Thermodynamic Modelling for the Prediction and Optimisation of Long-Term Performance in Wooden Structures

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ABSTRACT

Over time, ancient wooden structures undergo challenges in structural integrity and stability, influenced by various environmental conditions such as temperature fluctuations and humidity variations. Maintenance and protection of this invaluable architectural heritage require precise performance predictions and optimisations. While existing research has delved deeply into performance prediction of wooden structures, it predominantly focuses on empirical observations and experimental analyses, with minimal establishment and validation of theoretical models. Moreover, extant methods for prediction and optimisation often overlook the strain variation of wood under different temperatures and the stochastic nature of environmental factors. This study seeks to address this research gap by investigating the relationship between strain in the grain direction of ancient wooden beams and temperature, and by formulating a comprehensive thermodynamic model. Additionally, a novel optimisation approach using the chicken swarm optimisation (CSO) algorithm has been introduced to further refine performance parameters of wooden structures. By integrating the theoretical model with the CSO, this research offers a novel perspective and methodology for the prediction and optimisation of the long-term performance of wooden structures.

1. INTRODUCTION

Wooden structures, especially those found within ancient buildings, have long been regarded as invaluable architectural heritage due to their natural material attributes and historical traces [1-4]. Influenced by a myriad of environmental conditions, such as temperature fluctuations and changes in humidity over extended historical periods, these structures' physical properties are affected, and challenges are posed to their long-term structural integrity and stability [5-7]. Precise performance predictions and optimisations have emerged as pressing needs for the maintenance and protection of these architectural legacies.

Ancient wooden structures hold an irreplaceable position in history and culture [8-11]. Insights into their performance shifts under varying environmental conditions not only facilitate scientifically-grounded protective measures, ensuring prolonged safety and stability but also offer valuable references for modern wooden structure design and construction [12-17]. Moreover, by forecasting the long-term performance of wooden structures, scientific foundations can be provided for the restoration, reinforcement, and maintenance of ancient buildings, thus potentially extending their lifespan and preserving more historical heritage for future generations.

While numerous studies address the performance prediction of wooden structures, the majority place emphasis on empirical observations and experimental analyses, with fewer venturing into the establishment and validation of theoretical models [18-21]. Additionally, prevalent prediction methods often overlook wood's strain variations at different temperatures, which might result in prediction discrepancies. Furthermore, traditional optimisation approaches are primarily rooted in deterministic models, disregarding the stochastic nature of environmental factors, possibly rendering optimisation outcomes less accurate and robust.

In this study, a deep dive is taken into the relationship between strains in the grain direction of ancient wooden beams and temperature, culminating in the development of a comprehensive thermodynamic model. This establishes a robust theoretical foundation for the accurate prediction of wooden structures' performance under various environmental conditions. To further refine the performance parameters of these wooden structures, the CSO, a novel and efficient optimisation approach simulating the foraging behaviour of chicken flocks to locate optimal solutions, is introduced. By marrying these two core components, a novel and scientific methodology for the long-term performance prediction and optimisation of wooden structures is presented, bearing significant implications for both the protection of ancient architecture and applications in modern wooden constructions.

2. CONSTRUCTION OF THE THERMODYNAMIC MODEL FOR WOODEN STRUCTURES

Wooden beams in ancient buildings hold significant structural and cultural importance. Not only are they integral to the structural framework, but they also bear rich historical and cultural significance. Ensuring their long-term stability and safety becomes paramount. Over prolonged usage, such beams often undergo the influence of various environmental
factors, with temperature fluctuations being one of the primary contributors. Thermal expansion and contraction, arising from temperature changes, can induce strains, adversely affecting the integrity and stability of these wooden structures.

