Thermal performance of wavy finned absorber solar air heater

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ABSTRACT

This paper presents an experimental investigation on the thermal performance enhancement of solar air heater having wavy fins attached below the absorber plate. Tests were conducted to cover a wide range of parameters such as mass, velocity, fin spacing and insolation under actual outdoor conditions. The effect of these parameters on the thermal performance has been examined and the results have been compared with plane solar air heater. The maximum enhancement in thermal efficiency for wavy finned absorber solar air heater for fin spacing of 2 cm has been found to be 28.71% as compared to fin spacing of 6 cm and 116.67% as compared to plane solar air heater. The maximum value of ΔT/I for wavy fin spacing 2 cm, 6 cm and plane solar air heater has been achieved as 0.067, 0.048 and 0.029 m²·°C/W respectively. Wavy finned absorber solar air heater has been found to be 67.44 to 121.43% thermally efficient as compared to plane solar air heater within the investigated range of system i.e. fin spacing of 2 to 6 cm and operating parameters i.e. mass velocity of 0.0065 - 0.033 kg/s/m². A substantial enhancement in thermal efficiency was achieved in comparison to plane solar air heater and this improvement is a strong function of system and operating parameters.

1. INTRODUCTION

Solar energy is considered as an optimistic and green source of energy and also used for many industrial and domestic applications. In solar energy exerions, solar air heaters provide the moderate air temperatures and used for the drying of crops, space heating etc.[1]. The performance of plane solar air heater is found to be low due to the lower heat transfer coefficient between the absorber plate and the air flowing through the duct and thus leads to higher thermal losses to the ambient [2]. In order to improve the heat transfer rate in the solar air heater, fins, fins with baffles [3-5] artificial roughness [6-7] and packed beds [8-10] are introduced in the flow channel. Fins are the surfaces that extend from the absorber plate to enhance the heat transfer area, thus increases the heat transfer rate. Numerous research on heat transfer characteristics of fins such as plain, wavy, offset fins and louvered fins over the flat wall has been studied and a considerable augmentation in heat transfer takes place. Li et al. [11] studied the comparative performance for wavy fin and a plain fin with radially arranged winglets around each tube in fin and tube heat exchangers. Their results indicate that the heat transfer rate and pressure drop penalty of heat exchanger surfaces using wavy fin with five row tubes were almost same with six raw tubes wavy fin heat exchanger surfaces. Also, they developed the correlations for Nusselt number and friction factor. Optimised study of cross-cut flow control has been done by Gun et al. [12] for heat transfer enhancement in wavy fin heat exchangers by using concept of cross cut reference length (CRL). They found an optimal heat transfer when the cross-cut length was 0.4 CRL and in some cases optimum cross cut length was changed to 0.5 CRL by considering pressure drop. The flow and heat transfer characteristics for humped wavy fins with different humped radii and Reynolds number were studied numerically and experiments with different humped radii were performed the correlations for Nusselt number and heat conductance. Kumar and Chand [15] developed a mathematical model for herringbone corrugated fins to predict the effect of system, operating and meteorological parameters on the thermal and thermohydraulic performance of solar air heater. They found an improvement of 20.4% in thermal efficiency with the penalty of increased pressure drop at fin spacing 2.5 cm and mass flow rate of 0.026 kg/s. Priyam and Chand [16] studied the effect of mass flow rate and fin spacing on thermal and thermohydraulic performances of wavy finned absorber solar air heater. Their mathematical model predicted an enhancement of 62.53 - 63.41% in thermal efficiency and 29.39 - 29.43% in the effective temperature rise for the investigated mass flow range of 0.0138- 0.0834kg/s. In another study, the effect of the collector aspect ratio has been investigated on the thermal performances of wavy fin absorber solar air heater by Priyam and Chand [17]. They found that the
performance of wavy fin solar air heater improved with the increase in the collector aspect ratio. Analytical study on the wavy fin solar air heater was done by Priyam and Chand [18] to study the effect of wavelength and amplitude of wavy fin on thermal and thermodynamic performance. They found a grat enhancement in the thermal and thermodynamic performance with the wavy fin solar air heater and an optimal thermal efficiency as 73.2% has been found for the wavelength= 7 cm and mass flow rate of 0.061 kg/s.

