Energy and exergy analysis of flat plate solar collector for three working fluids, under the same conditions

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ABSTRACT

The growth and expansion of the population, has caused increased the use of energy in the last few years. One of the cleanest and renewable sources of the energy is the solar energy. The solar energy can be collected by solar collectors. One of the solar collectors is the flat plate solar collector (FPC), that it is used in domestic utilization.

Use of various Nano-fluids to improve the thermal properties of solar collectors, considered as one of the most effective method to optimize the flat plate collectors. In this study, a FPC in terms of energy and exergy, for three fluids (water, air and TiO₂ Nano-fluid) have been investigated. According to the results obtained and under the same conditions, destruction exergy of water is more than other two fluids and TiO₂ Nano-fluid has the least amount of destruction exergy. Also, by increasing in the total radiation on tilted surface (GT) TiO₂ Nano-fluid’s exergy efficiency is more than the other fluids in this study. By increasing ambient temperature, the exergy efficiency decreases, that water has the most variation.

Due to the temperature range of the inlet working fluid to the collector’s tubes, observed that outlet temperature of the TiO₂ Nano-fluid is about 50°C higher than when water enters it. Therefore, the initial statement about Nano-fluids is confirmed. In appropriate conditions, the collector’s efficiency is between 45% - 50%, thus FPC is one of the best devices for domestic utilization.

1. INTRODUCTION

Solar energy is one of the clean and renewable energy that is gratis. Therefore, using it will save wealth and end the dangers of emissions from fossil fuels.

For various purposes, in this regard different collectors designed and built. One of them is flat plate solar collector that it is stationary and its concentration rate is one. It is commonly used in residential buildings.

In domestic utilization based on solar energy systems, the flat plate solar collector is the system’s main part. FPC is a heat exchanger that, receives solar energy and then gives it to the working fluid that flows inside its tubes. By doing this, it will increase working fluid’s energy at FPC’s outlet. The effort is that the outlet fluid has a lot of energy. Therefore, a lot of scientific work has been done to investigate the FPC. These studies, aimed at understanding the factors affecting the performance of FPC, in order to build high quality collectors. So, energy and exergy analysis for FPC is very important.

In refs. [1-6] energy and exergy analysis methods, for flat plate solar collectors, such as energy and exergy efficiency, destruction exergy, working fluid’s outlet status are elaborated.


Geng Liu et al. [8] suggested a methodology for calculating the delivered and destruction exergy by the operation of a solar heating system. He showed that, radiation and convection heat transfer inside the solar collector and conversion of solar energy to thermal energy, extremely effective on destruction exergy.


S.Farahat et al. [11-12] did enerygetic optimization of flat plate solar collectors based on water working fluid, and showed the factors affecting the exergy efficiency such as design parameters, ambient and working fluid’s inlet temperature, total solar radiation and etc.

Farzad Jafarkazemi, Emad Ahmadifard [15] discussed about energy and exergy evaluation of flat plate solar collectors and showed that designing the FPC’s system, is which inlet water temperature is approximately 40°C more than the ambient temperature as well as a lower flow rate will enhance the system’s total performance.

Also, from different Nano-fluids used in the FPC [19-21] and then calculated its performance, many studies [17-21] have been done to determine Nano-fluid’s properties.

In the previous researches, provided exact equation for energy and exergy calculations. Given the importance of using solar collectors, and increasing demand in this case, energy and exergy analysis of these systems are very importance. Therefore, in this paper from three different fluids which are water, air and TiO₂ Nano-fluid, under the same conditions, will be used as the working fluid entering the collector. Also, energy and exergy of FPC will be compared in all three cases.
2. MODELING

2.1. Energy analysis

Collector’s energy analysis, in order to attain the amount of heat it receives, obtained its efficiency and working fluids outlet temperature is very important.

For this purpose, the climatic conditions of the place where the collector (such as solar radiation received, solar radiation angle, Sunset angle, latitude angle and etc.) is installed must be available.