While numerous studies have addressed the performance of wooden structures in ancient buildings, most are anchored in empirical observation and experimental analysis. By establishing a thermodynamic model, a more comprehensive and scientific perspective can be pursued, facilitating quantitative analysis and prediction of strain in these beams, thereby enhancing the scientific rigor and innovation of such studies. Given this backdrop, ancient wooden beams were selected as the study’s subject. By adopting a thermodynamic approach, relationships between grain direction strain and other factors, with temperature fluctuations being one of the primary contributors. Thermal expansion and contraction, arising from temperature changes, can induce strains, adversely affecting the integrity and stability of these wooden structures.

To detail the respective calculations:

The constraint at the beam ends produces reactive forces that resist strains induced by temperature variations. The magnitude of this reactive force depends on the length of the beam, its stiffness, and the deformation restrained by the beam end is \( \sigma_E \). The counteractive force provided by the tension spring at the beam end is represented by \( O \). The equations describe the equilibrium of deformation at the beam ends:

\[
\sigma_Y - \sigma_E = \sigma_I \quad (1)
\]

\[
\beta \Delta Y m - \frac{O m}{RS} = \frac{O}{J_a} \quad (2)
\]

Considering that both ends of the beam are usually fixed, these ends produce reactive forces that resist strains induced by temperature variations. The magnitude of this reactive force depends on the length of the beam, its stiffness, and the longitudinal elasticity of the wood. Stiffness of the beam describes its resistance to deformation when subjected to external influences, such as loads or temperature fluctuations. Longitudinal elasticity of the wood, on the other hand, quantifies the extent of deformation the wood undergoes when subjected to external stresses. Assuming the end reactive force is represented by \( O \) and strain by \( \Delta \gamma_1 \), the following equations detail the respective calculations:

\[
O = \frac{\beta \Delta Y m R}{S + \frac{RS}{J_a}} \quad (3)
\]

\[
\Delta \gamma_1 = \frac{O}{J_a m} = \frac{\alpha \Delta Y}{\frac{m J_a}{SR} + 1} \quad (4)
\]
Wooden beam connections in ancient structures are typically characterized as semi-rigid, rather than being fully rigid or simply hinged. This semi-rigidity introduces second-order bending moments into the beams, which in turn affect the overall structural stability and bending strain. The derivation of the additional strain $\Delta \gamma_2$, caused by the second-order bending effect from the beam end to its bottom, is outlined below.

$$m_b = m_0 + \frac{3}{4} m_b$$  \hspace{1cm} (5)

The calculated span of the beam is determined not solely by its actual length but also influenced by the stiffness of the end connections. The semi-rigid connection means that the actual calculated span of the beam might exceed its physical length, given that the flexibility of the connection increases the effective length of the beam. Figure 3 illustrates the principle behind the calculated span of ancient wooden beams. Assuming the arc wooden length is represented by $m_b$ and the clear span of the beam by $m_0$, the following expression gives the calculation for the span of the beam:

The calculated span of the beam $L_{MAX} = L_0 + O_{MAX} = L_0 \left(1 - \frac{1}{O_{ve}}\right) = L_0 S_t$  \hspace{1cm} (9)

Assuming the calculation length coefficient for the semi-rigid axial compression component is represented by $\omega$, the critical load $O_{ve}$ for the beam can be calculated using the formula:

$$O_{ve} = \frac{\tau^2 R_U}{(\omega m)^2}$$  \hspace{1cm} (10)

Considering the geometric imperfections of the beam and the effects of semi-rigid connections, the actual bending moment at the mid-span of the beam will usually exceed the bending moment based on linear-elastic analysis. This is referred to as the second-order bending moment, leading to an increase in the actual strain and deformation of the beam. Based on $\omega$, the moment amplification factor $S_t$ can be derived. The equation below represents the second-order bending moment at the mid-span of a wooden structure under rising temperature conditions:

$$\Delta L = (S_t - 1) L_0$$  \hspace{1cm} (11)

With all the aforementioned parameters and considerations, the additional strain caused by the second-order bending effect can be estimated. This additional strain is combined with the beam's original strain to determine the overall strain. Assuming the cross-sectional height of the beam is denoted by $g$, the formula below provides the calculation for the additional strain caused by the second-order bending:

$$\Delta \gamma = \frac{\Delta L g}{2RU} = \frac{L_0 O g}{2RU(O_{ve} - O)}$$  \hspace{1cm} (12)

