Performance Evaluation of a 2DOF_PID Controller Using Metaheuristic Optimization Algorithms

Mahmood H. Enad1, Raaed Faleh Hassan2, Ali A. Khaleel Mahmoud2, Amjad Jaleel Humaidi3

1 Electrical Techniques Department, Technical Institute of Karbala, Al-Furat Al-Awsat Technical University, Najaf 54001, Iraq
2 Department of Control and Automation Engineering Techniques, Electrical Engineering Technical College, Middle Technical University, Baghdad 10044, Iraq
3 Control and Systems Engineering Department, University of Technology, Baghdad 10066, Iraq

Corresponding Author Email: Amjad.j.humaidi@uotechnology.edu.iq

Received: 10 February 2024
Revised: 13 May 2024
Accepted: 20 May 2024
Available online: 25 June 2024

Keywords:
2DOF_PID, optimization, metaheuristic, PSO, genetic, dragonfly

ABSTRACT

This paper explores the advantages of the Two Degree of Freedom Proportional-Integral-Derivative (2DOF_PID) controller in tracking the reference signal and rejecting the disturbance signal at the same time. Three types of metaheuristic optimization algorithms are employed for tuning the controller’s parameters which are Particle Swarm Optimization (PSO), Genetic Algorithm (GA), and Dragonfly Algorithm (DA). These three algorithms have in common that they combine the exploratory concept (global search) and the exploitative concept (local search) in order to reach the optimal global solution. The effectiveness of these algorithms was taken advantage of to improve the performance of the control system that contains the controller. Second and third order plants were adopted for the purpose of testing, evaluating, and comparing the performance of the control system. This aim was accomplished by using each of the optimization algorithms for each plant. The simulation results showed the superiority of the DA in terms of obtaining the lowest value of the Integral Absolute Error (IAE) as the cost function.

1. INTRODUCTION

Due to its ease of use and resilience, the three-term, or the Proportional-Integral-Derivative (PID) controller is the most often employed in a wide range of industrial systems. The key advantage is the ease with which a PID controller may be tuned without requiring much control knowledge. Many academics have been inspired to offer design ideas for PID controllers. As a result, there is a wide collection of tuning rules in the literatures [1, 2].

Ziegler-Nichols presented the basic idea for adjusting the PID controller in 1942, and it is based on a mathematical formula that represents the PID parameters as functions of specific process parameters [3]. Later, many forms of self-tuning PID controllers were proposed [4-9].

PID controller automatic tuning and stabilization have been the subject of extensive research throughout the years [10-20]. While PID controller tuning procedures have shown efficacy in regulating lower-order processes, they frequently produce unsatisfactory results when applied to higher-order and nonlinear systems. Direct optimization, which frequently involves the solving of a nonconvex problem, is a highly effective method for optimizing PID parameters in such complicated systems [21-25].

On the other hand, fuzzy logic control and neural networks, which are the field of computational intelligence, have been used to deal with the problem of PID controller optimization. In the neural networks, the convergence time at the training cycle become inconvenient. The generation of the fuzzy membership function in the fuzzy logic control system build upon data analysis, model of the system and the designer skills [26-28]. Nowadays, metaheuristic algorithms which are evolutionary and nature-inspired optimization algorithms provide an alternative way to tune PID controllers. These algorithms use natural processes such as species evolution or particle swarm behavior to iteratively search for the best combination of parameters. The goal is to mimic nature's natural selection process or collective behavior to achieve optimal or near-optimal solutions [29, 30]. Despite the rapid development in methods for tuning the conventional PID controller, there remains an obstacle that hinders the effectiveness of the controller and is related to its structure [31, 32]. The PID controller represents a system with one degree of freedom. This means that the closed-loop transfer function of this system depends on only one variable, which is the error (the difference between the measured value and the desired value). However, although this system is robust and effective in many applications, it can face challenges in achieving reference input tracking and disturbance rejection simultaneously. Achieving reference input tracking and disturbance rejection simultaneously can be difficult in some cases, especially when the available information is limited or when the system is highly nonlinear. In those cases, the use of advanced control techniques or more complex models may be considered to achieve the desired performance [33, 34]. In order to overcome this limitation of traditional 1DOF_PID, a
two-degree-of-freedom (2DOF_PID) controller has emerged where setpoint tracking and disturbance rejection can be achieved separately. This division increases the system's ability to deal with different challenges and provide an effective response to requirements [35-37].

