Traitement du Signal

# Outage Probability Analysis of MIMO-OSTBC Relaying Network Over Nakagami-m Fading Channel Conditions 

Ravi Shankar ${ }^{\text {* }}$, Indrajeet Kumar ${ }^{2}$, Ritesh Kumar Mishra ${ }^{2}$<br>${ }^{1}$ ECE Department, Madanapalle Institute of Technology and Science, Madanapalle, India<br>${ }^{2}$ ECE Department, National Institute of Technology, Patna, India<br>Corresponding Author Email: ravishankar@mits.ac.in

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#### Abstract

The objective of this study is to examine the outage probability (OP) performance of the multiple-input multiple-output (MIMO) cooperative communication system over Nakagami$m$ fading channel conditions. Source node transmits orthogonal space time block code (OSTBC) codeword to the relay \& destination node and maximal ratio combiner (MRC) is used for the decoding purpose at the destination node. A mathematical framework is developed for the analysis of diversity order (DO) of the system. The closed form expression of OP is derived in terms of confluent hypergeometric function of two variables considering perfect channel state information (CSI). The Simulation results verified the accuracy of the derived analytical results. Furthermore, the results shown that the distances between the nodes significantly affect the OP performance.


## 1. INTRODUCTION

Wireless channel is broadcast in nature i.e., transmission of data in the air where everyone can receive. This nature can be exploited to achieve cooperative diversity. Using Cooperative communication [1], other users can cooperate with the source in forwarding the data to the destination node. The main advantage of the cooperative communication is if direct source-to-destination (SD) channel is in deep fade, the destination can still receive the source signal through relay. Relay assisted cooperation is the first step towards the 5th generation (5G) wireless system, which is expected to offer up to 20 Gbps in the downlink (D/L) and 10 Gbps in uplink (U/L) wireless communication [2]. Numerous relaying schemes have been proposed in the existing literatures such as amplify-and-forward (AF) [3-5], decode-and-forward (DF) [6] and selective decode and forward (S-DF) [7-12]. However, the works [3-6] suffer from several significant drawbacks. Firstly, the system performance is limited due to the noise amplification problem because of the consideration of the AF relaying protocol. Secondly, in case of DF protocol, the relay node may forward erroneous signal to the destination node. To overcome this problem S-DF is proposed. In case of S-DF relaying protocol, relay only forwards correctly decoded signal to the destination node. In the work [13], the authors investigated the multiple hop multiple phase S-DF relaying protocol considering perfect CSI conditions. Asymptotic tight expression of symbol error rate (SER) is derived employing quadrature phase shift keying (QPSK) modulation schemes and shown to be tight at high signal to noise ratio (SNR) regimes. Results show that end-to-end system performance improves with optimal source-relay power allocation factors. In [14], the authors investigate the OP performance of a single input single output (SISO) cooperative communication system
over Nakagami-m fading channel conditions. In [15], the authors present the novel framework for optimizing and investigating the OP performance of a MIMO AF cooperative communication network, where K relays, each with finite cache capacity, are deployed to assist the transmission from a base station equipped with R antennas to the destination. The authors present the best relay selection criterion to choose the best relay, which maximizes the received SNR at the receiving terminal. For this criterion, we derive asymptotic and exact theoretical expressions for the system OP over independent and identically distributed (i.i.d.) Nakagami-m fading channel conditions. In the works [16-17], the authors investigate the D/L full duplex non-orthogonal multiple access (NOMA) cooperative communication network model and selective DF technique over Nakagami-m fading channel with imperfect CSI. This work assumes that the destination and the source node have fixed power, whereas relay nodes have constrained energies and should harvest radio frequency (RF) energy from the source for operation power. However, to the best of our knowledge, there has been no work to derive the exact OP of the destination SNR in MIMO OSTBC S-DF relaying network over Nakagami-m fading channel conditions.
We conclude the following novel contributions from this paper:
(1). The closed form OP expressions are derived for MIMO OSTBC S-DF relaying network over Nakagami-m fading channel, with perfect CSI.
(2). Further, a framework is developed for deriving the DO for MIMO OSTBC S-DF relaying network.