It is evident from the literature that by providing wavy fins along the fluid flow increases the amount of heat transfer in the solar air heater but no experimental investigation has been done on the wavy fin solar air heater. In the present work, an experimental investigation has been carried out on the thermal performance of solar air heater with sinusoidal wavy fins below the absorber. The effects of mass velocity and the fin spacing on the thermal performance and rise in air temperature has been studied. Also, the variation of thermal efficiency as a function of $\Delta T/I$ for various fin spacing were examined. The obtained results are compared with results available in the literature.

2. MATERIALS AND METHODOLOGY

2.1 Experimental set up

The experimental set-up consists of a blower, wooden rectangular channel, G.I pipe, orifice meter, flow control valve, digital manometer, J-type thermocouples as shown in fig.1. The various system and operating parameters used in the analysis are listed in Table 1. The inner dimensions of the both rectangular channels were 1700 mm x 400 mm x 50 mm. The test section has a length of 1200mm and the flow straightener of 500 mm as per ASHRAE standards [19]. The side and the middle wall of the channel were of soft wood having thickness 25mm and 40mm. The bottom of the channels has a 22 gauge G.I sheet over a 50 mm of glass wool insulation supported by 10 mm plywood at the bottom. G.I sheet acts as an absorber in plane solar air heater, whereas, the wavy fins were attached below the absorber in the wavy finned absorber solar air heater. A total of five absorbers A1, A2, A3, A4 and A5 have been made with the fin spacing 2, 3, 4, 5 and 6 cm respectively. The spacing between the glass cover and the absorber plate is 50 mm. The fins as well as plate were blackened with blackboard paint. The area exposed is 0.48 m² for both the collectors. A total of 24 thermocouples was used, out of which 5 were used to measure the plate temperature of each collector and 7 each to measure air temperature inside the duct. The positions of thermocouples over the test section to measure air and plate temperature has been shown in fig.2. All thermocouples were connected to a data logger for digital display. A total of three data loggers (A,B,C) having 8-channels each has been used to record the temperature. The air mass flow rate flowing through duct was measured by using a calibrated orifice meter fitted with digital manometer. The calibration of orifice meter was done by fitting the orifice meter in series with the calibrated orifice plate with known coefficient of discharge. The outlet of the air heaters were connected to wooden convergent section coupled with G.I pipes, orifice meter, flow control valve and a 3 hp, 3-ph blower. The pictorial view of the experimental set-up is shown in fig.3. Insolation was recorded by a pyranometer as shown in fig.4 with digital output.

<table>
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<tr>
<th>Parameters</th>
<th>Value</th>
<th>Parameters</th>
<th>Value</th>
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<td>Length of Collector (L)</td>
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<td>Mass velocity</td>
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</tr>
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<td>Width of Collector (W)</td>
<td>400 mm</td>
<td>Fin spacing (w)</td>
<td>2,3,4,5,6 cm</td>
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<tr>
<td>Duct height (H)</td>
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<td>Thermal conductivity of glass wool (k&lt;sub&gt;gw&lt;/sub&gt;)</td>
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</tr>
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<td>Thickness of fin (δ&lt;sub&gt;f&lt;/sub&gt;)</td>
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<td>Thickness of insulation (δ&lt;sub&gt;ins&lt;/sub&gt;)</td>
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<tr>
<td>Actual length of fin (L&lt;sub&gt;act&lt;/sub&gt;)</td>
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<td>Amplitude of wavy fin (amp)</td>
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<td>Number of glass covers (N&lt;sub&gt;gc&lt;/sub&gt;)</td>
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<td>Wavelength of wavy fin (λ)</td>
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<td>Height of fin (L&lt;sub&gt;f&lt;/sub&gt;)</td>
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</table>

Figure 1. Schematic Diagram of Experimental set up

Table 1. System and operating parameters used

Figure 2. Positions of thermocouples in air stream and on absorber plate
2.2 Experimentation

