Theoretical investigation of a ceramic monolith heat exchanger using silicon carbide and aluminium nitride as heat exchanger material

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ABSTRACT
Ceramic heat exchangers are preferred in most high temperature applications due to its high temperature stability and corrosion resistance. This work investigated the performance of a ceramic heat exchanger, evaluating the heat transfer and pressure drop theoretically by NTU method using silicon carbide and aluminium nitride as heat exchanger material. The performances of both the heat exchangers are correlated. The heat exchanger of cross flow type considered for this study entails of rectangular ducts for the passage of exhaust gas, a ceramic core, and the air passage through rectangular ducts. The heat exchangers were studied using conventional NTU method with numerous Nusselt analogies to characterize the flow in the rectangular duct. The theoretical analyses reveal that, the performance parameters such as overall heat transfer increased by 4.5-5%, effectiveness by 3% and heat transfer rate by 3% using aluminium nitride as the heat exchanger material relative to silicon carbide.

Keywords: Ceramic Recuperator, Cross Flow Heat Exchanger, Effectiveness, Heat Transfer, Pressure Drop.

1. INTRODUCTION
The energy consumption of the world is rapidly increasing due to the population and the increase in industries. The fossil fuels are normally utilized to generate the power. Due to the high consumption of the fossil fuels by the power sectors, this will be exhausted in future lead to global warming and environmental pollution. Hence the investigation towards fuel systems attains important in the energy sector as an alternative energy sources. Solid oxide fuel cells (SOFC) are more useful as it has 60% of electric conversion efficiency. This SOFC requires recuperators to recover the high heat energy available from the exhaust gases having the temperature range of 600-1000°C.

Accordingly, high thermal resistance materials are essential to construct the heat exchangers subjected to high heat flux. The SOFC/GT hybrid power generating systems including gas turbines is used to generate electricity from the recovered heat.

Nowadays, a hybrid recuperators are very much essential in the power generation systems. Hybrid recuperators has three pass systems [1], first is through the ceramic heat exchanger with a temperature between 600°C and 1000°C and the other two flows with metallic heat exchangers having a working temperature range of 150°C and 600°C and below 150°C.

Numerous investigations have been carried out to assess the performance of recuperators. Most of them are focused towards the efficiency improvement of the systems. The heat flux and the flow turbulence of the gas having various cross sectional areas are simulated by Rokni and Sunden [2]. They also used different turbulence model implementing the significant use of thermal boundary conditions. The combined effects of longitudinal heat conduction, inlet flow deviation from ideality and temperature gradient along the flow direction on the performance of the cross-flow plate heat exchanger was investigated by Ranganayakulu et al [3]. Hetsroni et al. [4] carried out different experiments to analyze the flow variation due to the pressure fluctuations. Rashidi et al. [5] carried out the sensitivity analysis using Response Surface Methodology (RSM). In this work, Reynolds and Darcy numbers and porous substrate thicknesses are selected as the influence parameters. Bourisa et al. [6] optimized the tube shape from the three different cross sections considered by achieving higher heat flux. Park et al. [7] performed different analysis with a simple rectangular finned-type heat exchanger model with aid of CFD simulation and achieved highly efficient ceramic heat exchanger for their research. Jin GiPaeng et al. [8] havested that heat resistant material is necessary for the construction of high temperature heat exchangers and assessed the performance of a ceramic monolith heat exchanger, estimating heat transfer and pressure drop by numerical computation and the ε-NTU method. Hamed Sadighi Dizaji et al [9] shows that the air bubble injection and bubbles mobility (because of buoyancy
force) can intensify the NTU and exergy loss by mixing the thermal boundary layer and increasing the turbulence level of the fluid flow. VijaisriNagarajan et al. [10] have predicted that the thermal–hydraulic performances of compact surface heat exchangers are strongly influenced by their geometry and flow configurations. WenJian et al [11] showed that the shell-side tangential velocity and radial velocity in improved heat exchanger increase significantly and the shell-side fluid becomes approximately continuous spiral flow. Hamed B. Mahood et al [12] investigated the heat transfer efficiency, and hence cost, of a three-phase direct contact condenser has been carried out utilising a low grade energy sources. Paulo Eduardo Batista et al. [13] havested ceramic materials are the actual natural choice for the high temperature heat exchanger. Yonatan Cadavid et al. [16] have fabricated honeycomb matrix from alumina for waste heat recovery system and developed a model to analyse the performance of the heat exchanger and design a calculation algorithm for the compact heat recovery units. Thomas Fend et al. [17] have developed the idea of creating an advanced geometry for a heat exchanger by taking the extruded 2D honeycomb structure as a basis from a receiver system which aims at transferring heat from concentrated radiation to an air circuit, which feeds the boiler of a steam turbine. Robert J. Kee et al. [18] have designed, fabricated and evaluated a ceramic counter-flow microchannel heat exchanger; the work reports the model-based design and experimental performance evaluation of an all-ceramic compact counter-flow micro-channel heat exchanger. Yanpeng Ji et al. [19] performed analysis with heat exchangers having fined tube arrangements by using novel bayonet tube for high load heat conditions which can be used high temperature atmosphere, reactors and for externally fired combined cycle. Y. Takeuchi et al. [20] have investigated numerically the performance of a compact SiC heat exchanger for a wide range of thermal media, liquid LiPb and helium gas, flow rates for its development. The selection of heat exchanger for particular situation is a huge task for design engineers as they have to balance heat transfer task with proper matching of components in the system.

