Real time implementation of feedback linearization control based three phase shunt active power filter

Ghadbane Ismail¹,*, Benchouia Mohamed Toufik², Barkat Said¹

¹. Laboratory L.G.E, M’sila University, M’sila, Algeria
². Laboratory L.G.E, Biskra University, Biskra, Algeria

ABSTRACT. In This paper, we present an experimental study of feedback Linearization applied to regulate the DC bus voltage of three-phase shunt Active Power Filter (APF). The feedback linearization controller is introduced to improve tracking performance characteristics, power quality and minimized consumption of the reactive power. To identify the reference currents we used an algorithm based on the Self Tuning Filter (STF). We generate the firing pulses of the IGBT inverter by using a hysteresis current controller, which is implemented on an analog card. An experimental bench has been implemented. It consists an active filter parallel to IGBTs, a nonlinear load RL, a dSPACE digital prototyping system (DS1104 development board) for generating the references of the harmonic currents and an analog card to realize the control of harmonic currents by hysteresis. The experimental results under steady state and transient conditions is illustrated with signal-flow graphs and corresponding analysis show the feasibility and the effectiveness of the designed active filter, associated with feedback Linearization controller capability in meeting the IEEE 519-1992 recommended harmonic standard limits.

RÉSUMÉ. Dans cet article, nous présentons une étude expérimentale de la linéarisation à feedback appliquée à la régulation de la tension du bus continu du filtre de puissance actif triphasé. Le contrôleur de linéarisation à feedback est introduit pour améliorer les performances de suivi, la qualité de l’énergie et la consommation réduite de la puissance réactive. Pour identifier les courants de référence, nous avons utilisé un algorithme basé sur le filtre de synchronisation automatisé (STF). Nous générons les impulsions de déclenchement de l’onduleur IGBT en utilisant un contrôleur de courant à hystérésis implanté sur une carte analogique. Un banc expérimental a été mis en place. Il s’agit d’un filtre actif parallèle aux IGBT, d’un RL de charge non linéaire, d’un système de prototypage numérique dSPACE (carte de développement DS1104) permettant de générer les références des courants harmoniques et d’une carte analogique pour contrôler les courants harmoniques par hystérésis. Les résultats expérimentaux dans des conditions stables et transitoires sont illustrés par des graphiques de flux de signaux et l’analyse correspondante montre la faisabilité et l’efficacité du filtre actif conçu, associé à la capacité du contrôleur de linéarisation à rétroaction à respecter les limites harmoniques standard recommandées par IEEE 519-1992.
1. Introduction

These last years, the increasing use of the devices of power electronics, the electric systems involved more and more problems in disturbances or harmonic distortions of the electrical supply networks. This phenomenon touches the whole of the industrial sectors (use of graduators, rectifiers, speed variations...), tertiary sector (data-processing or lighting of the offices, trades...) and domestic (television sets, apparatuses electric household appliances general public...) The harmonic distortion is generated by the nonlinear loads connected to a network and which absorbs non-sinusoidal currents (Abdelmadjid et al., 2006; Afonso et al., 2000; AitChihab et al., 2014).

These harmonics of current go to their turn to generate harmonic tensions at the various points of connection to the network. For other electric components connected in these points, this harmonic pollution has harmful effects. Among these effects, one can in particular quote the deformation of the tension network with not connection whereas the distributer of energy is held to provide a power clean. This pollution can also lead to the heating of the cables and of electric components or even with the sudden stop of revolving machines, even total destruction of all this equipment (Hasan & Osman, 2007; Leszek & Zarnecki, 2006;)

To decrease or remove these disturbances and thus to improve quality of energy distributed, several solutions exist the reduction of the impedance of short-circuiting, modification of the static inverter polluting in terms of topology and/or the order in order to intervene directly with the source of the harmonic disturbances, devices of filtering. The use of devices attracted great attention since two decades ago. Since its introduction some twenty years ago, the Active Power Filter (APF) presents a good solution for disturbance treatment, particularly for harmonic currents and/or voltages (Mohamed et al., 2008; Nadhir et al., 2014; Sabir et al., 2017; Singh et al., 2000).

APF is an up-to-date solution to power quality problems. The shunt APF allows the compensation of current harmonics and unbalance, together with the power factor correction, and can be a much better solution than the conventional approach (capacitors and passive filters) The performance of the APF is determined by the kind of control used. It is more emphasized when the voltages of the electrical network contain harmonics and/or are unbalanced.