By knowing the amount of monthly average solar radiation received on the horizontal surface of the earth, monthly average diffuse radiation calculated from the equation 1 [10]:

\[
\bar{H}_d = \bar{H}_b(1 - 1.13K_t)
\]  
(1)

\(\bar{H}_d\) is monthly average diffuse radiation, \(\bar{H}_b\) is monthly average radiation received on the horizontal surface of the ground, \(K_t\) is monthly average clearness index.

To obtain the amount of monthly average absorbed solar radiation by FPC, (2-14) steps are followed.

At first, according to the incident beam angle and FPC glass, refracted beam angle can be calculated from the equation 2 [22-23]:

\[n_1 \sin \alpha_i = n_2 \sin \theta\]

(2)

\(n_1\) and \(n_2\) are refracted index for air and glass respectively, \(\alpha_i\) is incident beam angle and \(\theta\) is refracted beam angle.

Transmittance absorption losses factor is [22-23]:

\[
\tau_\alpha = \exp\left(-\frac{KL}{\cos \theta}\right)
\]

(3)

\(KL\) is absorbed solar radiation rate for glass

Then transmittance refraction losses factor is [22-23]:

\[
\tau_r = \frac{1}{2} \left(1 - \frac{r_{\perp}}{1 + r_{\perp}} + 1 - \frac{r_{\parallel}}{1 + r_{\parallel}}\right)
\]

(4)

In this equation \(r_{\parallel}\) and \(r_{\perp}\) are parallel and perpendicular component of unpolarized radiation respectively and can be calculated from equations 5 and 6 [22-23]:

\[
r_{\parallel} = \frac{\tan^2(\theta - \alpha)}{\tan^2(\theta + \alpha)}
\]

(5)

\[
r_{\perp} = \frac{\sin^2(\theta - \alpha)}{\sin^2(\theta + \alpha)}
\]

(6)

Therefore, transmittance factor for glass is [22-23]:

\[
\tau = \tau_\alpha \times \tau_r
\]

(7)

At this step, absorptance factor can be found from the properties of the absorber, which is [22-23]:

\[
\alpha_\alpha = 1 + 2.0345 \times 10^{-3} \alpha - 1.99 \times 10^{-4} \alpha^2 + 5.324 \times 10^{-6} \alpha^3 - 4.799 \times 10^{-8} \alpha^4
\]

\(\alpha_\alpha\) is absorptance factor at normal incident can be found from the properties of the absorber.

The amount of effective product transmittance – absorptance that finally absorbs the absorber is [22]:

\[
(\tau \alpha)_b = (1.01 \tau)\alpha_b
\]

(9)

For given collector tilted angle (\(\beta\)), the effective incidence angle for diffuse radiation from sky and effective incidence angle for ground reflected radiation, can be calculated from equations 10 and 11 respectively [22-23]:

\[
\theta_{e,D} = 59.68 - 0.1388\beta + 0.001497\beta^2
\]

(10)

\[
\theta_{e,G} = 90 - 0.5788\beta + 0.00269\beta^2
\]

(11)

By placing \(\theta_{e,D}\) and \(\theta_{e,G}\) in the equation 2 and solving equations number 2 to 9, the effective product transmittance – absorptance that finally will be diffused and the effective product transmittance – absorptance that finally reflected from the ground can be calculated from equations 12 and 13 respectively [22-23]:

\[
(\tau \alpha)_D = (1.01 \tau)\alpha_D
\]

(12)

\[
(\tau \alpha)_G = (1.01 \tau)\alpha_G
\]

(13)