The wavy fins of known physical characteristics were welded on the absorber plate as shown in fig.5 and fitted between the absorber plate and the bottom plate of solar air heater. The collectors were tested in the horizontal position as per ASHRAE-93 standards [19]. Outdoor testing of both plane and wavy fin solar air heater were done on clear sky days. Before the initiation of experimentation, all the components of the set up and the measuring instruments such as data logger, manometer and the pyranometer had been checked for their proper operation. After that the blower was switched on ensuring no leakage in the joints of duct. The mass flow rate in the duct was adjusted using a flow control valve. The blower was adjusted to run 1 hr prior to the time at which the first data logging start. The temperature of the various thermocouples, wind speed, manometer reading and insolation were recorded daily at an interval of 30 minutes from 9:30 am to 4:30 pm. The test was run for a fixed mass velocity for a specific day. It was decided to take six values of mass flow rates (the partial opening to the full opening of the flow control valve) in order to cover the usual range of mass velocity and five sets of fin spacing.

2.3 Thermal performance

The data such as pressure drop across orifice plate, air and absorber plate temperature at various positions in the channel were recorded to compute the thermal performance of wavy finned absorber solar air heater. The following equations were used to calculate the air mass flow rate (m), energy gain by air (Q_u), thermal efficiency (η) and heat conductance (hA).

\[
m = C_d A_\eta \left[ \frac{2 \rho \Delta P}{1 - \beta^2} \right]^{0.5}
\]

where, \( \Delta P \) is the pressure drop across orifice.

The energy gain by air is,

\[
Q_u = \dot{m} C_p (T_o - T_i)
\]

The average value of inlet air temperature (T_i), outlet air temperature (T_o), for wavy finned absorber solar air heater is calculated as,

\[
T_i = \frac{T_{6A} + T_{7A}}{2}
\]

\[
T_o = \frac{T_{1A} + T_{2A} + T_{3A}}{3}
\]

and for plane solar air heater it is calculated as,

\[
T_i = \frac{T_{5B} + T_{6B}}{2}
\]

\[
T_o = \frac{T_{8A} + T_{1B} + T_{2B}}{3}
\]

The thermal performance of flat plate solar air heater operating under quasi steady state conditions can be given by using the following equation [2];

\[
\eta = \frac{\dot{m} C_p (T_o - T_i)}{IA_c}
\]

Also, for the solar air heaters taking air at ambient temperature, the following equations for thermal efficiency can be given as [2].

\[
\eta = F_0 \left[ (\tau \alpha)_e - U_L \left( \frac{T_o - T_i}{I} \right) \right]
\]

where, \( F_0 \) is the heat removal factor corresponding to outlet air temperature.

Equation shows the plot of efficiency as a function of \( (T_o - T_i)/I \) will result a straight line with slope \(-F_0 U_L\) and the intercept \(F_0(\tau \alpha)_e\).
presented as plots of thermal efficiency vs ΔT/I, the intercept $F_k(\tau\alpha)$ and slope $-F_kU_L$ of these curves can be converted to $F_kU_L$, $F_k(\tau\alpha)$, and $F_U$ by the following and suggested by Duffie & Beckman [2].

$$F_k(\tau\alpha)_e = F_0(\tau\alpha)_e \left(1 + \frac{A_cF_0U_L}{mC_p}\right)^{-1}$$  \hspace{1cm} (9)$$

$$F_kU_L = F_0U_L \left(1 + \frac{A_cF_0U_L}{mC_p}\right)^{-1}$$  \hspace{1cm} (10)$$

$$F_U = -\frac{mC_p}{A_c}\ln\left[1 - \frac{F_0U_LA}{mC_p}\right]$$  \hspace{1cm} (11)$$

The equations (7) and (8) can be represented on a single plot having the same quantity, efficiency on ordinate and $(T_0 − T_f)/I$ on abscissa. Also, this can be obtained from a single regression linear fit line from equation (8).

2.4 Error analysis

Although extreme care has been taken to perform experiments but there is always a chance of error in experimental measurements. So, it is necessary to determine the maximum possible error in the experimental measurements. The error analysis was done for the error interval associated with experimental results. The methodology suggested by Kline and Mc-Clintock [20] has been used to measure the error.