The rest of the paper is organized as follows; MIMO OSTBC S-DF system model is given in section 2. OP performance and DO analysis have been given in Section 3. In section 4 , simulation results are given and finally in section 5 paper conclusions are given.

## 2. SYSTEM MODEL

Consider MIMO OSTBC S-DF relaying network in which the source, relay and destination nodes are equipped with $M_{S}$, $M_{R}$ and $M_{D}$ number of antennas, respectively [13]. Spatially uncorrelated flat fading Nakagami-m fading channel is considered, and the fading links are assumed to be independent and identically distributed with each other. Since the source and relay nodes are employed by same OSTBC, we take $M_{S}=$ $M_{R}=M$ [9]. The signal transmission is divided into two phases, broadcast phase and relaying phase. During the broadcast phase, the source node transmits the MIMO OSTBC codeword $B_{S} \in C^{M * T S}$ to relay and destination, respectively. Where $T_{S}$ represents the number of time slots. The received code-word's at the destination node, $Y_{S D} \in \mathbb{C}^{M_{D} \times T_{S}}$ and at the relay node, $Y_{S R} \in \mathbb{C}^{M \times T}$, corresponding to the MIMO OSTBC code-word transmission from the source node can be written as [12],
$Y_{S D}=\sqrt{P_{S} / M R_{C}} H_{S D} B_{S}+Z_{S D}$,
$Y_{S R}=\sqrt{P_{S} / M R_{C}} H_{S R} B_{S}+Z_{S R}$.
where $P_{S}$ and $R_{C}$ denote the available power at the source node and coding rate, respectively. The terms of the $\mathrm{SD} H_{S D} \in$ $\mathbb{C}^{M_{D} \times M}$ and source-to-relay (SR) $H_{S R} \in \mathbb{C}^{M \times M}$ channel matrices are independent with each other, distributed as Nakagami- $m$ random variables (RVs) with a fading severity or shape parameter, $m_{i} \geq 0.50$; $i \in\{S D, S R\}$ and controlling spreads $\delta_{S D}^{2}$ and $\delta_{S R}^{2}$, respectively [19]. The channel fades for different links are assumed to be statistically independent. This is a reasonable assumption as the relays are usually spatially well separated. In the relaying phase, relay node re-transmits only successfully decoded


Figure 1. MIMO-OSTBC S-DF cooperative communication
Signal to the destination node, otherwise, it will remain in the idle state. The received symbol blocks at the destination node $Y_{R D} \in \mathbb{C}^{M_{D} \times T_{S}}$, corresponding to transmission from relay node can be written as [13],

$$
\begin{equation*}
Y_{R D}=\sqrt{P_{R} / M R_{C}} H_{R D} B_{S}+Z_{R D} . \tag{3}
\end{equation*}
$$

where $P_{R}$ denotes the power transmitted from the relay node. The relay-to-destination (RD) channel matrix $H_{R D} \in \mathbb{C}^{M_{D} \times M}$ is comprised of terms, which are independent with each other,
distributed as Nakagami- $m$ RVs with a fading severity or shape parameter, $m_{R D} \geq 0.50$ and controlling spread $\delta_{R D}^{2}$. The channel noise matrices $Z_{R D}, Z_{S R}$ and $Z_{S D}$ in (3), (2) and (1), respectively, are zero mean circular shift complex gaussian (ZMCSCG) RVs with variance $N_{0}$, respectively. Since the OSTBC based MIMO transmission orthogonalizes and converts the MIMO fading channel into scalar channels. The instantaneous SNR at the receiving terminal (destination node) is given as,

$$
\begin{equation*}
\gamma_{D}=\frac{c_{O} P_{S}}{R_{C} M N_{0}}\left\|H_{S D}\right\|_{F}^{2}+A_{R} \frac{c_{1} P_{R}}{R M N_{0}}\left\|H_{R D}\right\|_{F}^{2} . \tag{4}
\end{equation*}
$$