Table 1. Flat plate solar collector features

<table>
<thead>
<tr>
<th>sign</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\alpha_c)</td>
<td>2 (m²)</td>
</tr>
<tr>
<td>(\alpha_s)</td>
<td>0.91</td>
</tr>
<tr>
<td>(\alpha_i)</td>
<td>20 (degree)</td>
</tr>
<tr>
<td>(\beta)</td>
<td>30 (degree)</td>
</tr>
<tr>
<td>(D_i)</td>
<td>0.012 (m)</td>
</tr>
<tr>
<td>(D)</td>
<td>0.014 (m)</td>
</tr>
<tr>
<td>(\varepsilon_P)</td>
<td>0.9</td>
</tr>
<tr>
<td>(\varepsilon_g)</td>
<td>0.88</td>
</tr>
<tr>
<td>(\delta_g)</td>
<td>0.004</td>
</tr>
<tr>
<td>(\delta_c)</td>
<td>0.04</td>
</tr>
<tr>
<td>(\delta)</td>
<td>0.005</td>
</tr>
<tr>
<td>(h_0)</td>
<td>320 (W/m².K)</td>
</tr>
<tr>
<td>(K_P)</td>
<td>0.05 (W/m.K)</td>
</tr>
<tr>
<td>(K_s)</td>
<td>385 (W/m.C)</td>
</tr>
<tr>
<td>(KL)</td>
<td>0.04</td>
</tr>
<tr>
<td>(L_w)</td>
<td>2 (m)</td>
</tr>
<tr>
<td>(m)</td>
<td>0.01 (Kg/s)</td>
</tr>
<tr>
<td>(N_f)</td>
<td>1</td>
</tr>
<tr>
<td>(N_T)</td>
<td>7</td>
</tr>
<tr>
<td>(n_1)</td>
<td>1</td>
</tr>
<tr>
<td>(n_2)</td>
<td>1.526</td>
</tr>
<tr>
<td>(P_i)</td>
<td>100 (Kpas)</td>
</tr>
<tr>
<td>(T_a)</td>
<td>280 (K)</td>
</tr>
<tr>
<td>(T_P)</td>
<td>340 (K)</td>
</tr>
<tr>
<td>(T_i)</td>
<td>298.15</td>
</tr>
<tr>
<td>(W_i)</td>
<td>0.12 (m)</td>
</tr>
<tr>
<td>(V)</td>
<td>10 (m/s)</td>
</tr>
<tr>
<td>(V_c)</td>
<td>1 (m/s)</td>
</tr>
</tbody>
</table>

Therefore, monthly average absorbed solar radiation by FPC is [22-23]:

\[
\bar{S} = \bar{H}_b R_b (\tau \alpha)_b + (\tau \alpha)_D \left(\frac{1 + \cos \beta}{2}\right) \bar{H}_d + \rho_G (\tau \alpha)_G \left(\frac{1 - \cos \beta}{2}\right) (\bar{H}_b + \bar{H}_d)
\]

(14)

\(R_b\) is monthly beam radiation tilt factor, \(\rho_G\) is ground reflectance factor.

Monthly average total solar radiation is [22-23]:
\[ T_t = \frac{8}{(\tau \alpha)_{ave}} \]  

\( (\tau \alpha)_{ave} \) is average effective product transmittance – absorptance and can be calculated from equation [16] [22-23]:

\[ (\tau \alpha)_{ave} = 0.96 \ (\tau \alpha)_b \]  

By calculated overall heat loss coefficient, the rate of useful energy collected from FPC and FPC’s efficiency obtained. Overall heat loss coefficient, include three terms:

1. top loss coefficient [15]:

\[ U_t = \frac{1}{\frac{h_w}{C_p} + \frac{1}{U_p} + \frac{1}{h_p} \frac{1}{C_p}} \]  

\( h_w \) is number of glass cover, \( T_p \) is mean absorber temperature, \( T_a \) is ambient air temperature, \( h_w \) is wind convection heat loss coefficient, \( C \) and \( f \) are constant parameters [15].

\[ h_w = \frac{0.65V^{0.6}}{L^{0.4}} \]  

\( C = 365.9(1 - 0.00883\beta + 0.0001298\beta^2) \)

\( f = (1 - 0.04h_w + 0.0005h_w^2)(1 + 0.091N_g) \)

2. bottom heat loss coefficient [22]:

\[ U_b = \frac{1}{\frac{1}{U_b} + \frac{1}{h_b}} \]  

\( t_b \) is thickness of back insulation, \( h_{cb-a} \) is convection heat loss coefficient from back to ambient, \( K_b \) is conductivity of back insulation.