If the value of any parameter is calculated using certain measured quantities then error in measurement of 'φ' (parameters) is given as:

$$\frac{\delta \varphi}{\varphi} = \left[\left(\frac{\delta \varphi}{\delta x_1}\right)^2 + \left(\frac{\delta \varphi}{\delta x_2}\right)^2 + \ldots + \left(\frac{\delta \varphi}{\delta x_n}\right)^2\right]^{0.5}$$  \hspace{1cm} (12)$$

where, $\delta x_1, \delta x_2, \delta x_3, \ldots \delta x_n$ are the possible errors in measurements $x_1, x_2, x_3, \ldots x_n$ and $\delta \varphi$ is called as absolute uncertainty and $\delta \varphi/\varphi$ is known as relative uncertainty. The fractional error analysis of the mass flow rate and the efficiency are found to be 0.0743 and 0.013 respectively. Table 6 shows the accuracy of measuring instruments.

3. RESULTS AND DISCUSSION

This experimental work investigates the effect of fin spacing of wavy finned absorber solar air heater under Jamshedpur, India weather between 14-04-2016 to 31-05-2016 with clear sky conditions. Jamshedpur city of India lies on the geographical coordinates of 22° 48’ N, 86° 11’ E.

Fig.6 shows the variation of insolation versus local time of all the days at which the study was conducted. As expected, the insolation increased from sunrise to peak at noon and then decreased in the afternoon till sunset. The average values of insolation for the experiments of 2, 3, 4, 5 and 6 cm spacing were 861.89, 872.29, 869.02, 867.2 and 858.3 W/m² respectively. The measured insolation were stable throughout the study.
Fig. 6. Variation of Insolation versus different standard local time of (a) 2 cm fin spacing (b) 3 cm fin spacing (c) 4 cm fin spacing (d) 5 cm fin spacing (e) 6 cm fin spacing.

Fig. 7 shows the air temperature rise at different mass velocities for 2, 3, 4, 5 and 6 cm fin spacing. As expected, for each cases, the value of the air temperature rise increases at sun rise to a maximum value at noon and start decreasing in the afternoon. Also, rise in temperature decreases with increasing mass velocity. The maximum value of the air temperature rise was achieved between 12:00 hr to 13:00 hr of local time and varied in magnitude for each day depending on the meteorological conditions such as wind speed and insolation. It also finds that the rise in air temperature increased by decreasing the fin spacing for the same mass velocity. As the fin spacing decreased, the velocity of air also increased for the same mass velocity. The highest average and instantaneous peak rise in air temperature obtained for lowest fin spacing (2 cm) were 50.47°C and 64.33°C respectively, with a mass velocity of 0.0065 kg/s-m², whereas, the average and the maximum value of the air temperature rise obtained for maximum mass velocity of 0.33 kg/s-m² were 33.51°C and 46.13°C, respectively. On the other hand, higher value of fin spacing (6 cm), the average and instantaneous peak rise in air temperature were obtained as 35.44°C and 48.13°C for lower mass velocity (0.0065 kg/s-m²) and 25.80°C and 37.68°C for higher mass velocity (0.033 kg/s-m²) respectively.
Figure 7. Effect of fin spacings on the temperature difference at mass velocities (kg/s-m²): (a) 0.0065, (b) 0.0146, (c) 0.02, (d) 0.025, (e) 0.029, (f) 0.033