Here, $A_{R}$ represents the state of the relay node, is given as,

$$
A_{R}=\left\{\begin{array}{ll}
0 & \text { if } \gamma^{R}<\gamma_{T}^{R}  \tag{5}\\
1 & \text { if } \gamma^{R} \geq \gamma_{T}^{R}
\end{array} .\right.
$$

where $\gamma_{T}^{R}$ and $\gamma^{R}$ denotes the threshold SNR and the instantaneous SNR at the relay node, respectively. The $\gamma^{R} \mathrm{cab}$ be written as,
$\gamma^{R}=\frac{c_{2} P_{S}}{R_{C} M N_{0}}\left\|H_{S R}\right\|_{F}^{2}$.
where $c_{2}, c_{1}$ and $c_{0}$ denote the power dependent power transfer factors for the source-relay, relay-destination and source-destination channels, respectively. The $\mathrm{OP}_{\gamma_{T}}^{O P}$ can be written as,

$$
\begin{align*}
& P_{\gamma T}^{\text {oUTGGE }}=  \tag{7}\\
& \quad \operatorname{Pr}\left\{\left.\gamma^{D}\right|_{A_{r}=0} \leq \gamma_{T}^{D}\right\} \operatorname{Pr}\left\{A_{r}=0\right\}+\operatorname{Pr}\left\{\left.\gamma^{D}\right|_{A_{r}=1} \leq \gamma_{T}^{D}\right\} \operatorname{Pr}\left\{A_{r}=1\right\} .
\end{align*}
$$

where $\gamma_{T}^{D}$ and $\operatorname{Pr}\{$.$\} denote the threshold SNR at the$ destination node and probability operator, respectively. In this work, it is assumed that the source and relay node consume equal power, i.e., equal power allocation, so we can take, $P_{S} \leq$ $P / 2$ and $P_{R} \leq P / 2$, where $P$ denotes the total available power budget. Also, it has been considered that the relay and source node do not have the knowledge of RD and SD channel gains, respectively. Now, it obvious that the relay and source transmit with their maximum powers. Utilizing these transmit powers, the following notations,

$$
P_{0}^{\prime} \triangleq c_{0} \rho / 2, P_{1}^{\prime} \triangleq c_{1} \rho / 2, P_{2}^{\prime} \triangleq c_{1} \rho / 2,
$$

where

$$
\begin{equation*}
\rho=P / R N_{0} M \tag{8}
\end{equation*}
$$

and assuming $\gamma_{T}^{D}=\gamma_{T}^{R}=\gamma_{T}$ for simplicity purpose, OP expression given in (7) can be written as,
$P_{\gamma_{T}}^{\text {OUTAGE }}=$
$\operatorname{Pr}\left\{P_{0}^{\prime}\left\|H_{S D}\right\|_{F}^{2} \leq \gamma_{T}\right\} \operatorname{Pr}\left\{P_{2}^{\prime}\left\|H_{S R}\right\|_{F}^{2}<\gamma_{T}\right\}$

We assume that RD distance is smaller than the SD distance. Note that $c_{0}$ and $c_{1}$ impact the link-budget and the normalized fading comes on top of this. Therefore, we can write $c_{0} \leq c_{1}$ which implies that $P_{0}^{\prime} \leq P_{1}^{\prime}$ (see (8) above). This scenario is necessary for further mathematical development in section 3 .

## 3. ANALYSIS OF OP

### 3.1 OP analysis

Using the notations
$a \triangleq P_{0}^{\prime}\left\|H_{S D}\right\|_{F}^{2}, b \triangleq P_{1}^{\prime}\left\|H_{R D}\right\|_{F}^{2}, g \triangleq P_{2}^{\prime}\left\|H_{S R}\right\|_{F}^{2}$,
and $h \triangleq a+b$, the OP expression given in (9) can be written a

$$
\begin{equation*}
P_{\gamma_{T}}^{\text {OUTAGE }}=\operatorname{Pr}\left\{a \leq \gamma_{T}\right\} \operatorname{Pr}\left\{g<\gamma_{T}\right\}+\operatorname{Pr}\left\{h \leq \gamma_{T}\right\} \operatorname{Pr}\left\{g \geq \gamma_{T}\right\} . \tag{11}
\end{equation*}
$$