3. heat loss coefficient from the collector edge [22]:

\[ U_e = \frac{1}{\frac{1}{K_b} + \frac{1}{h_{ce-a}}} \]  

\( t_e \) is thickness of edge insulation, \( h_{ce-a} \) is convection heat loss coefficient from edge to ambient, \( K_e \) is conductivity of edge insulation.

Therefore, overall heat loss coefficient is [11-12]:

\[ U_t = U_t + U_c + U_b \]  

The useful heat gain by the working fluid is [1]:

\[ Q_a = \dot{m}C_p(T_{out} - T_{in}) \]

\( \dot{m} \) is working fluid mass rate, \( C_p \) is heat capacity, \( T_{out} \) and \( T_{in} \) are outlet and inlet temperature respectively.

The useful heat gain of FPC system, considering the heat losses from the FPC to the atmosphere, is [11,22]:

\[ Q_a = A_c [G_t(\tau \alpha) - U_L(T_p - T_a)] \]

\( A_c \) is collector area, \( G_t \) is total solar radiation.

Collector’s performance, collector efficiency and collector efficiency factor calculated from equations 27 and 28 [11]:

\[ \eta = \frac{Q_a}{A_c \cdot \dot{m}} \times 100 \]  

\[ F_C = \frac{1}{W_l} \left[ \frac{1}{U_b} + \frac{1}{h_w} \right] \]  

\( W_l \) is tubes spacing, \( D \) is tube outside diameter, \( D_t \) is tube inside diameter, \( h_l \) is heat transfer coefficient inside of the tube, \( \eta \) is fin efficiency, \( C_b \) is bond conductance.

Fin efficiency is [22-23]:

\[ F_l = \frac{\tanh(X(W_l - D))}{X(W_l - D)} \]

\( X \) is a constant parameter and equal to [22-23]:

\[ X = \frac{U_l}{K_b \beta} \]

\( K_b \) is bond thermal conductivity, \( b \) is bond width, \( \gamma \) is bond thickness.

Plate’s material is copper. \( K \) is plate heat transfer coefficient, \( \delta_t \) is plate thickness.

Bond conductance can be calculated from equation 31 [22-23]:

\[ C_b = \frac{K_b b}{\gamma} \]

\( K_b \) is bond thermal conductivity, \( \delta_t \) is plate thickness.

The fluid outlet temperature has a very important role in collector systems. In FPC it is equal to [9]:

\[ T_{out} = T_{in} + \frac{1}{U_l} \left( \frac{S_{dw}}{U_l} - T_a(T_r - T_a) \right) \]  

\[ \frac{1}{1 - \exp \left( -A_c \frac{U_l - F_C}{m \cdot C_p} \right)} \]

\( S_{dw} \) is average absorbed solar radiation in (W/m²) [22]

\[ \bar{S}_{dw} = \frac{G_t}{(\tau \alpha)_{ave}} \]

2.2 Exergy analysis

Exergy analysis is a method that use the second law of thermodynamics for the analysis, design and improvement of energy. Exergy is defined as the maximum amount of power which can be produced by a system and has an important role in thermodynamic analysis.

Exergy analysis for a control volume can be calculated from equation 34 [24]:

\[ \frac{dEXcv}{dt} = \sum \left( 1 - \frac{T_0}{T} \right) \dot{Q}_j - \left( W_{cv} - P_0 \frac{dV_{cv}}{dt} \right) + \sum \dot{m}_t EX_i - \sum \dot{m}_e EX_e - EX_d \]  

When FPC system is in a steady state, exergy balance is [2,14]:

\[ EX_{in} - EX_{out} - EX_L - EX_d = 0 \]

1.inlet exergy:
Exergy flows into a system includes two terms, inlet exergy with mass flow and inlet exergy with solar radiation absorbed by the collector.