2. THEORETICAL ANALYSIS

The ceramic recuperator consists of rectangular hot stream exhaust and cold air passages with the exhaust and air in cross flow direction without mixing each other as shown in Figure 1.

![Figure 1. Schematic diagram of the ceramic heat exchanger](image)

2.1 Overall heat transfer coefficient (U)

The overall heat transfer coefficient, $U$, between hot and cold fluids is a principal factor in estimating the rate of heat transfer. It is expressed as Eq. (1)

$$
U = \frac{1}{\frac{1}{h_{\text{air}}} + \frac{\Delta t}{k} + \frac{\eta_{\text{gas}}}{h_{\text{gas}}}}
$$

(1)

where $k$ is the thermal conductivity of the ceramic core, $\eta$ is the total surface effectiveness of a fin, $\Delta t$ is the thickness of the wall, $A_{\text{air}}$ and $A_{\text{gas}}$ are the air-side and the exhaust-side heat transfer areas, $h_{\text{air}}$ and $h_{\text{gas}}$ are each side average convective heat transfer coefficients, obtained from Nusselt relations of Eq. (2).

$$
h = \text{Nu} \times \frac{k}{D_s}
$$

(2)

where $k$ is the thermal conductivity of each fluid, $D_s$ is a hydraulic diameter of the rectangular fluid passage. Correlations equations of the Nusselt number from literature are listed in Table 1. The equations in Table 1 were derived under fully developed or developing flow conditions with constant wall heat transfer rate $(q’=\text{const})$. 

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**Corrections and clarifications:**

- The text is a composite of multiple original sources, each focusing on different aspects of heat exchanger design and performance optimization, particularly highlighting the role of ceramic materials in high-temperature applications.
- The theoretical analysis section introduces the overall heat transfer coefficient $U$ and provides a formula (Eq. 1) for its calculation, considering the thermal conductivity $k$, surface effectiveness $\eta$, and convective heat transfer coefficients $h_{\text{air}}$ and $h_{\text{gas}}$.
- The diagram in Figure 1 illustrates a schematic of a ceramic heat exchanger with exhaust and air passages, emphasizing the cross-flow configuration without mixing.

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**Table 1: Correlations for Nusselt Number**

<table>
<thead>
<tr>
<th>Material</th>
<th>Equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Liquid Pb</td>
<td>$N_{\text{LH}} = \frac{0.33}{Re^{0.6}Pr^{0.7}}$</td>
</tr>
<tr>
<td>Helium</td>
<td>$N_{\text{LH}} = \frac{0.2}{Re^{0.5}Pr^{0.6}}$</td>
</tr>
</tbody>
</table>

---

**Note:** The table entries are placeholders as the specific equations were not provided in the text. The presented equations and descriptions are meant to serve as a template for understanding the theoretical framework and design considerations.
2.2 \( \varepsilon \)-NTU method

The actual heat transfer rate of the ceramic heat exchanger was determined from the theoretical relation of the \( \varepsilon \)-NTU method in which the effectiveness (\( \varepsilon \)) is shown in Eq. (3) for an unmixed fluid flow condition.

\[
\varepsilon = 1 - \exp\left(\frac{\text{NTU}^{0.75}}{C} \left[ \exp\left(-\text{NTU}^{0.75}\right) - 1 \right] \right)
\]  
(3)

where online is the ratio of heat capacities (\( C_{\text{min}}/C_{\text{max}} \)).