Moreover, the Self Tuning Filter STF is proposed for extracting harmonic currents instead of classical harmonics extraction based on High Pass or Low Pass Filters (Lorenzo et al., 2007; Abdusalam et al., 2008) The three-phase currents/voltages are detected using current/voltage sensors. The inverter currents are controlled by using hysteresis comparators. The hysteresis control is characterized by its simplicity and its intrinsic speed. (Beaulieu & Ouhrouche, 2007; Ghamri et al., 2012; Saetieo et al., 1995).
2. System configuration

Fig. 1 presents the shunt active power filter topology based on a three-phase voltage source inverter, using IGBT switches, connected in parallel with the AC three-phase system through three inductors $L_f$. The capacitor $C$ is used in the DC side to smooth the DC terminal voltage. The nonlinear load is a three-phase diode rectifier supplying a RL load. This load generates harmonic currents in the supply system. The proposed control strategy can be divided into two parts. The first part is the harmonic isolator (reference current generation). It consists in generating the harmonic current references and uses STF instead of HPF or LPF usually used in the classical instantaneous real and imaginary power theory, first proposed by H. Akagi (Abdusalam et al., 2008). This harmonic isolator will be implemented into a DSPACE system (ds1104 prototyping card) in the experimental study.

The second part is the current control of the power converter. This controller generates the suited switching pattern to drive the IGBTs of the inverter by using a modulated hysteresis current controller. In the experimental study, this controller is implemented into an analog card.

![Figure 1. Power system configuration](image)

Fig. 2 presents the schematic diagram of the three-phase active power filter and the associated control strategy for harmonic mitigation. The filter is connected in parallel with the mains. The non-linear load is a three-phase diode rectifier feeding a
RL load. As mentioned above, the control method is divided into two parts. The first one consists in the harmonic isolator implemented into a DSPACE DS1104 development board. The second part is the analog hysteresis current controller, developed in our laboratory.

3. Harmonic isolation

The identification method chosen effect the quality of the compensation of current harmonics. Many theories of instantaneous power exist in scientific literature the extension of the reactive power to non-sinusoidal waveforms is now a subject of
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controversy. Many new theories have been proposed. Akagi (Beaulieu & Ouhrouche, 2007) proposed a theory based on instantaneous values in three-phase power systems with or without neutral wire, and is valid for steady-state or transitory operations, as well as for generic voltage and current waveforms called as Instantaneous Power Theory or Active-Reactive (p-q) Theory which consists of an algebraic transformation (Clarke Transformation) of the three-phase voltages in the a-b-c coordinates to the \( \alpha-\beta \) coordinates, followed by the calculation of the p-q theory instantaneous power components by eliminating the DC component of the instantaneous active power (corresponding to the fundamental component of load current) using a selective Filter STF, so the harmonic components can be identified. Figure 3 shows the modified scheme for the identification of reference currents during simultaneous compensation of harmonic currents and reactive power using the method of instantaneous power by using STF.

\[
\begin{bmatrix}
    v_{\alpha} \\
    v_{\beta}
\end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix}
    1 & -1/2 & -1/2 \\
    0 & \sqrt{3}/2 & -\sqrt{3}/2
\end{bmatrix} \begin{bmatrix}
    v_{sa} \\
    v_{sb} \\
    v_{sc}
\end{bmatrix}
\]

(1)

**Figure 3. The method of instantaneous active and reactive power**

This method is based on measuring the instantaneous three-phase variables present on the grid with or without zero-sequence components. This method is valid both in steady-state phase. In this control algorithm (Figure 2), measurements of voltages and currents expressed as a three phase (abc) are converted to two-phase system (\( \alpha-\beta \)) is equivalent to using the transform from Concordia leaving the power invariant.
The power is composed of three parts, in the presence of harmonics: reactive (Q), active (P) and deformed (D) as shown by the following equation:

$$S = \sqrt{P^2 + Q^2 + D^2}$$  \hspace{1cm} (3)

The instantaneous active power, denoted \(P(t)\) is defined by the following equation:

$$P(t) = v_{sa}i_{sa} + v_{sb}i_{sb} + v_{sc}i_{sc}$$  \hspace{1cm} (4)