a. Inlet exergy with mass flow is [2,11]:

\[
\dot{E}_{\text{in},f} = \dot{m}_f C_p \left( T_{\text{in}} - T_a - \left( T_a \ln \frac{T_{\text{in}}}{T_a} \right) \right) + \frac{\dot{m} \Delta P_{\text{in}}}{\rho}
\]  

(35)

\(\Delta P_{\text{in}}\) is the pressure difference of the working fluid with the surroundings at FPC’s inlet.

b. Inlet exergy with solar radiation absorbed by the collector is [4]:

\[
\dot{E}_{\text{in},q} = \eta_o G_t \cdot A_c \left( 1 - \frac{T_a}{T_s} \right)
\]  

(36)

\(T_s\) is Apparent solar temperature, \(\eta_o\) is optical efficiency and equal to [15,16]:

\[
\eta_o = \frac{5}{11} \ln \left( \frac{T_o}{T_f} \right)
\]  

(37)

Thus, inlet exergy is [2-3]:

\[
\dot{E}_{\text{in}} = \dot{E}_{\text{in},f} + \dot{E}_{\text{in},q}
\]  

(38)

2. Outlet exergy:
The outlet exergy includes only the outlet exergy with mass flow and equal to [2,7]:

\[
\dot{E}_{\text{out}} = \dot{m}_c C_p \left( T_{\text{out}} - T_a - \left( T_a \ln \frac{T_{\text{out}}}{T_a} \right) \right) + \frac{\dot{m} \Delta P_{\text{out}}}{\rho}
\]  

(39)

\(\Delta P_{\text{out}}\) is the pressure difference of the working fluid with the surroundings at FPC’s outlet.

3. Leakage exergy
Includes heat leakage from the absorber plate to the environment. The outlet exergy is the desired exergy and the exergy leakage equals the undesired exergy losses.

\[
\dot{E}_{L} = U_L \cdot A_c \left( T_p - T_s \right) \left( 1 - \frac{T_s}{T_p} \right)
\]  

(40)

4. Destruction exergy:
Destruction exergy includes three terms which is discussed below.

a. Destruction exergy due to pressure drop of inside the tube [2,26]:

\[
\dot{E}_{\text{d,}\Delta P} = \frac{\dot{m} \Delta P}{\rho} \left( \frac{T_{\text{in}} - \ln \frac{T_{\text{out}}}{T_{\text{in}}} - T_{\text{in}}}{\text{out}} \right)
\]  

(41)

\(\Delta P\) = p.g.(Lz.sin\(\beta\) + \(h_1\))

(42)

\(g\) is gravity acceleration, \(Lz\) is tube length, \(h_1\) is total pressure drop and equal to [26]:

\[
h_1 = \frac{g m^2}{\rho g p^2 \pi^2 D^2_1} \left( \frac{r^4}{4} + \sum_{i=1}^{n_t} K_L \right)
\]  

(43)

\(n_t\) is number of tube, KL is partial pressure drop coefficient of connections that in tube’s inlet equal to 1 and at outlet equal to 0.5, \(f\) is friction coefficient and obtained from equation 45 [25]:

\[
f = \begin{cases} 
\frac{64}{Re} & \text{for laminar flow} \\
0.079 \frac{Re^{0.25}}{Re^{0.25}} & \text{for turbulent flow}
\end{cases}
\]  

(44)

b. Destruction exergy due to solar temperature difference with absorber plate surface [2-3]:

\[
\dot{E}_{\text{d,}\Delta T_s} = \eta_o G_t \cdot A_p \cdot T_a \left( \frac{1}{T_p} - \frac{1}{T_a} \right)
\]  

(45)

c. Destruction exergy due to the temperature difference between absorber plate surface and working fluid that is [2,7]:

\[
\dot{E}_{\text{d,}\Delta T_f} = \dot{m} \cdot c_p \cdot T_a \left( \ln \frac{T_{\text{out}}}{T_{\text{in}}} - \frac{T_{\text{out}} - T_{\text{in}}}{T_p} \right)
\]  

(46)