The formula below provides the calculation for the strain in the grain direction at the mid-span of a wooden structure when the temperature increment is $\Delta T$:

$$\Delta e = \Delta e_1 + \Delta e_2 = \frac{O}{J_{sm} m_b} + \frac{L_0 O g}{2RU(O_{ve} - O)}$$  \hspace{1cm} (13)

For ancient wooden structures, cyclic temperature effects can lead to thermal expansion and contraction, resulting in strain. This cyclic process can be divided into four key stages. First, initial rise phase. From the starting state, the temperature begins to rise, causing the wooden structure to experience thermal expansion. Due to this temperature increase, thermal expansion commences, causing the strain in the grain direction to rise from its initial value. In this phase, strain is positively
correlated with the temperature increment. Second, high-temperature stability phase. The temperature reaches its peak and remains relatively stable for a period. Consequently, the strain in the wooden structure also reaches its maximum. During this phase, since the temperature remains mostly constant, the strain in the wooden structure is relatively stable. Third, cooling phase. The temperature begins to drop from its peak, returning to a state similar to the starting conditions. Owing to this decrease, the wooden structure starts to contract, leading to a reduction in strain from its maximum value. During this phase, the strain is negatively correlated with the decrease in temperature. Finally, low-temperature stability phase. The temperature returns to its initial state and remains relatively stable during this phase. The strain in the wooden structure also returns to its initial state. With the temperature maintaining a low, stable condition, the strain within the wooden structure remains relatively consistent.

3. OPTIMISATION OF WOODEN STRUCTURE PERFORMANCE PARAMETERS

The influence of temperature on wooden structures cannot be overlooked. Such influence prompts expansion or contraction in the wood, thereby altering its internal stress and strain distribution. Through thermodynamic analysis, a deeper understanding of the specific impact of temperature variations on the performance of wooden structures has been achieved, providing a theoretical foundation for subsequent performance parameter optimisation. Not only can optimisation of these performance parameters enhance the stability of wooden structures, but it can also ensure their long-term safe use. Given the precious nature of ancient wooden architectural structures, this is of particular significance.

The design of the CSO aims to find the global optimal solution rather than getting trapped in local optima. This characteristic is essential in the complex problem of wooden structure performance parameter optimisation. The goal is to identify the best combination of parameters to ensure the performance and stability of the wooden structure. The CSO, endowed with significant adaptability, can handle a variety of performance parameters, adapting to different wooden structure characteristics and requirements. Detailed elaboration on the design steps of the algorithm follows.

Initial positions for several roosters are chosen randomly, representing different combinations of wooden structure performance parameters. Based on the performance model of the wooden structure, a fitness value is assigned to each rooster. This value indicates the superiority of that parameter combination. The position of the rooster with the highest fitness value is updated to improve the overall stability of wooden structures. Following this, the position update mechanism for the chick's solution, which facilitates the inheritance of fitness. Let the position of the mother hen of the \( u \)-th chick during the \( y \)-th iteration be denoted by \( z_{u,k}(y) \), and the following coefficient by \( DM \). The update mechanism for the chick's position is expressed as:

\[
\delta^2 = \begin{cases} 
1, d_u < d_j \\
\exp \left( \frac{d_j - d_u}{d_u + \gamma} \right), d_u > d_j \in [1, B_j], j \neq u 
\end{cases}
\]

