

Potential of Solar Heating for Ultra-Low-Energy Passive Buildings in Cold Regions

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ABSTRACT

The ultra-low-energy (ULE) passive buildings are an important trend of building energy conservation. China has been steadily pushing forward energy-saving policies for buildings, and started to promote the ULE passive buildings. Solar heating has a great application potential in the ULE passive buildings, which are required to consume a very low amount of energy. This paper establishes a simplified model of slab-type residential unit in cold regions of northern China, and correlates the areas of solar heating available on the south wall and the roof with the heating loss of the building, according to the change law of solar radiation. In addition, the calculation formulas for wall and roof heating factors were proposed under the ULE condition, and applied to compute the heating factors of major cities in northern China. The calculation results verify the effectiveness of the formulas. Through statistical analysis, it is learned that wall and roof heating factors are closely correlated with the regional latitude. Hence, the relationship between them were fitted, and verified by a case study in Shijiazhuang, China. The fitted relationship was proved correct, laying the basis for fast and accurate evaluation of solar heating potential in cold regions.

1. INTRODUCTION

In recent years, the environmental awareness is growing among ordinary people. The energy consumption of buildings has become a major influencing factor of the environment [1]. During their operations, buildings consume a huge amount of energy, emitting lots of greenhouse gases (GHGs) into the air [2]. It is a common desire to control building energy consumption [3], and reduce its environmental impact [4]. In developed countries of Europe and North America, many newly constructed buildings consume zero energy [5], and even produce energy [6]. By contrast, the development energy-saving buildings is still in its infancy in China.

In cold regions, heating takes up a major part of building energy consumption [7]. The reduction of heating energy consumption has long been a research hotspot [8]. The relevant studies mostly focus on two aspects. The first aspect is to reduce heating energy consumption through energy-saving design. For example, China has implemented progressive energy-saving policies. The energy-saving goal was 30% in the 1980s, 50% in the 1990s and 65% in the early 21st century [9]. Many cities and regions in China have introduced foreign energy-saving techniques and rolled out policies to develop ultra-low-energy (ULE) passive buildings [10]. The other aspect is to strengthen the use of renewable energy [11] and reduce the proportion of conventional energy sources in the energy structure, e.g. resorting to solar heating [12].

With the advancement of science and technology, great progress has been made in the energy-saving techniques for buildings, including efficient use of solar energy [13], energy-saving envelope structure [14], energy-saving doors and windows [15] and application of phase change heat storage

materials [16]. In northern China, the incentive policies on the ULE passive buildings provide a strong support to the use of solar heating in buildings [17]. Scholars at home and abroad have explored extensively into solar heating [18]. However, these studies are too professional to be mastered by general designers [19]. Little attention has been paid to making general designers determine the solar heating parameters, both rapidly and effectively, as per energy-saving requirements.

Focusing on buildings in cold regions in northern China, this paper correlates the solar energy available on wall and roof in the heating season with the heating energy consumption in the ULE mode, and obtains a fast and accurate method to calculate the potential of solar energy utilization for heating. The research results facilitate the solar heating design for general designers.

2. METHODOLOGY

2.1 Simplified model of solar heating buildings

Before implementing solar heating for a building, it is necessary to determine how much solar energy the building can acquire, and the heating energy consumption of the building throughout the heating season. In winter, the sunshine duration is relatively short. The building mainly acquires the solar energy via the south wall and the roof [20]. Thus, these two surfaces of the building were taken as the research objects. First, a simplified model of slab-type residential unit was established (Figure 1). The maximum size of the wall-mounted solar collector $S_{wall,c}$ can be expressed as:

$$S_{wall,c} = a \times h - a_{win} \times h_{win} \quad (1)$$

The maximum size of the roof-mounted solar collector $S_{roof,c}$ can be expressed as:

$$S_{roof,c}=a \times L \quad (2)$$

The building area of the established model S_{buil} can be calculated by:

$$S_{buil}=a \times L \quad (3)$$

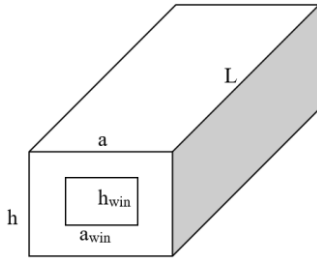


Figure 1. Simplified model of slab-type residential unit

2.2 Solar energy on south wall and roof and unit heat consumption index

The following works should be done before judging if the radiation received on building surfaces can satisfy the heating demand of the building: identifying the law of sunshine and building energy consumption, examining the solar energy received on building surfaces, and determining the heating energy consumption of the building.

