

$$V_s \omega^2 r \rho_p - 6\pi\mu r_p v_p - V_s \rho_l \omega^2 r = 0$$

$$\omega^2 r (\rho_p - \rho_l) - \frac{6\pi\mu r_p v_p}{V_s} = 0$$

$$\omega^2 r (\rho_p - \rho_l) = \frac{6\pi\mu r_p v_p}{\frac{4}{3}\pi r_p^3}$$

$$v_p = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

Appendix B: Calculation of velocity of reinforcement particle at 220 rpm at a mould radial distance of 29mm

$$v_p = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

$$v_{p(sand)} = \frac{4 \times (0.4 \times 10^{-3})^2 \times 23.038^2 \times (29 \times 10^{-3})^2 \times (1600 - 737)}{18 \times 2.66 \times 10^{-3}} = 0.177 \text{ m/sec}$$

Similarly

$$v_{p(wood)} = \frac{4 \times (0.1 \times 10^{-3})^2 \times 23.038^2 \times (29 \times 10^{-3})^2 \times (892 - 737)}{18 \times 2.66 \times 10^{-3}} = 0.00199 \text{ m/sec}$$

where,

$$r_p = 0.4 \times 10^{-3} \text{ m for sand particles}$$

$$r_p = 0.1 \times 10^{-3} \text{ m for wood particles}$$

$$\omega = 23.03 \text{ rad/sec}$$

$$r = 0.029 \text{ m}$$

$$\rho_{p(wood)} = 892 \text{ kg/m}^3$$

$$\rho_{p(sand)} = 1600 \text{ kg/m}^3$$

$$\rho_l = 737 \text{ kg/m}^3 \text{ at } 130^\circ \text{C}$$

$$\mu = 2.66 \times 10^{-3} \text{ Pas}$$

Appendix C: Estimation of time taken by the particle to reach the mould wall

$$v_p = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

$$\frac{dr}{dt} = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

$$\frac{r - r_0}{t - t_0} = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

At $t=0$ and $r_0=0.1 \times 10^{-3} \text{ m}$

$$t = \frac{(r - 0.1 \times 10^{-3}) \times 18\mu}{4r_p^2 \omega^2 r (\rho_p - \rho_l)}$$

For sand particles

$$t_{sand} = \frac{(0.029 - 0.1 \times 10^{-3}) \times 18 \times 2.66 \times 10^{-3}}{4 \times (0.4 \times 10^{-3})^2 \times 23.038^2 \times (29 \times 10^{-3})^2 \times (1600 - 737)} = 0.1629 \text{ s}$$

For wood particles

$$t_{sand} = \frac{(0.029 - 0.1 \times 10^{-3}) \times 18 \times 2.66 \times 10^{-3}}{4 \times (0.1 \times 10^{-3})^2 \times 23.038^2 \times (29 \times 10^{-3})^2 \times (892 - 737)} = 14.51 \text{ s}$$

Appendix D: Temperature of the melt at the particular time taken by particles to reach the mould wall

$$T(t) = T_a + (T_0 - T_a)e^{-kt}$$

For sand particles

$$T(0.1629) = 20 + 110e^{-4.054 \times 10^{-5} \times 0.1629} = 129.999^\circ \text{C}$$

For wood particles

$$T(14.51) = 20 + 110e^{-4.054 \times 10^{-5} \times 14.51} = 129.935^\circ \text{C}$$

Appendix E: Viscosity of the melt at a particular time taken by the particles to reach the mould wall

$$\mu = A \exp\left(\frac{Q}{RT}\right)$$

For sand particles

$$\mu(0.163) = 1.0973 \times 10^{-5} \exp\left(\frac{17519.36}{8.31441 \times 402.99}\right) = 2.04698 \times 10^{-3} \text{ Pas}$$

For wood particles

$$\mu(14.51) = 1.0973 \times 10^{-5} \exp\left(\frac{17519.36}{8.31441 \times 402.935}\right) = 2.04844 \times 10^{-3} \text{ Pas}$$

Appendix F: Expression to find out the position of particle at a particular time period

$$v_p = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

$$\frac{dr}{dt} = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}$$

$$dr = \frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu} dt$$

$$\int_{r_0}^{r(t)} \frac{1}{r} dr = \int_0^t \frac{4r_p^2 \omega^2 (\rho_p - \rho_l)}{18\mu} dt$$

$$\ln(r(t)) - \ln(r(0)) = \frac{4r_p^2 \omega^2 t (\rho_p - \rho_l)}{18\mu}$$

$$e^{\ln(r(t))} = e^{\left[\ln(r(0)) + \frac{4r_p^2 \omega^2 t (\rho_p - \rho_l)}{18\mu}\right]}$$

$$r(t) = r_0 \exp\left[\frac{4r_p^2 \omega^2 r (\rho_p - \rho_l)}{18\mu}\right]$$