Recent books by Nield and Bejan [1] and Ingham and Pop [2, 3] present a comprehensive account of the available information in the field. The MHD free-convection and Mass Transfer flow with Hall current, viscous dissipation, Joule heating and Thermal diffusion is studied by Singh, A.K [4]. Kishan et al [5] studied the MHD free convection heat and mass transfer in a doubly stratified Darcy porous medium considering Soret and Dufour effect with viscous dissipation. Effect of doubly stratification on free convection in Darcian porous medium have been studied by Murthy et al [6]. Vidyasagar et al [7] studied the Mass Transfer effects on radiative MHD flow over a non isothermal stretching sheet and embedded in a porous medium. Srinivasulu and Bhaskar Reddy [8] studied the Thermo-diffusion and Diffusion-thermo effects on MHD boundary layer flow past an exponential stretching sheet with thermal radiation and viscous dissipation.

Lakshmi Narayana and Murthy [9] investigated the effects of Soret and Dufour on free convection heat and mass transfer from a vertical surface in a doubly stratified Darcy

porous medium. They have neglected effect of MHD (Viscous dissipation). Partha et al [10] studied the effect of magnetic field and double dispersion on free convection heat and mass transport considering the Soret and Dufour effects in a Non – Darcy porous medium. Srihari babu and Ramana reddy [11] studied the Mass transfer effects on MHD flow from a vertical surface with ohmic heating and viscous dissipation. Satya sagar Saxena and Dubey [12] studied the MHD free convection heat and mass transfer flow of viscoelastic fluid embedded in a porous medium of variable permeability with radiation effect and heatsource in slip flow regime. Satya sagar Saxena and Dubey [13] studied the Unsteady MHD heat and mass transfer free convection flow of polar fluids past a vertical moving porous plate in a porous medium with heat generation and thermal diffusion.

Sharma and Singh [14] studied the effect of variable thermal conductivity and heat source/sink on MHD flow near a stagnation point on a linearly stretching sheet. Recently, Adrian postelnicu [15] studied the heat and mass transfer characteristics of natural convection about a vertical surface embedded in a saturated porous medium subjected to a chemical reaction by taking account the Dufour and Soret effects. Bhupendra et al [16] investigated the soret and dufour effects on unsteady MHD mixed convection flow past radiative vertical porous plate embedded in a porous medium with chemical reaction. Stanford shateyi et al [17] studied the influence of magnetic field on heat and mass transfer by mixed convection from vertical surface in the presence of hall currents, radiation, soret and dufour effects. Vempati [18] studied the effect of flow parameters on the free convection and mass transfer of an unsteady magneto hydro dynamics flow of an electrically conducting viscous incompressible fluid past an infinite vertical porous plate under oscillatory suction velocity and thermal radiation. Ahmed et al [20] have discussed soret and radiation effect on MHD mass transfer flow with Hall effect in infinite vertical porous plate. Loganathan and Golden Stepha [21] studied chemical reaction effect in the presence of radiation on forced convective heat and mass transfer flow of micropolar fluid.

The objective of this paper is to study simultaneous heat and mass transfer by natural convection from a vertical surface embedded in a fluid saturated Darcian porous medium under the influence of magnetic field including Soret and Dufour effect in the presence of thermal radiation.

2. PROBLEM FORMULATION

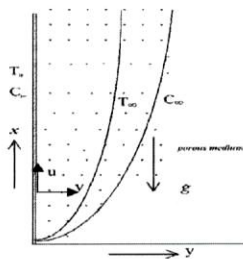


Figure 1. Flow model and physical coordinate system

Consider the natural convection in a porous medium saturated with a Newtonian fluid on a vertical flat plate. The x-coordinate is measured along the surface and the y-coordinate normal to it (see Figure 1). The temperature of the ambient medium is T_∞ and the wall temperature is T_w . The flow along the vertical flat plate contains a species A slightly soluble in the fluid B, the concentration at the plate surface is C_w and the solubility of A in B far away from the plate is C_∞ .