2.2.1 Solar radiation acquired on building surfaces

The intensity of direct solar radiation on the ground can be computed by [21]:

$$I_{DN}=I_0 P^m \quad (4)$$

The intensity of direct solar radiation on an inclined surface with random orientation and inclination (Figure 2) can be computed by [22]:

$$I_{D\theta}=I_{DN}[\cos \theta \sin h + \sin \theta \cos h \cos (\alpha - \gamma)] \quad (5)$$

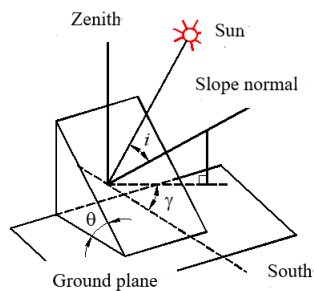


Figure 2. Solar rays on an inclined surface on the ground

The total intensity of solar radiation on an inclined surface with random orientation and inclination can be obtained by [23]:

$$I_{\theta}=I_{D\theta}+\left(\frac{1+\cos \theta}{2}\right) I_{HS}+I_r \quad (6)$$

The inclination of the wall is 90° . Then, the intensity of solar

radiation received by a vertical wall I_{wall} can be obtained by:

$$I_{wall}=I_{DN}[\cosh \cos (\alpha - \gamma)]+\frac{1}{2} I_{HS}+I_r \quad (7)$$

The daily solar radiation energy received by the wall H_{wall} can be described as:

$$H_{wall}=I_{wall} S_{wall} \int_{T_{sta}}^{T_{end}} dT \quad (8)$$

The inclination of the roof is 0° . Then, the intensity of solar radiation received by the horizontal roof I_{roof} can be obtained by:

$$I_{roof}=I_{DN} \sin (h)+\frac{1}{2} I_{HS} \quad (9)$$

The daily solar radiation energy received by the roof H_{wall} can be described:

$$H_{wall}=I_{wall} S_{wall} \int_{T_{sta}}^{T_{end}} dT \quad (10)$$

2.2.2 Heating energy consumption of the building

In a cold region, the heating energy consumption of a building is usually described by the heating loss index q_H . The heating loss of the building refers to the heat supplied to the indoor heating equipment per building area in a unit time to maintain the calculated indoor temperature, under the mean temperature of the heating season:

$$q_H=q_{HT}+q_{INF}+q_{IH} \quad (11)$$

3. RESULTS

Under ideal conditions, the heating demand of a building should be satisfied by the solar energy acquired by the building. Suppose the building has a sufficiently large energy storage device. Then, the building should acquire enough solar energy, such that the thermal energy converted from the solar energy can offset the heating energy consumption of the building. As mentioned before, the building mainly acquires the solar energy via the south wall and the roof in winter. Hence, these two building surfaces are the focus of the subsequent analysis:

3.1 Relationship between solar heating potential of south wall and heating loss of the building

During the heating season, the solar heating energy acquired by the building via the south wall $H_{q,win}$ can be defined as:

$$H_{q,win}=\eta \sum_{Z_0}^Z H_{q,wall} \quad (12)$$

During the heating seasons, the heating energy consumption of the building, i.e. its heating loss Q_{heat} [24], can be described as:

$$Q_{heat}=24 z q_h S_{buil} \quad (13)$$

If the solar heating energy can fully satisfy the heating loss, we have:

$$Q_{heat} = H_{q,win} \quad (14)$$

Sorting out formulas (1)-(14), we have:

$$q_h = \frac{\eta S_{wall} \sum_{Z_{q1}}^Z \int_{T_{min}}^{T_{max}} I_0 p^m \left\{ [\cosh \cos(\alpha - \gamma)] I_{DN} [\cosh \cos(\alpha - \gamma)] + \frac{1}{2} I_{HS} + I_r \right\} dT}{24z S_{buil}} \quad (15)$$

For a specific region, the above formula can be rewritten as:

$$S_{wall} \sum_{Z_{q1}}^Z \int_{T_{min}}^{T_{max}} I_0 p^m \left\{ [\cosh \cos(\alpha - \gamma)] I_{DN} [\cosh \cos(\alpha - \gamma)] + \frac{1}{2} I_{HS} + I_r \right\} dT \quad (16)$$

Formula (16) can be considered as a constant. Here, it is defined as the regional radiation constant N_q for the vertical wall. Then, formula (15) can be expressed as:

$$q_h = \frac{\eta S_{wall}}{S_{buil}} N_q \quad (17)$$

In this case, the heating loss index is only correlated with the heat collection area of the wall, the building area, and the efficiency of the solar collector. Specifically, the heating loss has a positive correlation with the heat collection area of the wall and a negative correlation with the building area.