Combining the robustness of metaheuristic optimization approaches with the advantages of a 2DOF-PID controller is the main task of this paper. In conjunction with concepts of exploration and exploitation, three categories of metaheuristic algorithms are employed, which are PSO, GA, and DA. These algorithms are used to fine-tune the controller's parameters to significantly increase the performance of typical second- and third-order linear time invariant (LTI) plants.

2. TWO DEGREE OF FREEDOM PID CONTROLLER

The use of a 2DOF PID controller can result in good performance for both set-point tracking and disturbance rejection. Figure 1 depicts the control system in which the general structure of the proposed 2DOF_PID controller is employed.

![Figure 1. General structure of the control system based on 2DOF_PID controller](Image)

As its name suggests, 2DOF_PID controller contains an additional degree of freedom compared to the traditional PID controller, as the components of the controller are divided into feedforward \( G_f(s) \) compensator and series or feedback \( G_fb(s) \) compensator [37]. The series or feedback compensator has the natural form of the conventional PID controller:

\[
G_fb(s) = K_p\left(1 + \frac{1}{T_1 s} + T_0 s\right)
\]  

where, \( K_p \) is the proportional gain, \( T_1 \) is the integral time constant, and \( T_0 \) is the derivative time constant.

The feedforward part has the form of the conventional PD compensator:

\[
G_f(s) = -K_p(\alpha + \beta T_0 s)
\]  

where, \( \alpha \) and \( \beta \) are the additional two parameters for 2DOF_PID controller. This controller receives two input which are the set point \( R(s) \), and \( Y'_f(s) \).

\[
Y'_f(s) = H(s)Y(s), H(s) \text{ is the transfer function of the feedback sensor, and } Y'(s) \text{ is the system response } Y(s) \text{ corrupted with noise signal } N(s). \text{ The output of the controller is the control signal } U(s) \text{ which drives the controlled process}
\]

\( G_p(s). \) The system response \( Y(s) \) is governed by the control signal \( U(s) \) and disturbance \( d(s) \). The zero steady state error of the setpoint tracking and disturbance rejection can be achieved if the following assumptions are satisfied:

1. The feedback sensor \( H(s) \) is unity, and the noise \( N(s) \) is zero.
2. The disturbance signal \( d(s) \) is entered directly to the controlled process \( G_p(s) \), i.e., \( G_d(s) \) is unity.

Therefore, the control system will be modified as shown in Figure 2.

![Figure 2. Modified structure of the control system based on 2DOF_PID controller](Image)

The following relationship will dictate how the system responds: set point tracking and disturbance rejection:

\[
Y(s) = \begin{bmatrix}
G_p(s)[G_fb(s) + G_f(s)] \\
1 + G_p(s)G_fb(s)
\end{bmatrix}
\begin{bmatrix}
R(s) \\
d(s)
\end{bmatrix}
\]

where, the \( G_p(s) \) is the controlled plant.

3. METAHEURISTIC OPTIMIZATION ALGORITHMS

A metaheuristic algorithm is a structure that is generally applied to various optimization problems and needs minor modifications to deal with the specific problem. The need for metaheuristic algorithms has emerged for the following reasons:

1) Metaheuristic algorithms are easy to understand and simple, which increases the ability to make decisions.
2) Metaheuristic algorithms are effective in finding the exact solution [38].

In this paper, three algorithms from the family of metaheuristic algorithms will be adopted for the purpose of studying their effectiveness in tuning the 2DOF_PID controller. These algorithms are:

**Genetic Algorithm**

Genetic algorithm is one of the optimization algorithms that relies on a random global search method which simulates the evolution of natural inheritance based on the concept of survival of the fittest. The flowchart of the genetic algorithm
behavior is explained as shown in Figure 3 [39].