It is noted that $a, b$ and $g$ are Chi-square distributed RV with the degree of freedom $2 M_{R} M_{D} m_{S D}, 2 M_{R} M_{D} m_{R D}$ and $2 M_{S} M_{R} m_{S R}$, respectively. The probability density expression (PDF) of Chi-square distributed $\mathrm{RV}_{a}$ can be expressed as,

$$
\begin{equation*}
f_{\mathrm{A}}(a)=\frac{a^{M_{R} M_{D} m_{S D}-1}}{\left(2 P_{0}^{\prime}\right)^{M_{R} M_{D} m_{S D}} \Gamma\left(M_{R} M_{D} m_{S D}\right)} e^{-\frac{a}{2 P_{0}^{\prime}}} . \tag{12}
\end{equation*}
$$

Applying the similar procedure, we can express the PDF of Chi-square distributed RV $b$ and $g$, respectively in similar form as given in (12).

By performing some mathematical manipulations, it can be shown that,

$$
\begin{align*}
& \operatorname{Pr}\left\{a \leq \gamma_{T}\right\}=\frac{\gamma\left(M_{R} M_{D} m_{S D}, \frac{\gamma_{T}}{2 P_{0}^{\prime}}\right)}{\Gamma\left(M_{R} M_{D} m_{S D}\right)}, \\
& \operatorname{Pr}\left\{g \geq \gamma_{T}\right\}=\frac{\Gamma\left(M_{R}^{2} m_{S R}, \frac{\gamma_{T}}{2 P_{2}^{\prime}}\right)}{\Gamma\left(M_{R}^{2} m_{S R}\right)} . \tag{13}
\end{align*}
$$

where $\Gamma(),. \Gamma(.,$.$) and \Gamma($.$) denote the Gamma function,$ upper incomplete Gamma function and lower incomplete Gamma function, respectively [18].

### 3.2 Derivation for the PDF of $h$

The PDF of $h$ can be found out by using the concept of characteristics function (CF). The CF of $h$ can be expressed as the product of CF of $a$ and $b$, can be expressed as,
$\Upsilon_{\mathrm{A}}(\alpha)=\int_{0}^{\infty} f_{\mathrm{A}}(a) e^{j a \alpha} d a$.
Using (12) into (14) and using [(3.381.4) [18]], $\Upsilon_{A}(\alpha)$ can be written as,

$$
\begin{equation*}
\Upsilon_{\mathrm{A}}(\alpha)=\left(1-i 2 P_{0}^{\prime} \alpha\right)^{-M_{R} M_{D} m_{S D}} . \tag{15}
\end{equation*}
$$

Following the similar procedure, the CF of $b$ can be expressed as,
$\Upsilon_{B}(\alpha)=\left(1-i 2 P_{1}^{\prime} \alpha\right)^{-M_{R} M_{D} m_{R D}}$.
The CF of $h$ can be expressed as,

$$
\begin{align*}
\Upsilon_{H}(\alpha) & =\Upsilon_{B}(\alpha) \times \Upsilon_{\mathrm{A}}(\alpha) \\
& =\left(1-i 2 P_{1}^{\prime} \alpha\right)^{-M_{R} M_{D} m_{R D}} \times\left(1-i 2 P_{0}^{\prime} \alpha\right)^{-M_{R} M_{D} m_{S D}} . \tag{17}
\end{align*}
$$

The PDF of $h$ can be expressed as,
$f_{H}(h)=\frac{1}{2 \pi} \int_{0}^{\infty} \Upsilon_{H}(\alpha) e^{-j h \alpha} d \alpha$.