Hence, formula (15) can be converted into:

$$\frac{N_q}{q_h} = \frac{S_{buil}}{\eta S_{wall}} \quad (18)$$

The heating loss index q_H of buildings is a fixed value in a specific region. Hence, the value of N_q/q_H must be a constant. Here, the N_q/q_H value is defined as the solar heating factor of vertical wall (wall heating factor) M_w :

$$M_w = \frac{S_{buil}}{\eta S_{wall}} \quad (19)$$

3.2 Relationship between solar heating potential of roof and heating loss of the building

Similarly, the solar heating energy acquired by the building via the roof $H_{w,win}$ through the heating season can be defined as:

$$H_{w,win} = \eta \sum_{Z_0}^Z H_{roof} \quad (20)$$

If the solar heating energy can fully satisfy the heating loss, $H_{w,win}$ must be equal to Q_{heat} .

Sorting out formulas (1)-(20), a floor parameter (n) was introduced, for the roof can supply energy to different floors in the building:

$$q_h = \frac{\eta S_{roof} \sum_{Z_0}^Z \int_{T_{min}}^{T_{max}} I_0 p^m \left\{ [\cosh \cos(\alpha - \gamma)] I_{DN} [\cosh \cos(\alpha - \gamma)] + \frac{1}{2} I_{HS} + I_r \right\} dT}{24zn S_{buil}} \quad (21)$$

For a specific region, we have:

$$\frac{S_{roof} \sum_{Z_0}^Z \int_{T_{min}}^{T_{max}} I_0 p^m \left\{ [\cosh \cos(\alpha - \gamma)] I_{DN} [\cosh \cos(\alpha - \gamma)] + \frac{1}{2} I_{HS} + I_r \right\} dT}{24z} \quad (22)$$

Formula (22) can be considered as a constant. Here, it is defined as the regional radiation constant N_r for the horizontal roof. Then, formula (21) can be expressed as:

$$q_h = \frac{\eta S_{roof}}{n S_{buil}} N_r \quad (23)$$

Similar to the calculation principle of the wall, formula (23) can be converted into:

$$\frac{N_r}{q_H} = \frac{n S_{buil}}{\eta S_{roof}} \quad (24)$$

The heating loss index q_H of buildings is a fixed value in a specific region. Hence, the value of N_r/q_H must be a constant. Here, the N_r/q_H value is defined as the solar heating factor of horizontal roof (roof heating factor) M_r :

$$M_r = \frac{n S_{buil}}{\eta S_{roof}} \quad (25)$$

3.3 Validation of the calculation method for solar heating potential

Our calculation method for solar heating potential was verified based on the parameters of Tian Binshou, Shao et al. [25] in their research on winter solar heating for a single-story building in Kangxian County, Gansu Province, China. The specific parameters are as follows:

Geographical location: 33°20'N, 105°36'; building area: 155.76m²; heating time: 8h/d; building heating loss 33W/m²; heating load 45W/m²; overall efficiency of solar heating: 0.40; solar collector area: 21.6m²; collector inclination: 50°; collector location: roof; compensation ratio of north-south orientation: 0.94.

Based on the above parameters, the solar collector area was designed based on our calculation principle. The inclination of the roof-mounted solar collector 50° was substituted into formulas (1)-(20) for calculation. The results show that the roof heating factor with the inclination of 50° was 5.60. If the solar radiation received by the collector needs to supply 67.5% of energy to the building for 8h each day, then the solar collector should be 16.64m² in size. Considering the overall heating load, the area of the solar collector was modified as 22.70m², only 1.1m² smaller than the actual design of 21.6m². The small error (4.9%) indicates that our calculation method can complete preliminary evaluation of solar heating design in an accurate and rapid manner.