In the stationary reference can be written:

$$P(t) = v_{s\alpha}i_{s\alpha} + v_{s\beta}i_{s\beta}$$  \hspace{1cm} (5)

Can be written, the instantaneous imaginary power as follows:

$$q(t) = -\frac{1}{\sqrt{3}} \left( (v_{sa} - v_{sb})i_{\alpha} + (v_{sb} - v_{sc})i_{\beta} + (v_{sc} - v_{sa})i_{\bar{\beta}} \right) = v_{sa}i_{\alpha} - v_{sb}i_{\beta}$$  \hspace{1cm} (6)

Q power meaning than the usual reactive power. In fact, unlike the reactive power, which considers only the fundamental frequency, the imaginary power takes into account all the harmonic components of voltage and current that is why it is given a different name (imaginary power) as a unit with the volt-ampere imaginary (VAI).

The part of the relations (5) and (6), we can establish the following matrix:

$$\begin{bmatrix} P \\ Q \end{bmatrix} = \begin{bmatrix} v_{s\alpha} & v_{s\beta} \\ -v_{s\beta} & v_{s\alpha} \end{bmatrix} \begin{bmatrix} i_{\alpha} \\ i_{\bar{\beta}} \end{bmatrix}$$  \hspace{1cm} (7)

with: \(\bar{P}\) Continuous power related to the fundamental component of active power and voltage, \(\bar{Q}\) Continuous power related to the fundamental component of reactive current and tension, \(\bar{P}\) and \(\bar{Q}\) Powers of alternatives related to the sum of the components of disruptive current and voltage.

By inverting the relation (7), we can recalculate the currents in the coordinate \(\alpha \beta\) as shown in the following equation.
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\[
\begin{bmatrix}
i_a \\
i_\beta
\end{bmatrix} = \frac{1}{v_{sa}^2 + v_{sb}^2} \begin{bmatrix} v_{sa} - v_{sb} \\ v_{sb} \\ v_{sa}
\end{bmatrix} \begin{bmatrix} p \\ q
\end{bmatrix}
\]  

(8)

Considering equations (8) and (9), we can separate the current benchmark in the three components, active and reactive at the fundamental frequency and harmonics.

Finally, it is easy to obtain the reference currents along the axes abc by the inverse transformation of Concordia

\[
\begin{bmatrix}
i_\alpha^* \\
i_\beta^*
\end{bmatrix} = \frac{1}{v_{\alpha}^2 + v_{\beta}^2} \begin{bmatrix} v_{\alpha} - v_{\beta} \\ v_{\beta} \\ v_{\alpha}
\end{bmatrix} \begin{bmatrix} \tilde{P} \\ \tilde{q}
\end{bmatrix}
\]  

(9)

\[
\begin{bmatrix}
i_\alpha^* \\
i_\beta^* \\
i_c^*
\end{bmatrix} = \sqrt{3} \begin{bmatrix} 1 & 0 \\ -1 & \sqrt{3} \\ -1 & \sqrt{3} \\ 2 & 2 \\ 2 & 2
\end{bmatrix} \begin{bmatrix} i_\alpha^* \\ i_\beta^*
\end{bmatrix}
\]  

(10)

To obtain a satisfactory extraction, the dynamic mode is slow. In general, cut-off frequency is selected enough low, between 5 Hz and 35 Hz, which generates then an instability of the active filter of power during fast variations of the load.

In the contrary case, if more raised cut-off frequency is chosen, precision determination of the alternate component is altered and can prove to be insufficient.

The self-tuning filter is the most important part of this control which allows to make insensible the PLL to the disturbances and filtering correctly the currents in α-β axis. Hong-Skok Song (Abdelmadjid et al., 2006) had presented in his PhD work how recovered the equivalent transfer function of the integration expressed by the block diagram of the STF tuned at the pulsation \( \omega_c \) is shown in the figure 5. The transfer function of this filter is:

According to the α-β axes, the expressions linking the components FMV output \( x_{\alpha\beta} \) to input \( x_{\alpha\beta} \) components are:

\[
\begin{align*}
\hat{x}_a &= \left(\frac{K}{s}\right) [x_a(s) - \hat{x}_a(s)] - \frac{\omega_c}{s} \hat{x}_\beta(s) \\
\hat{x}_\beta &= \left(\frac{K}{s}\right) [x_\beta(s) - \hat{x}_\beta(s)] - \frac{\omega_c}{s} \hat{x}_\alpha(s)
\end{align*}
\]