Therefore, destruction exergy is [2,3,7]:

\[
\dot{E}_{\text{d}} = \dot{E}_{\text{d,}\Delta P} + \dot{E}_{\text{d,}\Delta T_s} + \dot{E}_{\text{d,}\Delta T_f}
\]  

(47)

By doing the balance of exergy, exergy efficiency to understand the FPC performance is defined, that is [11,15]:

\[
\eta_{\text{EX}} = \frac{\dot{m} \cdot c_p \left( T_{\text{out}} - T_{\text{in}} - \left( T_a \ln \frac{T_{\text{out}}}{T_a} \right) \right) \left( \frac{\Delta P}{\rho} \right)}{G_t \cdot A_p \cdot \left( 1 - \frac{T_s}{T_p} \right)}
\]  

(48)

\[
= 1 - \left( 1 - \eta_o \right) + \frac{\dot{m} \Delta P}{\rho G_t \left( 1 - \frac{T_s}{T_p} \right)} \left( T_{\text{out}} - T_{\text{in}} \right)
\]  

\[
\frac{\eta_o T_a}{\left( 1 - \frac{T_s}{T_p} \right) \left( \frac{1}{T_p} - \frac{1}{T_a} \right)} + \frac{\left( \frac{G_t}{G_t} - \frac{T_{\text{out}}}{T_{\text{in}}} \right)}{G_t \left( \frac{1}{T_p} \right)} \left( 1 - \frac{T_a}{T_p} \right)
\]  

\[
\left( \frac{m c_p T_a}{G_t A_c} \left( \ln \frac{T_{\text{out}}}{T_{\text{in}}} - \frac{T_{\text{out}} - T_{\text{in}}}{T_p} \right) \right)
\]  

3. THERMO-PHYSICAL CHARACTERISTICS OF THE NANO-FLUID

Nano-fluids are liquid suspensions of particles that one of their particles dimensions smaller than 100 nm. Nano-fluid that in this study is TiO₂ Nano-fluid, considered as powder that an average particle’s diameter is 15 nm, which adds to the base fluid (water) to improve its thermal properties.

Density of Nano-fluid is [19]:

\[
\rho_{\text{nf}} = \rho_{\text{wp}} + (1 - \varphi_v) \cdot \rho_{\text{bf}}
\]  

(49)

\(\varphi_v\) is volume concentrations, \(\rho_{\text{wp}}\) and \(\rho_{\text{bf}}\) are density of nano powder and base fluid (water) respectively.

Thermal capacity of Nano-fluid is [20]:

\[
\left( \rho \cdot C_p \right)_{\text{nf}} = \varphi_v \cdot \left( \rho \cdot C_p \right)_{\text{wp}} + (1 - \varphi_v) \cdot \left( \rho \cdot C_p \right)_{\text{bf}}
\]  

(50)

\(C_p\)_{\text{wp}} and \(C_p\)_{\text{bf}} are thermal capacity of nano powder and base fluid respectively.

And viscosity of Nano-fluid is [21]:

\[
\mu_{\text{nf}} = \mu_{\text{bf}} \left( 1 + 2.5 \varphi_v + 6.5 \varphi_v^2 \right)
\]  

(51)

<table>
<thead>
<tr>
<th>Nano powder</th>
<th>(\rho) (kg/m²)</th>
<th>(C_p) (J/kg.K)</th>
<th>(\varphi_v) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>TiO₂</td>
<td>997.1</td>
<td>4182</td>
<td>0.99</td>
</tr>
</tbody>
</table>
Table 3. Working fluids properties

<table>
<thead>
<tr>
<th>fluid</th>
<th>(\rho) (kg/m(^3))</th>
<th>(C_p) (kJ/kg.K)</th>
<th>(\mu) (Pa.s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>997.1</td>
<td>4182</td>
<td>890.5 (\times 10^{-6})</td>
</tr>
<tr>
<td>Air</td>
<td>1.72</td>
<td>1007</td>
<td>18.45 (\times 10^{-6})</td>
</tr>
</tbody>
</table>

4. RESULT AND DISCUSSION

In this study, for a flat plate solar collector that its features are defined, by using three fluids that are water, air and TiO\(_2\) Nano-fluid under the same condition energy and exergy equations are modeling and solving.

