Analysis of the Movement Characteristics of Corona Winds during Needle-Plate Discharge

Jiewen Deng¹, Hongwei Qu², Jianqing Lin³, Guoxin Yu⁴ and Qin Deng⁴*

¹School of Energy Power and Mechanical Engineering, North China Electric Power University, Beijing 102206, China
²School of Energy and Power Engineering, Northeast Dianli University, Jilin 132012, China
³Nuclear Power Engineering Co., Ltd, Shenzhen 518027, China
⁴Beijing green energy technology Co., Ltd,Beijing 102206, China

Email: dengqin1818@163.com

ABSTRACT

In order to study corona wind flow during the negative corona discharge of needle plates, a total-ion numerical model of corona winds was established based on a constant-coefficient partial differential equation. By coupling the electrostatic field Poisson equation and the fluid control equation, we analyzed the electrohydrodynamics of needle-plate coronas. At the respective voltages of -9 kV and -16 kV, an experiment was conducted on the velocities of the corona wind flows generated from corona electrodes of three different curvature radii. The corresponding results show that the corona wind’s low velocity at the needle point (the site of the corona) increased rapidly along the axial direction, leveled off at a certain value, and then dropped down. The larger the potential difference between plates, the faster the corona wind; the smaller the radius of curvature of the corona, the faster the corona wind to be generated around the pole tip.

Keywords: Corona wind, Partial differential equation, Electro hydrodynamics, Air ionization, High voltage discharge.

1. INTRODUCTION

Electrostatic precipitator (ESP) [1] is commonly used in removing charged particles by carrying them towards the plate for absorption under the action of a high-voltage electrostatic field. The key to dust removal performance improvement lies in removing 0.3-1.0 μm particles in a more efficient manner. However, when drifting towards the dust collector plate, particles of this size range can be greatly affected by the flow field near electrode plate which is ruled by the electro fluid formed during needle-plate discharge. Actual operation is frequently accompanied by problems such as dust re-entrainment and cathode line swell [2-4], which is closely linked to the flow field distribution in the vicinity of the electrode plate.

The corona phenomenon in electrostatic precipitator results from self-maintained discharge [5-8] in a very uneven electric field that is formed between plates during the electric discharge around the upper needle end of cathode lines. Due to the formation and quick motion of massive charged ions under the action of the electric field force, their collision with particles in the air triggers an air jet and further disturbs nearby gases, and thus the corona wind forms with the occurrence of a corona [9]. According to many researchers, it is the corona wind generated by the corona in the electrostatic precipitator that mainly propels particles towards the plate side, which has a great impact on the dust removal performance. To overcome this problem, some studies have been undertaken on measurement of corona winds, but the findings differ greatly from each other. For example, Hinds indicated that the speed of corona winds exceeded 75 m/s in the corona region [10].

Current experimental systems applied to measuring corona wind velocity are complicated and costly, with tracer particles as the medium in most cases [11]. By gauging the speed of tracer particles moving in the air, the corona wind velocity can be calculated and falls within the range of 1-10 m/s [12-15].

In terms of experimentation, Zeng Yuxuan et al. [16] studied the relationship between input power, electrode spacing and ionic wind velocity by using a two-dimensional laser particle imaging velocimetry technique. With the semi-empirical formula, Ling and Lin [17] obtained the mean speed (1.162 m/s) of the ionic corona wind between a circular corona electrode and an earth plate. Gong Tao [18] employed a multi-pin-net structure to have stable electricity discharged. The product of steady-velocity corona winds resulted in an ionic wind of certain speed. Wang Wei [19] studied the characteristics of thrust of corona winds generated by using the same structure. Yang Lanjun et al. [20] applied PIV to the measurement of ionic winds of needle-plate electrodes,
The products of corona discharge included electrons, negative ions, positive ions [26], and neutral ions. For this complex physical process, most researchers sacrifice the accuracy of calculation for the reduction in computational load by using the single-ion method. In this paper, the total-ion mathematical model was employed to describe corona wind [20].

The flow control equation:

\[ \rho_{\text{air}} \left( \frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla)\mathbf{v} \right) = -\nabla p + \mu \nabla^2 \mathbf{v} + f \]  

where: \( \mu \) is the air viscosity coefficient, \( f \) is the body force exerted on the flow.

Poisson equation of electrostatic field [27]:

\[ E = -\nabla V \]  

\[ \nabla^2 V = -\frac{\rho}{\varepsilon_0} = -\frac{\varepsilon (n_e - n_+ - n_-)}{\varepsilon_0} \]

where: \( E \) is the space vector of the electric field, \( V \) is the potential of a spatial position \((x, y, z)\), \( \rho \) is the bulk density of charge volume at the spatial position \((x, y, z)\), \( \varepsilon_0 \) is the vacuum dielectric constant, and \( n_e, n_+, n_- \) and \( n \) represent the ion concentrations of electrons, positive ions and negative ions, respectively.