(11)
We obtain the following block diagram for STF

![Block Diagram of STF](image)

*Figure 4. Self-tuning filter*

4. Non-linear controller synthesis

In the stationary reference the dynamic equations of the active filter are given by:

\[
\begin{align*}
\frac{dV_{dc}}{dt} &= \frac{p_{dc}^*}{C_{dc}V_{dc}} \\
\frac{dI_{fa}}{dt} &= -\frac{R_f}{L_f} I_{fa} + \frac{V_{fa} - V_{sc}}{L_f} \\
\frac{dI_{fb}}{dt} &= -\frac{R_f}{L_f} I_{fa} + \frac{V_{fb} - V_{sc}}{L_f}
\end{align*}
\]

(12)

We have three outputs to regulate in this control strategy.

I- Subsystem 1

The equation of this subsystem is:

\[
\frac{dV_{dc}}{dt} = \frac{p_{dc}^*}{C_{dc}V_{dc}}
\]

(13)

The first sub-system of order 1, is characterized by its state, \(x=V_{dc}\) and its control: \(u=p_{dc}\). We can write the equation as follows:
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\[ \dot{x} = f(x) + g(x)u \]  \hspace{1cm} (14)

\[ f(x) = 0 \quad \text{and} \quad g(x) = \frac{1}{C_{dc}V_{dc}} \]

5. DC voltage controllers synthesis

The voltage regulation \( V_{dc} \) is provided by the subsystem 1. To achieve this object requires we must choose \( y = V_{dc} \) as output, then, we seek its relative degree.

\[ y = V_{dc} = h(x) \]

\[ \nabla h = \frac{\partial h}{\partial x} = \frac{\partial V_{dc}}{\partial V_{dc}} = 1 \]  \hspace{1cm} (15)

Its derivative is given by:

\[ \dot{y} = \frac{\partial h}{\partial x} \dot{x} = \frac{\partial h}{\partial X} = (f(x) + g(x)u) \]  \hspace{1cm} (16)

And as Lie derivatives, we write:

\[ \dot{y} = L_f h(X) + L_g h(X)u \]  \hspace{1cm} (17)

With:

\[ L_f h(X) = 0 \quad , \quad L_g h(X) = \frac{1}{C_{dc}V_{dc}} \]

It follows that:

\[ \dot{y} = \frac{1}{C_{dc}V_{dc}} P_{dc}^* \]  \hspace{1cm} (18)

The law of order is expressed by:

\[ P_{dc}^* = \frac{1}{L_g h(x)} (-L_f h(x) + v) = C_{dc} V_{dc} v \]  \hspace{1cm} (19)
\[ \nu = k_v (V_{dc}^* - V_{dc}) + \frac{d}{dt} V_{dc}^* \]  
(20)

\[ \nu = k_v (V_{dc}^* - V_{dc}) \]  
(21)

Figure 5. The photograph of the shunt APF prototype

\[
\begin{align*}
\frac{d i_{fa}}{dt} &= -\frac{R_f}{L_f} i_{fa} + \frac{V_{fa} - V_{xa}}{L_f} \\
\frac{d i_{fb}}{dt} &= -\frac{R_f}{L_f} i_{fb} + \frac{V_{fb} - V_{xb}}{L_f}
\end{align*}
\]  
(22)

The second sub-system of order 2, is characterized by its vector state \( x = [i_{fa} i_{fb}]^T \). Alpha and beta vector control is

\[ u = [v_{fa}^* v_{fb}^*]^T \]  
We can write the system of equations (22) under the form: \( \dot{x} = f(x) + g(x)u \) when:

\[ f(x) = \begin{bmatrix} f_1(x) \\ f_2(x) \end{bmatrix} = \begin{bmatrix} \frac{R_f}{L_f} i_{fa} - \frac{1}{L_f} V_{fa} \\ \frac{R_f}{L_f} i_{fb} - \frac{1}{L_f} V_{fb} \end{bmatrix} \quad \text{and} \quad g(x) = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \]  
(23)
Now we will apply the state feedback control on models (22) and (23)

6. Experimental results

The complete active filter system is composed mainly of a three-phase source, a nonlinear load, a hysteresis current and a Non linear controller. We study the robustness of the non linear using experimental results for different operating modes. The test bench used for the experiment is presented in Fig. 5. The input step-down transformer (10.60KVA) is connected to the mains (380 V line to line) and delivers a lumped voltage of 220 V. The three-phase parallel active filter is achieved with a voltage source inverter. This VSI contains a three-phase IGBT 1200V, 50A (SKM 50 GB 123D). To ensure the dead time of control signals and the insulation, developed cards based on the IXDP630 component and specialized circuits (SKHI 22) are used.