As it seen in table 4 the values obtained from energy analysis are reported:

Table 4. Energy analysis result for FPC

<table>
<thead>
<tr>
<th>parameter</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(H_b)</td>
<td>20 M/J/M(^2)</td>
</tr>
<tr>
<td>(H_d)</td>
<td>6.44 M/J/M(^2)</td>
</tr>
<tr>
<td>(\theta)</td>
<td>0.6</td>
</tr>
<tr>
<td>(\theta_0)</td>
<td>0.8052</td>
</tr>
<tr>
<td>(\theta_2)</td>
<td>0.7099</td>
</tr>
<tr>
<td>(\alpha)</td>
<td>0.402</td>
</tr>
<tr>
<td>(\alpha_{ave})</td>
<td>0.773</td>
</tr>
<tr>
<td>(\alpha_B)</td>
<td>0.9064</td>
</tr>
<tr>
<td>(\alpha_D)</td>
<td>0.8639</td>
</tr>
<tr>
<td>(\alpha_G)</td>
<td>0.6914</td>
</tr>
<tr>
<td>(\theta)</td>
<td>12.95 Degree</td>
</tr>
<tr>
<td>(\theta_{elD})</td>
<td>56.86 Degree</td>
</tr>
<tr>
<td>(\theta_{elG})</td>
<td>75.06 Degree</td>
</tr>
<tr>
<td>(S_t)</td>
<td>36.84 M/J/M(^2)</td>
</tr>
<tr>
<td>(G_t)</td>
<td>47.65 M/J/M</td>
</tr>
<tr>
<td>(U_l)</td>
<td>5.276 W/m(^2).K</td>
</tr>
<tr>
<td>(U_c)</td>
<td>3.076 W/m(^2).K</td>
</tr>
<tr>
<td>(U_b)</td>
<td>0.5 W/m(^2).K</td>
</tr>
<tr>
<td>(U_e)</td>
<td>1.6 W/m(^2).K</td>
</tr>
<tr>
<td>(h_w)</td>
<td>29.95 W/m(^2).K</td>
</tr>
<tr>
<td>(Q_w)</td>
<td>1018 W</td>
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<td>(S_w)</td>
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Figure 1. Effects of ambient temperature to FPC efficiency at variable total solar radiation.

As it seen in fig. 1, effect of ambient temperature is shown in the total solar radiation range between 500-1200 Watts. It can be interpreted that efficiency of FPC is directly related to ambient temperature So that, by increasing ambient temperature and total solar radiation FPC Efficiencies increases. Approximately FPC Efficiencies at an appropriate collector tilt angle and working fluid mass flow rate during the year is between 45% – 55% that is a suitable range.

As it seen in fig. 2, for working fluids that its inlet temperature is between 290 – 320 kelvins, outlet temperature is obtained. TiO\(_2\) Nano-fluid has the highest outlet temperature that its outlet temperature approximately (70-80)\(^\circ\)C higher than water and (30-40)\(^\circ\)C higher than air. therefore, Nano-fluids has the more ability than other working fluids.

Figure 2. Working fluids outlet temperature, based on their inlet temperature.

Figure 3. Exergy of water, based on total solar radiation.

In fig.3, fig.4 and fig.5 effect of total radiation on working fluids exergy, in range between 500-1200 (W/m\(^2\)) is discussed. According to the obtained diagrams, when total solar radiation is increasing, exergy increases. Destruction exergy is very affected from solar radiation when ambient temperature is constant. Inlet exergy of working fluids is very higher than outlet exergy.
As it seen in fig. 6, fig. 7 and fig. 8 effect of ambient temperature on working fluids exergy, in range between 274-310 kelvins is discussed.

As the ambient temperature increases, the inlet exergy decreases, which water has the most changes and TiO\textsubscript{2} Nano-fluids gives the slightest changes in these conditions.