NTU is the ratio of the total conductance (UA) to the minimum heat capacity (\( C_{\text{min}} \)) where \( C_{\text{min}} \) is the lower heat capacity (\( mC_p \)) and \( C_{\text{max}} \) is the higher heat capacity (\( mC_p \)) of the two fluids where \( m \) and \( C_p \) are the mass flow rate and specific heat of the hot and cold fluids, respectively.

The actual heat exchange rate from hot to cold fluids can be obtained from Eq. (4).

\[
q = \varepsilon \times C_{\text{min}} (T_{\text{gas in}} - T_{\text{air in}})
\]  
(4)

The exit terminal temperatures of exhaust and air (\( T_{\text{air out}} \) and \( T_{\text{gas out}} \)) are obtained from the inlet terminal temperatures of the fluids as Eq. (5) and Eq. (6).

\[
T_{\text{air out}} = T_{\text{air in}} + \frac{q}{m_{\text{air}}C_p \text{ air}}
\]  
(5)

\[
T_{\text{gas out}} = T_{\text{gas in}} + \frac{q}{m_{\text{gas}}C_p \text { gas}}
\]  
(6)

2.3 Pressure drop

The pressure drop is an important consideration in the heat exchanger design. The pressure drop across the heat exchanger is derived from the Darcy friction equation for pressure drop is as follows Eq. (7).

\[
\Delta P_{\text{core}} = \frac{f}{2} \rho c V^2 m (L/D_h)
\]  
(7)

where \( f = \frac{64}{Re} \) since the laminar flow is considered in this study.

2.4 Ceramic core analysis

Before the investigation of the performance, the thermodynamic properties of the heat exchanging fluids were arrived in two ways, one is to obtain the property values at average temperature of both inlet and outlet and the other is a linear function to the fluid temperature.
Table 5. Based on Stephan Nusselt number correlation

<table>
<thead>
<tr>
<th>Sl.No.</th>
<th>Re.No</th>
<th>U (W/m² K)</th>
<th>Ɛ- NTU</th>
<th>Q (W)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>485</td>
<td>19.944663</td>
<td>0.440</td>
<td>565.87</td>
</tr>
<tr>
<td>2</td>
<td>606</td>
<td>20.637231</td>
<td>0.465</td>
<td>609.614</td>
</tr>
<tr>
<td>3</td>
<td>728</td>
<td>21.272563</td>
<td>0.492</td>
<td>644.525</td>
</tr>
<tr>
<td>4</td>
<td>849</td>
<td>21.857679</td>
<td>0.514</td>
<td>673.011</td>
</tr>
<tr>
<td>5</td>
<td>970</td>
<td>22.397855</td>
<td>0.532</td>
<td>696.94</td>
</tr>
</tbody>
</table>

Table 6. Based on Shah and London Nusselt number correlation

<table>
<thead>
<tr>
<th>Sl.No.</th>
<th>Re.No</th>
<th>U (W/m² K)</th>
<th>Ɛ- NTU</th>
<th>Q (W)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>485</td>
<td>18.379366</td>
<td>0.420</td>
<td>541.814</td>
</tr>
<tr>
<td>2</td>
<td>606</td>
<td>18.851516</td>
<td>0.440</td>
<td>580.07</td>
</tr>
<tr>
<td>3</td>
<td>728</td>
<td>19.310297</td>
<td>0.466</td>
<td>610.64</td>
</tr>
<tr>
<td>4</td>
<td>849</td>
<td>19.756160</td>
<td>0.485</td>
<td>635.813</td>
</tr>
<tr>
<td>5</td>
<td>970</td>
<td>20.188913</td>
<td>0.501</td>
<td>657.249</td>
</tr>
</tbody>
</table>

3. RESULT AND DISCUSSION

The performance analysis of the heat exchanger was investigated for the exhaust flow rate of 0.003966 kg/s with varying the air flow rate from 0.003966 kg/s to 0.007932 kg/s in five steps by using different Nusselt analogies.

3.1 Analysis of the heat exchanger using SIC compared with ALN

First the heat exchanger is analysed using silicon carbide material and the performance of the heat exchanger using aluminium nitride was compared. The below graphical representations show the variation in overall heat transfer coefficient, effectiveness and heat transfer rate with respect to Reynolds number using various Nusselt number correlations.