Similarly, the position of the hen is chosen at random. Using the same approach as the rooster, a fitness value is allocated to each hen. Hens primarily conduct local searches, selecting a relatively small neighbourhood range to explore areas near the current optimal position in search of superior solutions. If the identifier of the rooster in the sub-group where the \( u \)-th hen is located is \( e_1 \), and the identifier of a randomly selected rooster or hen is \( e_2 \) (with \( e_1 \neq e_2 \)), and a random number within the range \([0,1]\) is represented by \( rand \), then the position update mechanism for the hen is provided by:

\[
z_{u,k}(y+1) = z_{u,k}(y) + A_1 \ast rand \\
+ A_2 \ast rand \ast (z_{e_1,k}(y) - z_{u,k}(y))
\]

\[
A_1 = \exp \left( \frac{d_u - d_{e_1}}{d_u + \gamma} \right)
\]

\[
A_2 = \exp(d_{e_2} - d_u)
\]

The positions of chicks are determined based on the locations of their corresponding hens; they conduct searches around their hens. If a chick identifies a solution superior to that of its hen, the hen updates its position, thereby adopting the chick's solution, which facilitates the inheritance of fitness. Let the position of the mother hen of the \( u \)-th chick during the \( y \)-th iteration be denoted by \( z_{i,j}(y) \), and the following coefficient by \( DM \). The update mechanism for the chick's position is expressed as:

\[
z_{u,k}(y+1) = z_{u,k}(y) + DM \ast (z_{i,j}(y) - z_{u,k}(y))
\]

The core objective elucidated in this study revolves around the application of the CSO to optimise the performance parameters of wooden structures, drawing insights from thermal analysis and prediction outcomes of ancient wooden architecture. This constitutes a multistage, structured process. Initially, a thermodynamic analysis of ancient wooden architecture was performed to grasp the reactions and alterations of wood under diverse temperature conditions. This involved studying the expansion and contraction behaviours of wood at varying temperatures and the consequent implications for the overall stability of wooden structures. Following this analysis, an optimisation problem concerning wooden structure performance parameters was formulated. Though potentially high-dimensional, involving numerous performance parameters, this problem was transformed into a bidimensional minimisation task, thereby effectively curtailing computational complexity and bolstering optimisation efficiency. The CSO was selected as the preferred optimisation tool, given its aptitude for global optimum search, especially well-suited for intricate optimisation problems. Employing the CSO, the solution space was systematically
navigated. In each iteration, relying on the position update rules for roosters, hens, and chicks, the solution was continuously adjusted to approximate the optimum. Once optimal parameters for timber structure performance are identified, they are applied to actual models of ancient wooden structures to validate their real-world efficacy.

For the optimisation of wooden structure performance parameters, pertinent design variables and optimisation objectives were determined. Physical property variables encompassed wood density, elastic modulus of the wood, tensile strength, compressive strength, and shear strength of the wood. Structural dimension variables included maximum and minimum sizes of beams, columns, and other structural elements, as well as designs of nodes or joints. Finally, technological variables covered wood dryness and manufacturing techniques. These variables are direct influencers of wooden structure performance and are adjustable within certain bounds.

Subsequently, the objective function for wooden structure performance optimisation is established. This step is pivotal as it delineates the goals to be achieved during the optimisation process. Within the ambit of wooden structure performance enhancement, the objective function ought to encapsulate key performance indicators of the wooden structure, tailored based on actual requirements and project objectives.

In terms of stability, since a structure's stability under various loads and environmental conditions is a fundamental performance indicator, an objective function was defined with the aim to maximise the stability of the wooden structure under specified conditions, or to ensure stability remains above a particular safety threshold. For durability considerations, given wood's vulnerability to environmental factors such as humidity, temperature, and biological attacks, another objective function was designed aiming to maximise the expected lifespan of the wooden structure or to minimise the frequency and cost of maintenance and repairs. In terms of stiffness and strength, which are pivotal parameters dictating deformation and failure of wooden structures under load, an objective function was conceptualised with the intent to maximise structural stiffness and/or strength, ensuring the structure can endure anticipated loads without excessive deformation or damage. Recognising the limited and sustainable nature of wood resources, an objective function was introduced to minimise the amount or volume of required wood while meeting other performance benchmarks.