Figure 8. Performance plot for solar air heaters for fin spacing 2cm

Figure 9. Performance plot for solar air heaters for fin spacing 3cm

Figure 10. Performance plot for solar air heaters for fin spacing 4cm

Figure 11. Performance plot for solar air heaters for fin spacing 5cm

Figure 12. Performance plot for solar air heaters for fin spacing 6cm

Figs. 8-12 show the experimental values of thermal efficiencies as a function of air temperature rise parameter, i.e; (Tc-Ti)/I of plane and wavy finned absorber solar air heater for various fin spacings. Each line of these figures has been obtained from the linear regression fit of the data for the corresponding fin spacings of the wavy fin absorber solar air heater. Also, the plot for the plane solar air heater has been done for the comparison. The plot shows the increased thermal efficiency with the increase in mass velocity for the both plane as well as wavy fin absorber solar air heaters. It is seen from...
fig. 8 that the efficiency of plane solar air heater increases from 18.54% to 29.2% as the mass velocity increases from 0.0065 kg/s-m² to 0.033 kg/s-m². The corresponding values of thermal efficiency for wavy finned absorber has been obtained as 40% to 65%. These values of efficiencies refer to the regression linear fit lines, whereas, the actual values have been found to vary for each mass velocity with the variation of (Tᵢ - Tₒ)/I for a specific mass velocity. For the mass velocity of 0.0065 - 0.033 kg/s-m² and fin spacing of 2 cm, regression linear fit line show an enhancement in thermal efficiency of 2.15 - 2.23 times in thermal efficiency as compared to plane solar air heater. For the various fin spacing of wavy fin solar air heater and plane solar air heater, the value of thermal efficiencies and the respective enhancement in thermal efficiency obtained from the respective regression linear fit lines have been listed in Table 2. It shows that the fin spacing of 2 cm have the maximum enhancement in efficiency followed by fin spacing of 3, 4, 5 and 6 cm respectively for all mass velocities.

**Figure 13. Performance plot for solar air heaters**

Fig. 13 shows the effect of fin spacing on the thermal performance of wavy fin absorber solar air heater as well as plane solar air heater. The performance lines plotted in the fig. 13 are the linear regression fit lines of experimental data points of corresponding spacing and represented in figs. 8-12. Results show that the performance of wavy finned absorber is a strong function of fin spacing. The difference in the performance of these wavy finned solar air heaters is due to the enhanced heat transfer area and the effective heat transfer coefficient between the wavy fin absorber and air. It is clear from fig. 13 that the fin spacing 2 cm shows the overall best performance followed by fin spacing 3 cm, 4 cm, 5 cm and 6 cm. This is due to the higher value of surface conductance (hA) of the lower fin spacing absorbing higher energy effectively and transfer more energy to the flowing air. The lower fin spacing, having high value of surface conductance, transfer energy from finned absorber to air more effectively and reduces the absorber plate temperatures and thus reduces the thermal losses from the absorber to the environment, resulting in enhanced thermal efficiency. The value of heat transfer coefficient (h) and (hA) overall heat conductance for the various fin spacing and mass velocities have been listed in Table 3. It can be seen from the table that the overall heat conductance and heat transfer coefficient increases with the decrease in fin spacing for the both minimum and maximum mass velocities. Thus the fin spacing of 2 cm is the most efficient absorber for all mass velocities. The enhancement in thermal efficiency of wavy finned absorber solar air heater as compared to plane solar air heater is found to decrease as the value of AT/I increases. The highest value of AT/I has been obtained for the lower fin spacing. This enhancement in thermal efficiency of these absorbers appears due to proceeding towards equality of average absorber plate temperature and air and also the decreasing values of absorber plate due to an appreciable rise in the value of overall conductance for the lower fin spacing (2 cm) absorber plate as compare to higher fin spacing (3, 4, 5 and 6 cm). These conditions favours the increase in collector efficiency factor (F') and hence enhanced collector heat removal factor related to outlet fluid temperature (Fₒ). Also, the value of the overall loss coefficient, Uₒ will decrease according to Shewan and Hollands[21] who have shown that the overall loss coefficient strongly depends on the mean absorber plate temperature as the collector efficiency factor approaches to unity.

The value of performance parameters Fₒ(τα)ₑ and FₒUₒ obtained from the intercept and slope of regression linear fit lines of various fin spacing are listed in Table 4. Also, the respective value of Fₑ and Uₑ has been calculated by calculating the constant value of (τα)ₑ. The value of (τα)ₑ has been calculated as 0.854, which is 1% greater than (τα) to include glass cover plate absorptance as suggested by Duffie and Beckman [2]. The solar air heaters test data presented as plots of thermal efficiency and (Tᵢ - Tₒ)/I, the intercept and slope can be converted to FₑUₑ, Fₑ(τα)ₑ and F'Uₑ by the equations (9-11).