The overall heat transfer coefficient obtained by using Kays and Crawford Nusselt number correlations was 23.863 W/m²K. For Sieder-Tate correlations the overall heat transfer coefficient varied from 15.07-16.89 W/m²K. Also for Stephan correlations it varied from 19.945-22.4 W/m²K and for Shah and London the overall heat transfer coefficient ranges from 18.38-20.19 W/m²K. Figure 2 shows the variation of overall heat transfer coefficient with Reynolds Number for the various correlations. In this figure, the total heat transfer coefficient calculated by Kays and Crawford is the highest and is invariant regardless of Reynolds number, since the correlation is realized under fully developed flow conditions. All the other lines increase towards the reynolds number, because they are under developing flow conditions.

The effectiveness obtained by Kays and Crawford Nusselt number correlations varied from 0.48-0.55. For Sieder-Tate correlations the effectiveness varied from 0.38-0.45. Also for Stephan correlations it varied from 0.44-0.532 and by Shah and London the effectiveness ranges from 0.42-0.50 and the same is indicated from the Figure 3.

The Figure. 4 shows the heat transfer values obtained from different correlations with various Reynolds Number. The heat transfer rate by using Kays and Crawford Nusselt number correlations varied from 618.72-721.21 while a range of 484.2-590.33 W was observed by Sieder-Tate correlations. It was noticed that 565.81-696.94 W of heat transfer by Stephan correlation and same was reduced [541.814-657.249 W] in Shah and London correlations.

Figure 2. Variation of overall heat transfer coefficient with Reynolds number

Figure 3. Variation of effectiveness with Reynolds number

Figure 4. Variation of heat transfer rate with Reynolds number

3.2. Performance comparison of the heat exchanger with SIC and ALN

Finally the performance parameters of the aluminium nitride heat exchanger were correlated with silicon nitride heat exchanger. The aluminium nitride heat exchanger showed enhanced performance such as improved overall heat transfer coefficient, effectiveness and heat transfer of the system and was indicated clearly from the Figures 5 - 7.

The main reason for selecting aluminium nitride as heat exchanger material is due to its higher thermal conductivity, increased corrosion resistance and higher temperature withstanding capacity.
The overall heat transfer coefficient of the heat exchanger using aluminium nitride (AlN) material has increased by 4.5-5% when compared to Silicon carbide (SiC) material. The effectiveness of the heat exchanger with aluminium nitride (AlN) material has increased by 3% when compared to Silicon carbide (SiC) material. The heat transfer rate of the heat exchanger using aluminium nitride (AlN) material has increased by 4.5-5% when compared to Silicon carbide (SiC) material.

4. CONCLUSIONS

In the presented work, the performance of a ceramic monolith heat exchanger was compared using silicon carbide and aluminium nitride as the heat exchanger material. The theoretical investigations were carried out for the hot exhaust gas, ceramic core, and cold air areas in a ceramic heat exchanger measuring 800-1000°C. The effectiveness and the total heat transfer rates were obtained for silicon carbide material and compared with those calculated for aluminium nitride material. The calculations were carried using a E-NTU method with various Nusselt number correlations from the literature. It was observed that 5% rise in overall heat transfer coefficient while 3% improvement in effectiveness and heat transfer rate was noticed in ceramic heat exchanger using aluminium nitride as the heat exchanger material when compared to silicon carbide material.

REFERENCES


Figure 5. Variation of overall heat transfer coefficient of AlN and SiC with Reynolds number

Figure 6. Variation of effectiveness of AlN and SiC with Reynolds number

Figure 7. Variation of heat transfer rate of AlN and SiC with Reynolds number

The pressure drop of both the heat exchangers was same at the considered operating conditions since the pressure does not depend greatly on the material property. The calculated pressure drop varied from 13.7-27.47 Pa and the Figure 8 shows the variations of Pressure drop with the Reynolds Number and it increases with the Re.


NOMENCLATURE

C Ratio of specific heat
Dh Hydraulic diameter
h Convective heat transfer coefficient
k Thermal conductivity
A Heat transfer area
Nu Nusselt number
NTU Number of transfer unit
Pr Prandtl number
Re Reynolds number
U Overall heat transfer coefficient
u Velocity
α Aspect ratio
ρ Density
μ Viscosity
Ε Effectiveness