Thus, the objective function might be represented as:

\[ f(x) = \alpha_1 \times \text{stability index}(x) + \alpha_2 \times \text{durability index}(x) + \alpha_3 \times \text{rigidity index}(x) + \alpha_4 \times \text{material utilisation index}(x) \]

(20)

where, \( x \) denotes the design variables and \( \alpha_i \) signifies the weights associated with each index, adjustable based on specific project requirements.

4. EXPERIMENTAL RESULTS AND ANALYSIS

An in-depth investigation was conducted into the relationship between strain along the grain direction of ancient wooden beams and temperature. A comprehensive thermodynamic model was established, providing a robust theoretical foundation for predicting the performance of wooden structures under various environmental conditions. Examination of the aforementioned Figure 4 reveals a specific pattern of strain variation over time in the grain direction of the ancient wooden beam. Between time intervals 0 and 8, the strain of the wooden beam remained relatively stable, with only minor fluctuations. This stability is possibly attributed to negligible impacts from temperature and other external factors during this period. A pronounced increase in strain is observed between time units 8 and 9, indicating a significant change. This sudden increase might have been caused by sudden external influences such as a sharp rise in temperature, a sudden change in humidity, or an increased external load. Following this abrupt increase, the strain gradually stabilised and maintained a consistent growth trend in the subsequent timeframe. It is indicated that at this stage, although external conditions continue to change, the impact on the wooden beam remains relatively stable, with no apparent abrupt changes observed. It can be inferred that the strain in ancient wooden beams is closely related to temperature and other environmental factors. For the majority of the time, the strain remains relatively stable under consistent external conditions. However, abrupt environmental changes, such as sharp temperature rises or humidity shifts, can cause sudden strain variations, potentially posing risks to the wooden structure. Monitoring and preventative measures are essential.

**Figure 4. Strain increment diagram of unconstrained ancient wooden beam during loading**

The strain increments in ancient wooden beams, as depicted in the previous Figure 5, were analysed. Between 20:00 and 8:00, regardless of whether under "unconstrained" or "constrained" conditions, a declining trend in strain increment was observed. The decline was more pronounced under "constrained" conditions. By 8:00, the strain increments under both conditions approached their lowest points. From 8:00 to 20:00, under "unconstrained" conditions, the strain increment began to rise gradually in the morning until around 16:00, after which a slight decrease was observed. Conversely, under "constrained" conditions, a more evident growth trend was observed from the morning until about 16:00, after which a decline commenced. By 20:00, the strain increment under "constrained" conditions remained higher than that under "unconstrained" conditions. Throughout the observation period, the variation in strain increment under "constrained" conditions was greater than that under "unconstrained" conditions. This greater variation might be attributed to the increased external influences imposed by the constraints. It is evident that the strain increment in ancient wooden beams correlates with time and external environmental factors such as temperature. Regular monitoring of these beams, taking into
account actual constraint conditions, is essential to ensure their safety and stability.

![Graph](image1.png)

1) Night

![Graph](image2.png)

2) Day

**Figure 5.** Comparative analysis of strain increment in ancient wooden beams under different constraint conditions

![Graph](image3.png)

**Figure 6.** Long-term strain increment ratio of ancient wooden beams under different temperature environments

As shown in Figure 6, Based on the depicted long-term strain increment ratios in ancient wooden beams and the prior discussion, further analysis was conducted. Both datasets showed a dispersed trend with increasing temperature, yet most data points congregated around their respective average lines. Data points for the warming phase primarily clustered around an average value of 2.16. Despite a few outliers, the majority of the data points fell within the 2.0 to 2.3 range, suggesting minimal variation in the strain increment ratio during warming. For the cooling phase, data points predominantly clustered around an average of 1.75, notably lower than the warming phase's average. Most of these data points fall within the 1.7 to 2.0 range.