<table>
<thead>
<tr>
<th>Type of Absorber</th>
<th>Fin Spacing (cm)</th>
<th>Mass flow rate (kg/s-m²)</th>
<th>Efficiency of plane solar air heater (%)</th>
<th>Efficiency of wavy fin solar air heater (%)</th>
<th>Enhancement in efficiency (%)</th>
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**Table 3.** Heat transfer coefficient and overall heat conductance

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<tr>
<th>Type of Absorber</th>
<th>Fin Spacing (cm)</th>
<th>Mass velocities (kg/s·m²)</th>
<th>Heat transfer coefficient of plane solar air heater (W/m²·K)</th>
<th>Overall Heat conductance of wavy fin solar air heater (W/K)</th>
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**Table 4.** Collector performance parameters

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<th>(-F_0 U_L)</th>
<th>(F_0)</th>
<th>Fin Spacing (cm)</th>
<th>(F_0 (\tau \alpha)_e)</th>
<th>(-F_0 U_L)</th>
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**Table 5.** Collector performances as a function of mass velocities

<table>
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<tr>
<th>Fin Spacing (cm)</th>
<th>Mass velocities (kg/s·m²)</th>
<th>(F_R (\tau \alpha)_e)</th>
<th>(F_R U_L)</th>
<th>(F' U_L)</th>
<th>(F_R (\tau \alpha)_e)</th>
<th>(F_R U_L)</th>
<th>(F' U_L)</th>
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<td>3</td>
<td>0.6808</td>
<td>5.105</td>
<td>6.30</td>
<td>0.6916</td>
<td>5.132</td>
<td>5.89</td>
<td>0.6922</td>
</tr>
<tr>
<td>4</td>
<td>0.6425</td>
<td>5.439</td>
<td>6.82</td>
<td>0.6461</td>
<td>5.470</td>
<td>6.35</td>
<td>0.6468</td>
</tr>
<tr>
<td>5</td>
<td>0.6089</td>
<td>5.463</td>
<td>6.86</td>
<td>0.6124</td>
<td>5.496</td>
<td>6.38</td>
<td>0.6138</td>
</tr>
<tr>
<td>6</td>
<td>0.6108</td>
<td>6.281</td>
<td>8.24</td>
<td>0.6151</td>
<td>6.322</td>
<td>8.24</td>
<td>0.6158</td>
</tr>
<tr>
<td>Plane</td>
<td>0.3452</td>
<td>6.755</td>
<td>8.64</td>
<td>0.3475</td>
<td>6.802</td>
<td>7.54</td>
<td>0.3479</td>
</tr>
</tbody>
</table>

The value of these parameters for the various fin spacing as a function of mass velocity are listed in Table 5. The values of \(F_R U_L\) and \(F'\) can be calculated by using a constant value of \((\tau \alpha)_e=0.854\) for the various mass velocities.

Fig. 14 shows the thermal efficiency comparison of 6 cm fin spacing with some solar air heater efficiencies available in the literature. The thermal efficiency of wavy fin solar air heater is greater than offset finned solar air heater of Youcef-Ali and Desmons [22] by 10.36% and finned solar air heater of Karim and Hawlader [23] by 29.63% for the investigated range of system and operating parameters. Also, the thermal efficiency values of Karim and Hawlader [15] for plane solar air heater show a deviation ±3.48% from the plane solar air heater of present result. This holds a good agreement between the experimental values and makes the perfection of data collected through experimentation.

**Table 6.** Accuracy of measuring instruments

<table>
<thead>
<tr>
<th>Sl. No.</th>
<th>Name of Instrument</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Pyranometer</td>
<td>±0.5%</td>
</tr>
<tr>
<td>2</td>
<td>Digital Manometer</td>
<td>±0.3%</td>
</tr>
<tr>
<td>3</td>
<td>Thermocouple</td>
<td>±0.1°C</td>
</tr>
</tbody>
</table>

**Figure 14.** Thermal efficiency comparison of 6 cm fin spacing solar air heater with some solar air heaters available in literature.
4. CONCLUSIONS