Ion diffusion equation:

\[ \frac{\partial n_e}{\partial t} + \nabla \cdot (-\mu_e n_e \mathbf{v} + n_e \mathbf{v} - D_e \nabla n_e) = (\alpha - \eta) \mathbf{v} \cdot \mathbf{v} \]  

\[ \frac{\partial n_+}{\partial t} + \nabla \cdot (-\mu_+ n_+ \mathbf{v} + n_+ \mathbf{v} - D_+ \nabla n_+) = -\alpha \mathbf{v} \cdot \mathbf{v} \]  

\[ \frac{\partial n_-}{\partial t} + \nabla \cdot (-\mu_- n_- \mathbf{v} + n_- \mathbf{v} - D_- \nabla n_-) = \eta \mathbf{v} \cdot \mathbf{v} \]  

\[ f = \rho E - \frac{1}{2} E^2 \nabla \varepsilon + \frac{1}{2} \nabla (E^2 \rho_{\text{air}} \frac{\partial \varepsilon}{\partial \rho_{\text{air}}}) \]

in which \( D_e, D_+ \) and \( D_- \) denote the diffusion coefficients of electrons, positive ions and negative ions, respectively; \( \mu \) is the mobility speed of each ion; \( \alpha \) represents the impact-ionization coefficient; \( \eta \) is the adhesion coefficient; \( \mathbf{v} \) is the electron drift velocity; \( \mathbf{v} \) is the flow velocity; \( f \) is the vector of electric body force and \( \rho_{\text{air}} \) is the air density.

3. RESULTS AND DISCUSSION

3.1 Electric field distribution

Figure 2 shows the electric field strength of sample points on the edge of the corona pole during the discharge process at different voltages and radiiues of curvature. According to the calculation results, points approaching the tip of the corona pole had higher electric field strengths because of the electrodes geometric effect. Around the pole tip with a small radius of curvature, there was significant spatial change of potential distribution, which contributed to a larger bulging part of the spatial field strength of cathode lines. Accordingly, the electric field inhomogeneity was remarkable such that it
resulted in the occurrence of “tip discharge” or corona. As can be seen from the results, the field strength became larger at positions closer to the discharge tip. When the curvature radii of the corona electrodes were the same, the higher the corona voltage, the higher the field strength; and when the corona voltages were equal, the smaller the curvature radii of the corona electrode, the higher the field strength. High field strength was the predominant factor affecting corona generation. The relationships between the radius of curvature of corona tip and the electric field strength coordinated with the conditions in which the electric corona can occur.

![Graph showing electric field strength at the edge of the corona pole.]

**Figure 2.** The electric field strength at the edge of the corona pole

### 3.2 Corona wind velocity field distribution

![Graph showing cloud map of corona wind velocity.]

**Figure 3.** Cloud map of corona wind velocity
Figure 3 shows the distributions of corona wind velocity at a range of curvature radiuses and discharge voltages. The velocity field in the needle plate facing area presents an N shape with higher values in the middle part. The development trends of corona winds at different radii of curvature were similar to each other. By referring to Figure 4, it can be seen that the smaller the absolute value of the voltage, the less the curvature radius responds to corona wind velocity; and the smaller the curvature radius of the needle end, the faster the corona wind becomes. The reason for this phenomenon is that a small curvature radius contributes to the generation of an uneven electric field of high strength much more easily, thus the body force generated by the electro fluid is greater. As a result, the initial force obtained by charged ions generated from corona maximized itself such that the acceleration was relatively large, which further increased the speed of the corona wind. From the velocity vector in the figure, we can see that the corona wind started from the corona pole tip, and moved toward the positive plate until encountering the blocking force against the positive plate. It then decelerated and spread out along the plate surface, leading to nearby gas flow. The trajectory of corona wind became curve-like, which, together with the gas flow, impedes dusts from gathering on the plate, thus reducing the dust removal efficiency.

3.3 Response of corona wind speed to voltage

Figure 4. Coordinate system of corona wind velocity field

To better analyze the variation of the velocity field near the tip of the corona wind, the coordinate system in Figure 4 was constructed with the direction along the anode plate taken as the X-axis, the direction along the center line of the corona pole as the Y-axis, and the point on the anode plate directly opposed to the center line of the corona pole as the coordinate origin.

Figure 5 shows Y-direction corona wind velocities at different voltages (when X=0, it refers to the central axis of the solution domain). The results show that under the same calculation conditions, areas along the Y direction are mainly divided into the acceleration region, stable region and attenuation region. The farther the wind was from the corona pole, the smaller the velocity. Corona wind formed at the tip of the corona pole. Within a short distance, the velocity increased from 0 to the maximum value, stabilized for a period, and then decreased rapidly. In addition, at different voltages, the larger the absolute value of corona discharge, the faster the corona wind; and the shorter the distance left for acceleration, the larger the axial scope of the steady-speed area. If the potential difference between plates is large, corona wind velocity will increase to the peak value for an instant. This law applies at various curvature radii of needle. By combining equation (2) and (7), it can be seen that the higher the potential difference, the larger the electric flow strength, which intensifies the electric field force and the value of the body force in equation (1). Therefore, the potential gradient distribution is the key to controlling the velocity field distribution in the corona area. As shown in Figure 2, the electric field strength was large near the tip of the corona, which decreased rapidly along the axial direction.