![Graph](image4.png)

1) Temperature increment

![Graph](image5.png)

2) Strain increment

**Figure 7.** Comparison of temperature and strain increments under various loads with tenon constraints in ancient wooden beams

As shown in Figure 7, several conclusions can be drawn concerning the temperature and strain increments in ancient wooden beams under various load conditions with tenon constraints. In all observed scenarios, the temperature increment displayed a similar pattern: initially declining with time, reaching a nadir at dawn, and subsequently ascending. This pattern persisted regardless of the applied load, although slight differences were observed between individual loading conditions. As for the strain increment, it paralleled the trend of temperature increment, first declining to its lowest point, then gradually rising. Wooden beams without tenon constraints demonstrated relatively minor fluctuations in strain increment, whereas those with tenon constraints exhibited more significant variations. This might be attributed to the constraints restricting the freedom of movement in the beams, rendering them more susceptible to temperature variations. Under differing load conditions, the strain increment pattern remained roughly analogous, though the magnitude of fluctuations differed. Thus, a correlation can be discerned between temperature and strain increments in ancient wooden beams under various loads with tenon constraints. The constraints on the tenon heightened the beam's sensitivity to temperature variations, with the magnitude of the applied load further influencing this sensitivity. The strain increment in the wooden beams also changed in response to temperature variations, a trend more pronounced when tenon constraints were applied.
Observations from Figure 8 indicate trends in the elastic modulus and rotational stiffness in ancient wooden beams under tenon constraints. Both the elastic modulus and rotational stiffness displayed analogous tendencies: from 20:00 in the evening until 16:00 the next day, both metrics surged before swiftly descending. The peak values for both the elastic modulus and rotational stiffness were reached around noon, suggesting external factors during this period, such as temperature and humidity, might exert the most substantial impact on the beam's properties. It can be concluded that, under tenon constraints, both the elastic modulus and rotational stiffness of the ancient wooden beams were influenced by external environmental factors, particularly during the midday hours. While both demonstrated similar trends, the absolute change in the elastic modulus exceeded that of the rotational stiffness. For the maintenance and preservation of ancient structures, the midday period merits special attention as the beam's performance might be most significantly affected at this time.

Based on Figure 9, a comparative analysis of the rise in stability and durability indices in ancient wooden beams under diverse conditions can be undertaken. In the graph depicting "rise in stability", the stability index exhibited fluctuations; in certain conditions, there was a marked enhancement in stability, while in others, a slight decline was evident. An average stability value of 8.49 was established, serving as a benchmark for evaluating stability across various conditions. In the "rise in durability" graph, durability too displayed a fluctuating trend with an average durability index of 4.431. It can be inferred that, within the considered conditions, both the stability and durability indices of ancient wooden beams experienced an upward shift, indicative of optimised performance parameters.

5. CONCLUSION

In-depth research was conducted into the relationship between strain in the longitudinal direction of ancient wooden beams and temperature, leading to the construction of a comprehensive theoretical thermodynamics model. Additionally, to further optimise the performance parameters of wooden structures, the CSO, mimicking the foraging behaviour of flocks of chickens to identify optimal solutions, was incorporated. From the analyses presented, pronounced strain variances in ancient wooden beams under varying temperature conditions were evident. A certain correlation between these strain disparities and temperature variations offers potential for predicting performance changes in wooden structures under various environmental conditions. In the longitudinal direction, the relationship between strain and temperature was rigorously investigated, culminating in the development of a theoretical thermodynamics model that provides significant theoretical backing for subsequent experiments. The integration of the CSO to identify the optimal solution, by emulating chicken foraging behaviour, offers a novel method for enhancing the performance parameters of wooden structures. The provided figures indicate improvements in stability and durability indices of ancient wooden beams under diverse operational conditions, further attesting to the efficacy of the CSO in wooden structure performance optimisation.

In summary, the strain properties of ancient wooden beams under varying temperatures were successfully investigated, and a corresponding theoretical model was established. Moreover, with the incorporation of the CSO, effective optimisation of wooden structure performance parameters was achieved. These findings offer pivotal insights for the preservation and restoration of ancient wooden architectural structures and carry significant implications for the design and application of modern wooden structures.
REFERENCES