Several assumptions are used throughout the present paper: (a) the fluid and the porous medium are in local thermodynamic equilibrium; (b) the flow is laminar, steady-state and two-dimensional; (c) the porous medium is isotropic and homogeneous; (d) the properties of the fluid and porous medium are constant; (e) the Boussinesq approximation is valid and the boundary layer approximation is applicable; (f) the concentration of dissolved A is small enough. In-line with these assumptions, the governing equations describing the conservation of mass, momentum, energy and concentration can be written as follows

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (1)$$

$$u = \frac{gK}{\nu} [\beta_T (T - T_\infty) + \beta_C (C - C_\infty)] - \frac{\sigma}{\rho} (B_0^2 u) \quad (2)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha_m \frac{\partial^2 T}{\partial y^2} + \frac{D_m k_T}{C_s C_p} \frac{\partial^2 C}{\partial y^2} - \frac{1}{\rho C_p} \frac{\partial q_r}{\partial y} \quad (3)$$

$$u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D_m \frac{\partial^2 C}{\partial y^2} + \frac{D_m k_T}{T_m} \frac{\partial^2 T}{\partial y^2} \quad (4)$$

Where all quantities are defined in the nomenclature. The boundary conditions of the problem are

$$y = 0 : v = 0, T = T_w, C = C_w \quad (5a)$$

$$y \rightarrow \infty : u \rightarrow 0, T \rightarrow T_\infty, C \rightarrow C_\infty \quad (5b)$$

Where T_w, T_∞, C_w and C_∞ have constant values.

Using the Rosseland approximation for radiation Chen [19], radiative heat flux is simplified as

$$q_r = -\frac{4\sigma}{3\alpha^*} \frac{\partial T^4}{\partial y} \quad (6a)$$

Where σ and α^* are the Stefan-Boltzman constant and the mean absorption coefficient, respectively. We assume that the temperature differences within the flow are such that the term T^4 may be expressed as a linear function of temperature. Hence, expanding T^4 in a Taylor series about T_∞ and neglecting higher order terms we get:

$$T^4 \cong 4T_\infty^3 T - 3T_\infty^4 \quad (6b)$$

Using equations (6a) and (6b) equation (3) becomes:

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha_m \frac{\partial^2 T}{\partial y^2} + \frac{D_m k_T}{C_s C_p} \frac{\partial^2 C}{\partial y^2} + \frac{16\sigma T_\infty^3}{3\alpha^* \rho C_p} \frac{\partial^2 T}{\partial y^2} \quad (7)$$

"Equations (1), (2), (4), (5), (7)" are now nondimensionalized using the following quantities:

$$\begin{aligned} \psi &= \alpha_m Ra_x^{1/2} f(\eta), \quad \theta = (T - T_\infty) / (T_w - T_\infty), \\ \phi &= (C - C_\infty) / (C_w - C_\infty), \\ \eta &= \frac{y}{x} Ra_x^{1/2}, \end{aligned} \quad (8)$$

Where the stream function ψ is defined in the usual way

$$u = \frac{\partial \psi}{\partial y}, v = -\frac{\partial \psi}{\partial x} \quad (9)$$

and $Ra_x = gK\beta(T_w - T_\infty)x / (v\alpha_m)$ is the local Rayleigh number. The governing equations become

$$f'(1+M) = \theta + N\phi \quad (10)$$

$$\left(1 + \frac{16}{3R}\right) \theta'' - f\theta' + D_f \phi'' = 0 \quad (11)$$

$$\frac{1}{Le} \phi'' + f\phi' + S_r \theta'' = 0 \quad (12)$$

Where Le, D_f, S_r, R and N are Lewis, Dufour, Soret numbers, Radiation and sustantation parameter, respectively

$$Le = \frac{\alpha_m}{D_m}, D_f = \frac{D_m k_T (C_w - C_\infty)}{C_s C_p \alpha_m (T_w - T_\infty)},$$

$$S_r = \frac{D_m k_T (T_w - T_\infty)}{C_s C_p \alpha_m (C_w - C_\infty)}, N = \frac{\beta_c (C_w - C_\infty)}{\beta_T (T_w - T_\infty)} \quad (13)$$

$$R = \frac{\rho C_p \alpha_m \alpha^*}{\sigma T_\infty^3}$$

We notice that N is positive for thermally assisting flows, negative for thermally opposing flows and zero for thermal-driven flows. The transformed boundary conditions are

$$\begin{aligned} f(0) &= 0, \theta(0) = 1, \phi(0) = 1 \\ \theta &\rightarrow 0, \phi \rightarrow 0 \text{ as } y \rightarrow \infty \end{aligned} \quad (14)$$