Upon the occurrence of corona, charged ions were subject to a strong electric field force (the acceleration field force) such that the corona wind velocity jumped upward from 0. Then, these ions entered an area where the electric field strength was poor. Accordingly, the electric field force exerted on them was weakened. Meanwhile, the corona wind speed rose to the maximum value and then stabilized. When approaching the earth plate, the corona wind decelerated under the blocking force of the baffle plate.
Figure 6 shows the change of corona wind velocity in the X direction (when \( Y = 10.5 \) mm, it refers to the horizontal position of the discharge tip in the solution domain). It can be seen that the higher the absolute value of the discharge voltage, the larger the corona wind velocity in the horizontal direction, and the easier it is for the wind to attenuate. In addition, the corona wind speed was 0 at the tip of the corona pole, rising quickly to the peak value and then plummeting in the horizontal direction. This phenomenon was commonly seen at different voltages, and the reason is: the flow of corona wind occurred in the corona area, whose changes in velocity triggered the velocity change in other positions; the larger the absolute value of the voltage, the larger the field strength, and the greater the electric field force exerted on the electric fluid, which in turn rendered the horizontal diffusion distance of charged particles small. As can be seen from Figure 2, the greater the absolute value of the voltage, the smaller the horizontal width of the high-speed area.

![Corona wind velocity in X direction at different radii of curvature](image)

**Figure 6.** Corona wind velocity in X direction at different voltages

3.4 Influence of curvature radius on corona wind velocity

Figure 7 shows Y-direction corona wind velocities at different radii of curvature. As can be seen, the farther the corona wind is from the corona pole in the X direction, the faster the wind speed attenuates whatever the curvature radius. The fact that the smaller curvature radius corresponds to quicker attenuation, indicates that apart from discharge voltage, the radius of curvature also played a contributory factor to the width of the high-speed corona wind area. At various radii of curvature, velocities approach 0, both at the tip of the corona pile and near anode plates, albeit the difference of regional velocity between electrodes. This phenomenon shows that curvature radius only affects the speed of corona wind and the boundary of high-speed corona wind area, but is powerless with respect to other trends of change. In addition, when the X value was 3 mm and 4 mm, the stable region was shorter. This phenomenon is also reflected in Figure 5. It can be inferred from the cloud map of corona velocity in Figure 3 that the phenomenon resulted from the limiting of the corona area. In negative corona discharge, negative ions and electrons were generated at the tip of the discharge electrode. Because the tip had a relatively high field strength, the electric field force of these charged ions was greater and thereby the accelerating time was shorter. Meanwhile, these charged ions were moving vertically to the anode plate when they left the tip of the discharge electrode. Under the action of a strong electric field force, it was difficult for these ions to spread in the horizontal direction. Therefore, the high-speed corona wind area had arc-shaped boundaries and mainly lay inside the corona area. When the X value was 3 mm or 4 mm, the vertical sampling line passed through only a small portion of the high-speed area, leading to a shorter stable region at the location.

![Y-direction corona wind velocity at different radii of curvature](image)

**Figure 7.** Y-direction corona wind velocity at different radii of curvature
Figure 8 shows the X-direction corona wind velocities at different radii of curvature. It was found that the smaller the radius of curvature, the larger the corona wind velocity in the area where the corona is facing the earth plate, and the faster the horizontal speed attenuation, which was reduced to a similar value in the end. In addition, when the curvature radius changed, the horizontal width of the high-speed-speed area also varied. By referring to the speed field in Figure 2, we summarized that the smaller the curvature radius, the narrower the fast-speed-speed area was horizontally. The two-dimensional asymmetrical solution domain used for calculation herein corresponds to the “spindle-like” high-speed area at the three-dimensional level. This area allowed negatively-charged particles to quickly leave the corona pole, increasing the probability of positively-charged particles to be neutralized. The neutral particles formed drifted towards the plate under the action of the corona wind, during which they could combine with electrons and be absorbed on the dust collector plate resultantly. Therefore, a rational design of corona pole layout can improve the near-corona dust environment by avoiding the clustering of massive dusts in the vicinity of the corona pole.

![Figure 8](image_url)

**Figure 8.** X-direction corona wind velocities at different radii of curvature

### 3. CONCLUSION

The research in this paper provides theoretical basis for the optimization of the flow field near the corona pole of ESP. The respective corona winds generated at a pair of voltages and three radii of curvature were simulated numerically. The main conclusions are:

1) The corona wind mainly forms in the corona area, and the change of the flow field in other locations is caused by the corona wind;

2) Under several corona voltages, all velocities of the corona wind within the corona area are accelerated first and then become stable, followed by reductions. At a fixed spatial position, the higher the absolute voltage value, the higher the corona wind velocity.

3) The change of curvature radius of the corona pole within the corona area contributes little to the stabilized area formed after the attenuation of corona wind. The smaller curvature radius results in a rise in the velocity of the corona wind and the axial width of the high-speed region, as well as the shrinkage of its overall horizontal width.

### REFERENCES


[12] Nakamura H., Ohyama R., “An image analysis of positive ionic wind velocity under the DC corona discharge in needle-cylinder electrode system,” *IEEE*