Substituting the expression of $\Upsilon_{H}(\alpha)$ into (18) and utilizing [(3.384.7) [18]], $f_{H}(h)$ can be expressed as,
$f_{H}(h)=$

$$
\begin{align*}
& \frac{h^{\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}-1\right)} e^{-\frac{h}{2 P_{0}^{\prime}}}}{\left(2 P_{0}^{\prime}\right)^{M_{R} M_{D} m_{S D}}\left(2 P_{1}^{\prime}\right)^{M_{R} M_{D} m_{R D}} \Gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right)} \times  \tag{19}\\
& \underbrace{{ }_{1}\left\{M_{R} M_{D} m_{S D} ; M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D} ;\left(\frac{1}{2 P_{0}^{\prime}}-\frac{1}{2 P_{1}^{\prime}}\right) h\right\}}_{L(h)} .
\end{align*}
$$

where ${ }_{1} F_{1}($.$) represents the single variable's confluent$ hypergeometric function [(9.210) [18]].

Using [(9.211.2) [18]], we get,
$L(h)=$
$\frac{1}{\Xi\left(M_{R} M_{D} m_{S D}, M_{R} M_{D} m_{R D}\right)} \int_{0}^{1} e^{\left(\frac{1}{2 R_{D}}-\frac{1}{2 R}\right)^{h t}} t^{M_{R} M_{D} m_{S D}-1}(1-t)^{M_{R} M_{D} m_{R D}-1} d t$.
where $\Xi\left(M_{R} M_{D} m_{S D}, M_{R} M_{D} m_{R D}\right)$ denotes the Beta function [18], defined as,
$\Xi\left(M_{R} M_{D} m_{S D}, M_{R} M_{D} m_{R D}\right)=\frac{\sqrt{M_{R} M_{D} m_{S D}} \times \sqrt{\sqrt{M_{R} M_{D} M_{D D} m_{S D}+M_{R} M_{D} m_{R D}}} .}{.}$
By using the notation

$$
\begin{align*}
& E_{K} \triangleq \\
& \frac{1}{\left(2 P_{0}\right)^{M_{R} M_{D} m_{S D}}\left(2 P_{1}\right)^{M_{R} M_{D} m_{R D}} \Gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right) \Xi\left(M_{R} M_{D} m_{S D}, M_{R} M_{D} m_{R D}\right)} \tag{22}
\end{align*}
$$

and some mathematical arrangements and manipulations, we get,
$\operatorname{Pr}\left\{h \leq \gamma_{T}\right\}=1-\mathrm{E}_{K} \int_{0}^{1} P_{1} t^{M_{R} M_{D} m_{S D}-1}(1-t)^{M_{R} M_{D} m_{R D}-1} d t$,
where $P_{1}$ is expressed as,
$P_{1}=\int_{\gamma_{T}}^{\infty} e^{-\frac{1}{2 P_{0}^{\prime}}\left(1-\left(1-\frac{P_{0}^{\prime}}{P_{1}^{\prime}}\right) t\right)} h^{h} h^{M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}-1} d h$.

$$
\begin{equation*}
P_{1}=(s)^{-M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}} \Gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}, s \gamma_{T}\right) \tag{25}
\end{equation*}
$$

where for simplicity, $s$ is defined as,

$$
\begin{equation*}
s=\frac{1}{2 P_{0}^{\prime}}\left(1-\left(1-\frac{P_{0}^{\prime}}{P_{1}^{\prime}}\right) t\right) \tag{26}
\end{equation*}
$$

Using the series representation of $\Gamma\left(M_{R} M_{D} m_{S D}+\right.$ $\left.M_{R} M_{D} m_{R D}, s \gamma_{T}\right) \quad[(8.352 .2)]$ and some mathematical manipulations, we get,

$$
\left.\begin{array}{l}
\operatorname{Pr}\left\{h \leq \gamma_{T}\right\}= \\
1-\left[\begin{array}{l}
\mathrm{E}_{K}\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}-1\right)! \\
\left.\quad \times \int_{0}^{1}\left\{e^{-\gamma_{T} s} \sum_{l=0}^{\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right)-1}\left[\frac{\left(\gamma_{T} s\right)^{l}}{l!} s^{-\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right)} \times\right]\right\} d t\right] \\
t^{M_{R} M_{D} m_{S D}-1}(1-t)^{M_{R} M_{D} m_{R D}-1}
\end{array}\right] \tag{27}
\end{array}\right] .
$$