The parameters of engineering interest for the present problem are the local Nusselt number and local Sherwood number, which are given by the expressions

$$Nu_x / Ra_x^{1/2} = -\theta'(0), Sh_x / Ra_x^{1/2} = -\phi'(0). \quad (15)$$

3. MATHEMATICAL SOLUTION

The set of non-linear ordinary differential equations (10) - (12) with boundary conditions (14) have been solved numerically, by using Crank Nicolson implicit finite difference method. A step size of $\Delta\eta = 0.01$ was selected to be satisfactory for a convergence criteria of 10^{-5} in all cases. The value of η_∞ was found to each iteration loop by the statement $\eta_\infty = \eta_\infty + \Delta\eta$. In order to see the effect of step size $\Delta\eta$ we ran the code for our model with two different step sizes $\Delta\eta = 0.01, \Delta\eta = 0.001$ and each case we found very good agreement between them.

4. RESULTS AND DISCUSSIONS

Numerical Calculations were carried out for different values of D_f, S_r, M, Le, R and N . For the Purpose of discussing the effect of various parameters on the flow behavior some numerical calculations have been carried out for non dimensional velocity profiles f' , temperature profiles θ , and concentration profiles ϕ .

In Figure 2, the velocity profile D_f, S_r, M presented for fixed values of D_f, S_r, M . The non dimensional velocity f' increases with the increasing of N . In Figure 3, we plotted velocity profile f' for different values of

D_f, S_r, M, N . From Figure 3 we observed that the velocity profile increases with the increasing of Lewis number Le . From Figure 4 we observed that the velocity profile f' increases with the increase of magnetic parameter M .

Figure 5 shows that the velocity profile increases with increase of radiation parameter R . Figure 6 shows that the Temperature profile increases with the increase of Soret number S_r . In Figure 7, the temperature profile plotted for different magnetic parameter M . From this figure we observed that the temperature profile decreases with increase of magnetic parameter M . Figure 8 plotted for different Radiation parameter R . From this figure we observed that the temperature profile increases with the increase of Radiation parameter R . Figure 9 shows the effect of Lewis number Le on the concentration. From Figure 9 we observed that the concentration profile decreases with the increase of Lewis number Le .

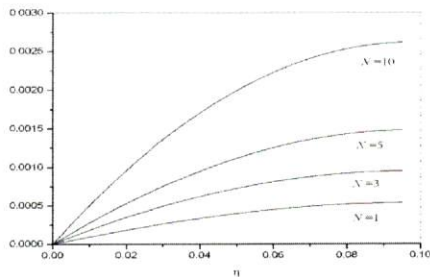


Figure 2. Velocity profiles for different values of N with $S_r = 0.001, D_f = 10.0, M = 0$

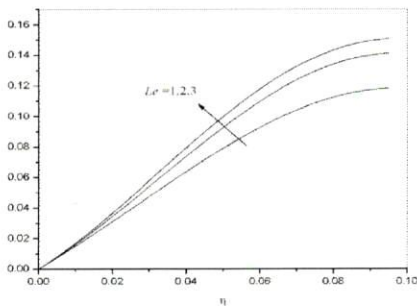


Figure 3. Velocity profiles for different Le with $S_r = 0.001, D_f = 10.0, M = 0, N = 1$.

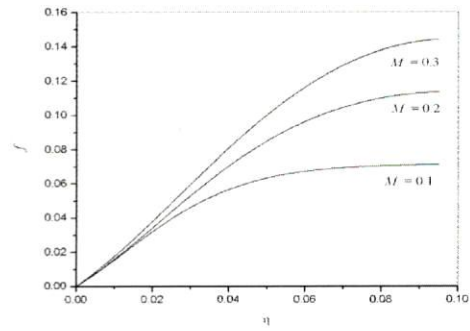


Figure 4. Velocity profiles for different Magnetic parameter with $S_r = 0.001, D_f = 10.0$

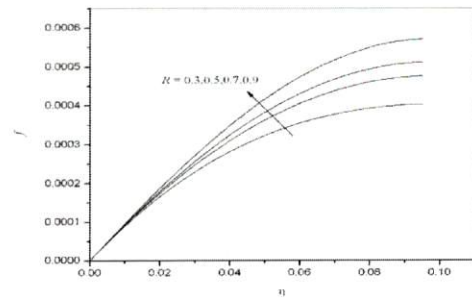


Figure 5. Velocity Profiles for different values of R with $S_r = 0.001, D_f = 10.0, M = 0, N = 1$