The performances of non linear control of the DC bus voltage of three phase shunt active power filter extensive experimentation for various operating conditions and parameters variation.

![Figure 6. Experimental results: filter current iF (A), source current iS (A), source voltage Vs (V) and DC voltage Vdc (V). Ch3 and Ch4 scale: 5 A/div; Ch2 scale: 100 V/div; Ch1 scale: 80 V/div; Time scale: 10 ms/div.](image)

First experimentation is done on fixed load, we observe that the DC-voltage is regulated well around the reference $V^*_{dc} = 420$ V. The mains current has a sinusoidal form and in phase with supply voltage (see Fig 6.), which minimizes the reactive power consumed by the inverter. It is confirmed for the two controllers in permanent response.

Second, to prove the dynamical response of the controllers at a transient condition, the DC side resistance is changed from $R_L$ to $R_L/2$. It can be seen that the voltage controlled by the non linear at Fig.7 joined quickly his reference
Finally, two tests have been performed to confirm the effectiveness of the control of DC voltage using a nonlinear controller. First, we fixed the reference voltage at the value $V_{dc}^* = 450V$ and the filter is switched; Figure 8 shows the results of the DC voltage link, after a transient response due to the charging capacitor (the capacitor has been charged initially at 210V), that the DC-voltage is regulated well around the reference $V_{dc}^* = 450V$. 

Figure 7. Experimental results with load changed: DC voltage and reference, Load current, Source current
Second, a double change of the reference is shown 450-300 and 450V. It can be noted that, the DC voltage regulated by the non linear controller follows its reference, there is no overshoot and the settling time is very small (see Fig. 9).

Figure 8. Experimental results with feedback linearisation control of Dc voltage and reference voltage

Figure 9. Experimental APF results with Feedback linearized: DC voltage Vdc (V) and DC reference voltage V^Rdc (V), Ch3 and Ch4 scale: 100 V/div, Time scale: 2s/div
Figure 10. Grid current and its spectrum (a) before filtering (b) after filtering

Fig. 10 show the grid current, mainly affected by the low order harmonics (5th, 7th, 11th), induced by the non-linear load; and as result, the THD factor is relatively high (23.6%). After compiling the APF, the grid current becomes quasi-sinusoidal, and no significant low order is noticed. Consequently, the total distortion factor (THD) is about 3.85%, meaning compliance with IEEE519-1992 norm.

Appendix

The experimental test bench parameters are:
Parameters
Source
Voltage (Vm)=120 V
Frequency (f) =50Hz
Resistance (RS)=0.42 Ω
Inductance (LS)=2.3 mH

Parameters
load
Resistance (Rl)=45 Ω
Inductance (Ll) =1.3 mH

Parameters
filter
DC link capacitor C=1100 μF
DC link voltage V*dC=420v
Inductance (LC)=0.8 mH
Hysteresis band Δi=0.2 A

8. Conclusion

The main goal of this article presented is articulated basically on two ideas, we have shown the effectiveness of the shunt active power filtering especially with the application of Non-linear control. After compensation The THD of the source voltage and the source current is well below 5%, the IEEE-519 standard imposes the harmonics limit. Further studies the power factor was corrected (power supply current and voltage became in phase). The control of the active power filter was divided into two parts, the first one realized by the DSpace system to generate the reference currents and the second one an analog card, implementing a hysteresis current controller. the proposed modified version of the p-q theory instead of classical extraction filters (low pass filters or high pass and) have been introduced by STFs, for both grid load currents and voltages. The use of this filter experimentally leads to satisfactory performances since it extracts the harmonic currents at high performances. Several tests have been performed in order to prove the efficiency of the controller. The experimental results presented in this article show that the method of feedback remarkably improves the operation of the active power filter in terms of the THD.

References