Generally, the range of exergy changes for inlet exergy is between 1400-1500 watts, for outlet exergy is between 180-20 watts, for leakage exergy is between 180-20 watts. But destruction exergy increases and its changes is between 1200-1450 watts.

As it seen in fig. 9, destruction exergy of water, more than other two fluids.

Also, the destroyed exergy of the TiO\textsubscript{2} Nano-fluid has the lowest value. Therefore, the use of Nano-fluids is more efficient.

In fig. 10, exergy efficiency based on total solar radiation that is between 700-1200 (W/m\textsuperscript{2}) has been shown. By increasing total solar radiation, the exergy efficiency is rising for all three working fluids. However, the increase in total solar radiation has a great impact on exergy efficiency of TiO\textsubscript{2} Nano-fluid.

In fig. 12, the effect of the ambient temperature on the exergy efficiency of the working fluids is shown. By increasing ambient temperature, the exergy efficiency is decreased, that water has the most negative variations in
exergy efficiency under the same condition. In this state, TiO$_2$ Nano-fluid also has the highest exergy efficiency.

**Figure 9.** Compare destruction exergy of working fluids, based on total solar radiation

![Figure 9](image)

Gradually decreases the exergy efficiency.

In this state, the TiO$_2$ Nano-fluid is more susceptible to overall heat loss than the other two fluids.

**Figure 10.** Compare exergy efficiency of working fluids, based on total solar radiation

![Figure 10](image)

In fig. 13, the effect of exergy efficiency on the optical efficiency is shown. It is observed that the TiO$_2$ Nano-fluid is more sensitive than other two fluids.

**Figure 11.** Compare exergy efficiency of working fluids, based on ambient temperature

![Figure 11](image)

In fig. 12, The effect of increasing the overall heat loss coefficient on the exergy efficiency is shown. As it increases, the TiO$_2$ Nano-fluid is more susceptible to overall heat loss than the other two fluids.

**Figure 12.** Compare exergy efficiency of working fluids, based on overall heat loss coefficient

![Figure 12](image)

4. CONCLUSIONS

1. By increasing total solar radiation, the energy and exergy efficiency are increase. But when the ambient temperature rises, the exergy efficiency decreases.
2. The use of a Nano-fluid working fluid in FPC systems, will increase the temperature at the outlet of collector.
3. The working fluid in the collector entrance, has a large exergy. But in outlet of FPC, it encounters a huge drop in exergy.
4. Destruction exergy in the collector is very high, which results in a sharp drop in the collector's exergy efficiency.
5. The overall loss coefficient in FPC is not a constant parameter and it has a great impact on the exergy efficiency. Therefore, the exact calculation is important to get the exact answer.
6. Optical efficiency is a parameter that has a great impact on the exergy efficiency. By increasing optical efficiency, the
magnitude of exergy efficiency increases.
8. At all stages, the use of Nano-fluid showed that it improves the performance of the FPC.

REFERENCES


NOMENCLATURE

A collectors area (m²)
Cₐ bond conductance
Cₚ heat capacity of the fluid (kJ/kg K)
D diameter (m)
Eₓ exergy (W)
f friction coefficient
F efficiency factor
FPC flat plate collector
G total solar radiation (w/m²)
hₜ total pressure drop
h convection heat Transfer coefficient(w/K.m²)
H monthly average radiation
Iₚ monthly average total solar radiation (MJ/m²)
K conductivity (W/m K)
Kₐ monthly average clearness index
KL absorbed solar radiation rate for glass
L₁ tube length (m)
ṁ mass flow rate (kg/s)
N refraction index
P number
Q heat transfer (W)
S radiation absorbed by collector (MJ/m²)
Sₚ radiation absorbed by collector (W/m²)
T temperature (K)
U collector loss coefficient (W/m² K)
V speed, velocity (m/s)
Wᵣ fluid inlet velocity (m/s)
X constant parameter
### Greek symbols

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<tr>
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<td>incident beam angle (degree)</td>
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<tr>
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### Subscripts

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