![Figure 3. GA flow chart](image)

**Particle Swarm Optimization**

This algorithm is originally presented in 1995 by Eberhart and Kennedy, it is a metaheuristic optimization method designed to resemble the social behavior of a swarm of birds or a human group [32, 40]. To employ this algorithm, a collection of particles is used, called a swarm, characterized by their positions and velocities. The swarm is distributed randomly in the solution search area and according to the specified ranges for the elements of the problem targeted in the optimization process. The dimensions of the search space \( n \) are determined by the required number of variables in the design, where the speed and position of each particle are represented by the following vectors:

\[
V_i = [v_{i1}, v_{i2}, ... , v_{in}]
\]

\[
X_i = [x_{i1}, x_{i2}, ... , x_{in}]
\]

The backbone of the optimization process is to update the position and velocity of each particle in each iteration according to the following relations:

\[
w = w_{up} - (w_{up} - w_{low}) \left( \frac{t}{t_{max}} \right) \quad (4)
\]

\[
v_{i}(t + 1) = C(wv_{i}(t)) + c_{1}r_{1}(P_{l} - x_{i}(t)) + c_{2}r_{2}(P_{g} - x_{i}(t)) \quad (5)
\]

\[
x_{i}(t + 1) = x_{i}(t) + v_{i}(t + 1) \quad (6)
\]

Table 1 lists the symbols appear in Eqs. (4)-(6).

![Table 1. Symbols of Eqs. (4)-6](image)

The functional behavior of the PSO algorithm is described by the flowchart depicted in Figure 4.

![Figure 4. PSO flow chart](image)

**Dragonfly Algorithm**

Dragonfly algorithm is an interesting recent optimization algorithm presented in 2016 by Mirjalili [41]. This algorithm is inspired by the dynamic behavior of dragonflies in the migration process, and the static behavior in the feeding process [42, 43]. Migration and feeding processes of a dragonfly swarm create the exploitation and exploration phases, respectively. The behavior of the dragonfly’s swarm consists of the following primitives:

1. **Separation**, which is the process of collision avoidance between swarm individuals and can be represented by the following relation:
where, $P$ and $P_j$ are the positions of current and jth neighboring individuals respectively, $M$ is the number of neighboring individuals.

(2) Alignment, which represents the compatibility of the individual’s speed with the speed of individuals in the same group, and it is governed by the following relation:

$$A_i = \frac{\sum_{j=1}^{M} V_j}{M}$$

where $V_j$ is the velocity of the jth individual.

(3) Cohesion is the goal of individuals to maintain their position at the center of the group, and its mathematical representation is:

$$C_i = \frac{\sum_{j=1}^{M} P_j - P}{M}$$

(4) Attraction, which is the movement of individuals towards a food source, and it is mathematically described by:

$$F_i = F_p - P$$

where, $F_i$ is the food source of ith individual, and $F_p$ is the food source position.

(5) Distraction, which is the diversion from the enemies, and its mathematical model is:

$$E_i = E_p + P$$

where, $E_i$ is the position of the ith individual enemy, and $E_p$ is the enemy’s position.

The positions of dragonfly’s individuals are updated inside the search space according to the step vector $\Delta P$ which is governed by the following relation:

$$\Delta P_i(t + 1) = s S_i + a A_i + c C_i + f F_i + e E_i + \omega \Delta P_i(t)$$

where, $s$, $a$, $c$, $f$, $e$ are the weights of separation, alignment, cohesion, attraction, and distraction respectively, $w$ is the inertia weight, and $t$ is the iteration number. Therefore, the position of ith individual at the next iteration is described by:

$$P_i(t + 1) = P_i(t) + \Delta P_i(t + 1)$$

Eq. (14) represents the updated dragonfly location, however if there are no adjacent solutions, the following modified equation must be used:

$$P_i(t + 1) = P_i(t) + Levy(d) \times P_i(t)$$

where, $d$ imply the position vectors' dimension, and the Levy function is determined by:

$$Levy(d) = 0.01 \times \frac{r_1 \times \Gamma(\beta)}{|r_2|^\beta}$$

where, $r_1$ and $r_2$ are random numbers between 0 and 1, $\beta$ is constant. The algorithm of dragonfly is illustrated in flowchart shown in Figure 5.