1. The thermal performance of a solar air heater can be enhanced by using wavy finned absorber and the fin spacing and mass velocity is important parameters for the performance.
2. The effect of insolation, fin spacing and mass velocities on thermal performance has been examined experimentally.
3. The highest value of rise in air temperature has been found for the lowest mass velocity of 0.0065 kg/s-m² as 64.33, 55.31, 52.23, 50.83 and 48.13°C for the fin spacing 2, 3, 4, 5 and 6 cm respectively between 12:00 hr to 13:00 hr of local time as the insolation was maximum, i.e., 1069, 1027, 940, 933 and 956 W/m² respectively.
4. Improved thermal performance of wavy fin solar air heater has been found due to the improved surface conductance of the finned absorber plate.
5. The maximum enhancement in thermal efficiency for wavy finned absorber solar air heater for fin spacing of 2 cm has been found to be 28.71% as compared to fin spacing of 6 cm and 116.67% as compared to plane solar air heater.
6. The maximum value of AT/I for wavy fin spacing 2 cm, 6 cm and plane solar air heater has been achieved as 0.067, 0.048 and 0.029 m²-°C/W respectively.
7. Wavy finned absorber solar air heater is found to be 67.44 to 121.43 percent thermally efficient as compared to plane solar air heater within the investigated range of system i.e. fin spacing of 2 to 6 cm and operating parameters i.e. mass velocity of 0.0065 - 0.033 kg/s-m².

REFERENCES

NOMENCLATURE

\[ h \] heat transfer coefficient (W/m\(^2\)K)  
\[ A_c \] collector area (m\(^2\))  
\[ \text{amp} \] amplitude of wavy fin  
\[ F' \] collector efficiency factor  
\[ F_R \] collector heat removal factor  
\[ H \] duct height (cm)  
\[ I \] insolation (W/m\(^2\))  
\[ L \] length of collector (m)  
\[ L_{act} \] actual length of fin (m)  
\[ \overline{h} \] heat transfer coefficient (W/m\(^2\)K)  
\[ A_{c} \] collector area (m\(^2\))  
\[ \text{amp} \] amplitude of wavy fin  
\[ F' \] collector efficiency factor  
\[ F_R \] collector heat removal factor  
\[ L_d \] height of fin (cm)  
\[ N_{gc} \] number of glass covers  
\[ T_i \] inlet air temperature (K)  
\[ W \] fin spacing (cm)  
\[ W \] width of collector (m)  
\[ \delta i \] thickness of fin (mm)  
\[ T_o \] outlet air temperature (K)  
\[ A \] total heat transfer area (m\(^2\))  
\[ C_p \] specific heat of air (J/kgK)  
\[ \rho_w \] thermal conductivity of glass wool (W/m-K)  
\[ T_{m} \] mean temperature of air (K)  
\[ T_{m} \] mean temperature of absorber plate (K)  
\[ \frac{m}{A_{c}} \] mass velocity (kg/s-m\(^2\))  
\[ \Delta T \] rise in temperature (K)  
\[ \lambda \] wavelength of wavy fin (mm)  
\[ C_d \] coefficient of discharge  
\[ \overline{h}A \] thermal conductance (W/K)  
\[ \delta \tau_{ms} \] transmittance absorbance product  
\[ \delta i_{ms} \] thickness of insulation (mm)  
\[ \eta \] thermal efficiency

APPENDIX

Error analysis

Although extreme care has been taken to perform experiment but there is always a chance of error in experimental measurements. So, it is necessary to determine maximum possible error in the experimental measurements. The error analysis was done for the error interval associated with experimental results. The methodology suggested by cline and Mc Clintock [20] has been used to measure the error. If the value of any parameter is calculated using certain measured quantities then error in measurement of \( \varphi \) (parameters) is given as:

\[
\frac{\delta \varphi}{\varphi} = \left[ \frac{\delta \varphi}{\delta x_1} \right]^2 + \left[ \frac{\delta \varphi}{\delta x_2} \right]^2 + \cdots + \left[ \frac{\delta \varphi}{\delta x_n} \right]^2 \right]^{0.5}
\]

where \( \delta x_1, \delta x_2, \delta x_3, \cdots, \delta x_n \) are the possible errors in measurements \( x_1, x_2, x_3, \cdots, x_n \) and \( \delta \varphi \) is called as absolute uncertainty and \( \frac{\delta \varphi}{\varphi} \) is known as relative uncertainty.