3.4 Wall and roof heating factors under the ULE condition

The solar collector is normally mounted on the wall or on the roof. Under the known solar heating efficiency, it is only necessary to compute the wall or roof heating factor to judge if the area of south wall or roof in a region could satisfy the heating demand. The radiation constants and heating factors in main cities of northern China were calculated based on the heating data of the ULE buildings and the *Standard for Energy-Saving Design of Ultra-Low-Energy Passive*

Table 1. Radiation constants and heating factors in main cities of northern China

Serial no.	City	Latitude	Heating period	Number of heating days (day)	Heat loss per unit time (h W/m ²)	Wall radiation factor (h W/m ²)	Wall heating factor	Roof radiation factor (h W/m ²)	Roof heating factor
1	Xi'an	34°15'	11.15-3.15	121	9.80	158.72	16.20	126.23	12.88
2	Zhengzhou	34°44'	11.15-3.15	121	9.80	157.77	16.10	123.8	12.63
3	Qingdao	36°04'	11.15-4.5	145	9.90	154.91	15.65	133.89	13.53
4	Jinan	36°40'	11.15-3.15	120	9.90	153.42	15.50	114.05	11.52
5	Taiyuan	37°51'	11.1-3.30	150	10.19	152.80	14.99	121.57	11.93
6	Shijiazhuang	38°03'	11.15-3.15	121	9.95	149.86	15.06	107.17	10.77
7	Dalian	38°54'	11.5-3.30	145	10.09	149.91	14.86	114.7	11.37
8	Tianjin	39°17'	11.15-3.15	121	10.05	146.70	14.60	101.64	10.12
9	Beijing	39°54'	11.15-3.15	121	9.95	144.69	14.54	98.05	9.85
10	Hohhot	40°48'	10.15-4.15	185	10.44	146.81	14.06	118.3	11.33
11	Shenyang	41°48'	11.1-3.30	150	10.39	141.63	13.63	100.6	9.68
12	Urumqi	43°46'	10.15-4.15	185	10.68	138.99	13.01	104.2	9.75
13	Changchun	43°55'	10.25-4.10	170	10.63	137.04	12.89	98.68	9.28
14	Harbin	45°45'	10.20-4.20	185	10.73	132.85	12.38	98.67	9.19

3.5 Correlation between heating factors and latitude

The following laws can be discovered from the data in Table 1:

(1) The heating factors have certain correlations with latitude: the higher the latitude, the smaller the heating factors,

and the more unfavorable for solar heating (Figure 3).

(2) The correlation coefficient between latitude and wall heating factor was -0.997, indicating a high correlation between the two factors; the correlation coefficient between latitude and roof heating factor was -0.88, also a sign of high correlation.

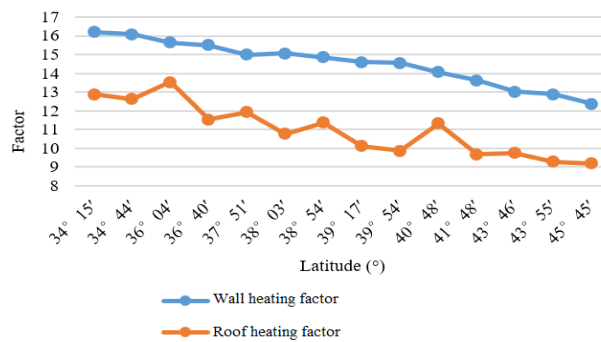


Figure 3. Relationship between latitude and heating factors

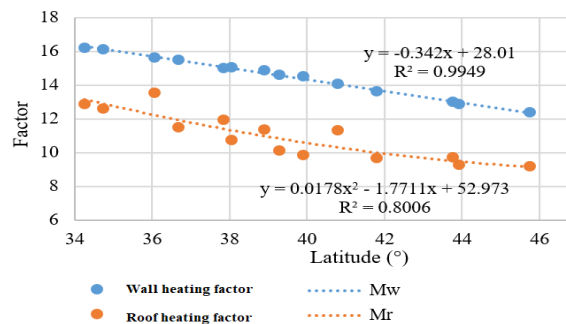


Figure 4. Fitted relationship curves between latitude and heating factors

Figure 4 can be obtained through data fitting. The correlation between latitude and wall heating factor can be obtained from the fitted relationship curves. The correlation coefficient (0.9949) can be determined by:

$$M_w = -0.342\phi + 28.01 \quad (26)$$

The correlation between latitude and wall heating factor can also be obtained from the fitted relationship curves. The correlation coefficient (0.8006) can be determined by:

$$M_r = 0.0178\phi^2 - 1.7711\phi + 52.973 \quad (27)$$

The wall and roof heating factors in cold regions of northern China can be derived through the above two formulas.