![Figure 5. DA flow chart](image-url)

The ability of the metaheuristic optimization algorithms to explore complex search spaces, address non-convex objective functions, and continuously adapt to find optimal solutions according to the characteristics of the problem, ensuring a balance between exploration and exploitation. All these characteristics make these algorithms powerful support tools for finding 2DOF-PID controller parameters that contribute to improving the control system in different applications.

4. SYSTEM CONFIGURATION

The optimization algorithms stated earlier have been adopted individually to tune the 2DOF PID controller parameters in order to enhance the control system's efficacy and performance, the resulting configured system is illustrated in Figure 6.

The error signal $e(t)$ which is the difference between $r(t)$ and $y(t)$ is delivered to the optimization algorithm block. The optimization algorithm block is adjusting the controller parameter to minimizes the cost function. Two controlled plants $G_p(s)$ were suggested to validate the performance of the control system. The first plant was a second order plant, while the other was a third order plant. The transfer functions of these plants are described as follows.

$$G_p(s) = \frac{0.438 s + 0.033861}{s^2 + 0.086096 s + 0.04215}$$

$$G_p(s) = \frac{-0.01261 s^2 + 335 s + 9.967e08}{s^3 + 6000 s^2 + 1.1e07 s + 6.979e09}$$
5. RESULTS AND DISCUSSION

This section presents the results of the simulation conducted on the control system that included the 2DOF_PID controller and the controlled plant. The results showed the performance of the control system when using the two plants described in Eqs. (16) and (17) separately. The three types of optimization algorithms mentioned above were used to adjust the controller elements, which leads to minimizing the Integral Absolute Error (IAE). The behavior of the control system was studied in each case, which is associated with the presence of a stepped reference signal and the appearance of a disturbance signal for a specific period.

The behavior of plant1 with transfer function described in (16) is shown in Figure 7. When the PSO is used, the behavior of the control system based for tracking the reference input and rejecting the disturbance is shown in Figure 7 (a). The effect of using GA on the system’s response is depicted in Figure 7 (b), while Figure 7 (c) shows the effect of using DA on the system’s performance towards the reference input signal and the disturbance signal.

From observing the simulation results, the response of the system to track the reference signal and reject the disturbance gave acceptable results in terms of low IAE, as
shown in Table 2.

<table>
<thead>
<tr>
<th>Function</th>
<th>Plant1</th>
<th>Plant2</th>
</tr>
</thead>
<tbody>
<tr>
<td>IAE</td>
<td>0.4456</td>
<td>0.148</td>
</tr>
<tr>
<td></td>
<td>0.0653</td>
<td>0.287</td>
</tr>
<tr>
<td></td>
<td>0.28</td>
<td>0.27</td>
</tr>
</tbody>
</table>

### 6. CONCLUSIONS

In this paper, the superiority of the 2DOF PID controller for tracking the reference input and rejects the disturbance was studied. The influence of employing three types of metaheuristic optimization algorithms in tuning this controller for controlling two types of plants was examined. Simulation results showed the ability of these algorithms to find the controller’s parameters that result in minimizing the cost function IAE (i.e., obtaining the global solution). Although the three optimization algorithms contributed to improving the performance of the control system and produced an acceptable response, the DA algorithm was the best. The advantage of DA resulted from its contribution to finding the lowest value for IAE when using the controller to control both plants. The reason the DA is better is that it focuses on independent moving of the individuals, giving it a greater range of exploration. Also, it is able to promptly adjust to changes in the problem domain, escaping from the local optima and keep looking for the global optimal solution.

The significant outcomes of the simulation procedure indicate that it is imperative to confirm the effectiveness of metaheuristic optimization algorithms in identifying the ideal controller parameters under uncertainty or dynamic system variations. Furthermore, this approach’s efficacy needs to be evaluated with Multiple-Input-Multiple-Output (MIMO) systems and/or higher order systems with additional cost functions.

### REFERENCES


output feedback control and remote PID design for networked motor systems. IEEE Transactions on Industrial Electronics, 58(12): 5396-5405. https://doi.org/10.1109/TIE.2011.2107720