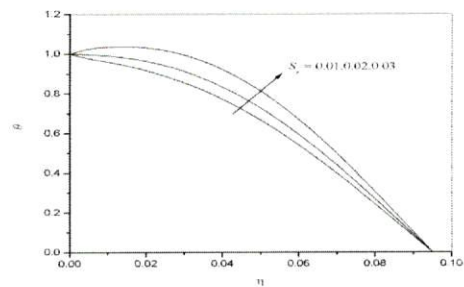


Figure 6. Temperature profiles for different soret parameters with $D_f = 10.0, M = 0, N = 1$.

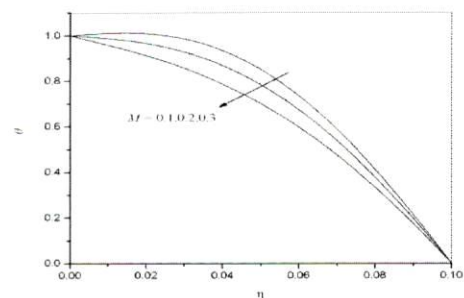


Figure 7. Temperature profiles for different magnetic parameters with $S_r = 0.001, D_f = 10.0$

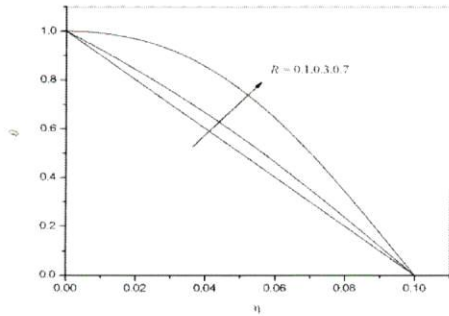


Figure 8. Temperature profiles for different values of R with $S_r = 0.001, D_f = 10.0, N = 1, M = 0, Le = 2$

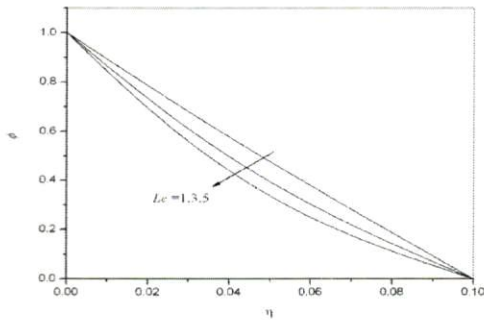


Figure 9. Concentration profiles for different Le with $D_f = 10.0, M = 0, S_r = 0.001$

5. CONCLUSIONS

In this paper we discussed MHD, Free convection heat and mass transfer from vertical surfaces in porous media with solet, dufour effects under the influence of thermal radiation. Using the similarity transformations a set of ordinary differential equations has been derived for the conservation of mass, momentum and species diffusion. These non linear, coupled differential equations have been solved under valid boundary conditions using implicit finite difference method. The conclusions of this paper are

- The velocity profile increases with increase of Magnetic parameter and Lewis number.
- The velocity and temperature profiles increases with the increase of Radiation Parameter.
- As increasing of Soret number the temperature profile increases where as the Concentration profile decreases with increase of Lewis number.

6. NOMENCLATURE

S_r	Soret number
T	Temperature
α^*	Mean absorption coefficient
R	Thermal radiation parameter
x, y	Cartesian co-ordinates along and normal to the surface, respectively
α_m	Thermal diffusivity
σ	Stefan-Boltzman constant
C	Concentration
C_p	Specific heat at constant pressure
C_s	Concentration susceptibility
Ra_x	Local Rayleigh number
u, v	Darcian velocities in the x and y directions
θ	Dimensionless temperature
ρ	Density
ψ	Stream function
β_T	Coefficient of thermal expansion
β_C	Coefficient of concentration expansion
ϕ	Dimensionless concentration
η	Similarity variable
ν	Kinematic viscosity
D_m	Mass diffusivity
f	Dimensionless stream function
K	Darcy permeability
k_T	Thermal diffusion ratio

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