4. DISCUSSION

4.1 Verification of heating factors

First, Shijiazhuang (latitude: 38°03'N) was adopted to verify the heating factors. The wall heating factor was calculated by formula (26) as 15.00, 4% smaller than the actual value (15.06) obtained by formulas (1)-(19); the roof heating factor was calculated by formula (27) as 11.35, 5.14% greater than the actual value (10.77) obtained by formulas (1)-(20). The results are acceptable for preliminary evaluation of solar heating design; Next, Tianjin (latitude: 39°17') was adopted to verify the heating factors. The wall heating factor was calculated by formula (26) as 15.00, 2.8% greater than the actual value (14.58) obtained by formulas (1)-(19); the roof heating factor was calculated by formula (27) as 10.12, 6.89% smaller than the actual value (10.87) obtained by formulas (1)-(20). The results are acceptable for preliminary evaluation of solar heating design. The above results show that formulas (26) and (27) can be used for quick calculation of regional heating factors in the design phase of solar heating plans for buildings.

4.2 Evaluation of solar heating potential based on heating factors

According to relevant regulations on energy-saving of residential buildings, the window-wall ratio on the south wall of residential buildings should not surpass 0.35 [26]. Thus, about 65% of the south wall can be used to receive solar energy. On this basis, the area of the wall of a building that can receive solar energy can be described as:

$$S_{wall} = 0.65 \times a \times h \quad (28)$$

$$S_{bui} = a \times h \times L \quad (29)$$

In this case, formula (19) can be converted into:

$$M_w = L / (0.65 \eta h) \quad (30)$$

According to Table 1, the wall heating factor is 15.00 in Shijiazhuang. Suppose the solar heating efficiency η is 0.35. Then, the value of L/h was 3.31. If the floor height is 2.8m, the building solely relying on the south wall for heating should not be deeper than 9.23m. However, the normal depth of residential buildings is about 12m. Obviously, it is impossible for ULE buildings in Shijiazhuang to realize solar heating

based on the south wall only. The south wall could supply about 75% of the heating energy. The remaining 25% can be supplied by the roof solar collector. The area of the roof of a building that can receive solar energy can be described as:

$$S_{roof} = a \times L \quad (31)$$

$$S_{bui} = n \times a \times L \quad (32)$$

where, n is the number of floors in the building.

In this case, formula (19) can be converted into:

$$M_w = n / \eta a \times h \times L \quad (33)$$

The n value can be calculated as 3.54, i.e. the solar energy collected on the roof can support the heating of 3.54 floors. Since the roof only needs to provide 25% of the heating energy to each floor, the solar energy collected by the roof and south wall combined can satisfy the heating demand of a 14-story building. Therefore, the ULE passive buildings in Shijiazhuang can adopt solar heating in winter.

5. CONCLUSIONS

The concept of solar heating factor was proposed, allowing the designers to evaluate the solar heating effect early in the design. The wall and roof heating factors were correlated with latitudes of major cities in northern China. In this way, the relationship between heating factors and latitude was summarized for the ULE passive buildings, and verified through a case study on a solar heating residential building in Kangxian County, Gansu Province, China. The author also put forward the calculation method for the relationship between the solar collector area needed for solar heating and building area, facilitating the design and calculation of solar heating in the design phase.

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NOMENCLATURE

- a* Room width, m
h Room height, m

H	Total radiation, kWh
$H_{D\theta}$	Total daily radiation of inclined surface
I	Radiation intensity, W/m^2
I_0	Solar constant: 1,353, W/m^2
HIS	Intensity of diffuse sky radiation, W/m^2
I_r	Intensity of direct solar radiation on the ground, W/m^2
L	Room depth, m
m	Air mass
M_r	Roof heating factor
M_w	Wall heating factor
N_q	Regional wall radiation constant
N_r	Regional roof radiation constant
P	Atmospheric transparency
q_H	Building heat loss, W/m^2
q_{HT}	Heat loss via the envelope structure per unit building area, W/m^2
q_{INF}	Heat loss via air permeation per unit building area, W/m^2
q_{IH}	Indoor heat gain per unit building area, W/m^2

Q	Heating consumption, kWh
S	Area, m^2
T	Sunshine duration, h
T_{sta}	Time of sunrise, h
T_{end}	Time of sunset, h
z	Number of days in the heating season, d

Greek symbols

θ	Inclination, $^\circ$
α	Solar azimuth, $^\circ$
γ	Azimuth of inclined surface, $^\circ$
η	Utilization efficiency

Subscripts

<i>buil</i>	Building
<i>roof</i>	Roof
<i>win</i>	Window
<i>wall</i>	Wall