1. Area of absorber plate

\[
A_p = (W \times L)
\]

\[
\delta A_p = \left[ \left( \frac{\delta A_p}{\delta L} \times \delta L \right)^2 + \left( \frac{\delta A_p}{\delta W} \times \delta W \right)^2 \right]^{0.5}
\]

2. Area of flow

\[
A_f = (W \times L_{act}) + n(L_d \times L_{act})
\]

\[
\delta A_f = \left[ \left( \frac{\delta A_f}{\delta L_{act}} \times \delta L_{act} \right)^2 + \left( \frac{\delta A_f}{\delta W} \times \delta W \right)^2 + \left( \frac{\delta A_f}{\delta L_d} \times \delta L_d \right)^2 \right]^{0.5}
\]

3. Area of orifice meter (\( A_o \))

\[
A_o = \frac{\pi}{4} d_o^2
\]

\[
\delta A_o = 2 \frac{\pi d_o}{4} = \frac{\pi d_o}{2}
\]

\[
\delta A_o = \left( \frac{\pi d_o}{2} \right) \delta d_o
\]

\[
\frac{\delta A_o}{A_o} = \frac{2 \delta d_o}{d_o} = \frac{2 \times 0.05}{d_o} = 0.526%\]

\[
\delta A_o = 2 \frac{\pi d_o}{d_o} = 2 \times 0.05 = 0.10%\]

\[
\delta A_o = \frac{\pi d_o}{2} = \frac{\pi d_o}{2} \times 0.05 = 0.125%\]

\[
\delta A_o = \frac{\pi d_o}{2} = \frac{\pi d_o}{2} \times 0.05 = 0.125%\]
4. Mass flow rate (\( \dot{m} \))

\[
\dot{m} = C_d A_o \left[ \frac{2 \rho \Delta P}{1 - \beta^4} \right]^{0.5}
\]

\[
\frac{\delta \dot{m}}{\dot{m}} = \left[ \left( \frac{\delta C_d}{C_d} \right)^2 + \left( \frac{\delta A_o}{A_o} \right)^2 + \frac{1}{4} \left( \frac{\delta \rho}{\rho} \right)^2 + \frac{1}{4} \left( \frac{\delta (\Delta P)}{\Delta P} \right)^2 + \frac{1}{4} \left( \frac{\delta \beta}{\beta} \right)^2 \right]^{0.5}
\]

\[
= \left[ (0.016)^2 + (0.00526)^2 + \frac{1}{4} (0.0083)^2 + \frac{1}{4} (1/25)^2 + \frac{1}{4} (0.00121)^2 \right]^{0.5}
\]

\[= 0.0437 \text{ or } 4.37\%
\]

5. Useful heat gain (\( Q_u \))

\[
Q_u = \dot{m} C_p (T_o - T_f)
\]

\[
\frac{\delta Q_u}{Q_u} = \left[ \left( \frac{\delta \dot{m}}{\dot{m}} \right)^2 + \left( \frac{\delta C_p}{C_p} \right)^2 + \left( \frac{\delta (\Delta T)}{(\Delta T)} \right)^2 \right]^{0.5}
\]

\[= [(0.0437)^2 + (1/1005)^2 + (0.5/15.2)^2]^{0.5}
\]

\[= 0.0547 \text{ or } 5.47\%
\]

6. Heat transfer coefficient (\( h \))

\[
\bar{h} = \frac{Q_u}{A_p (T_{pm} - T_{pm})}
\]

\[
\frac{\delta \bar{h}}{\bar{h}} = \left[ \left( \frac{\delta Q_u}{Q_u} \right)^2 + \left( \frac{\delta A_p}{A_p} \right)^2 + \left( \frac{\delta T_{pf}}{T_{pf}} \right)^2 \right]^{0.5}
\]

\[= \left[ (0.0547)^2 + (0.00358)^2 + (1/12)^2 \right]^{0.5}
\]

\[= 0.09974 \text{ or } 9.974\%
\]