In the integral given above, $s$ is a function of $t$. Substituting the value of $s$ given in (26) into (27), the mathematical manipulation leads to,

$$
\left.\begin{array}{l}
P_{2}= \\
\sum_{l=0}^{\substack{\left.M_{R} M_{R} M_{D} m_{S D}^{+} \\
M_{R} M_{D} m_{R D}-1\right)}}\left\{\begin{array}{l}
\frac{\gamma_{T}^{l} e^{-\frac{\gamma_{T}}{2 P_{0}^{\prime}}}\left(2 P_{0}^{\prime}\right)^{\left(M_{R} M_{R} M_{D} m_{S D}+\right.}}{l!} \times \\
\int_{0}^{1}\left\{(1-t)^{M_{R} M_{D} m_{R D}-1} t^{M_{R} M_{D} m_{S D}-1} e^{-\frac{\gamma_{T}}{2 P_{0}}\left(\frac{P_{0}^{\prime}}{P_{1}^{\prime}-1}\right)^{2}} \times\right. \\
\left(1-\left(1-\frac{P_{0}^{\prime}}{P_{1}^{\prime}}\right) t\right)^{l^{\left(l-M_{R} M_{D} m_{S D}+\right.}} .
\end{array}\right\} d t \tag{28}
\end{array}\right\}
$$

Utilizing [(3.385) [18]], we get the closed-form expression of $P_{2}$ in the form of confluent hypergeometric function $\Phi_{1}\left\{A_{11}, B_{11}, C_{11}, a, b\right\}$ of the variable $a$ and $b$ [(9.261.1) [18]]. Utilizing (21), (8) and $P_{2}$ in terms of $\Phi_{1}()$, (27) can be expressed as,
$\operatorname{Pr}\left\{h \leq \gamma_{T}\right\}=$
$1-\left(\frac{c_{0}}{c_{1}}\right)^{M_{R} M_{D} m_{S D}} e^{-\frac{\gamma_{T}}{\rho_{0}}} \sum_{l=0}^{\substack{M_{R} M_{R} M_{D} m_{s D}}} \frac{\gamma_{T}{ }^{\prime} m_{p o l}}{l!\left(\rho c_{0}\right)^{\prime}} \Phi_{1}\left\{\begin{array}{l}M_{R} M_{D} m_{S D}, M_{R} M_{D} m_{S D}+ \\ M_{R} M_{D} m_{R D}-l, M_{R} M_{D} m_{S D}+ \\ M_{R} M_{D} m_{R D},\left(1-\frac{c_{0}}{c_{1}}\right),\left(1-\frac{c_{0}}{c_{1}}\right) \frac{\gamma_{T}}{c_{0} \rho}\end{array}\right\}$.
The series of $\Phi_{1}$ (.) can be efficiently evaluated by applying the approximation $\left(1-\frac{c_{0}}{c_{1}}\right)<1$. Substituting (13) into (11), the OP can be expressed as,

$$
\begin{align*}
& P_{\gamma_{T}}^{\text {oUTAGE }}= \\
& \frac{\gamma\left(M_{R} M_{D} m_{S D}, \frac{\gamma_{T}}{\rho c_{0}}\right)}{\Gamma\left(M_{R} M_{D} m_{S D}\right)} \frac{\gamma\left(M_{R}^{2} m_{S R}, \frac{\gamma_{T}}{\rho c_{2}}\right)}{\Gamma\left(M_{R}^{2} m_{S R}\right)}+\operatorname{Pr}\left\{h \leq \gamma_{T}\right\} \frac{\Gamma\left(M_{R}^{2} m_{S R}, \frac{\gamma_{T}}{\rho c_{2}}\right)}{\Gamma\left(M_{R}^{2} m_{S R}\right)} . \tag{30}
\end{align*}
$$

### 3.3 DO Analysis

In case of high SNR, i.e., $\rho \rightarrow \infty, P_{\gamma_{T}}^{\text {OUTAGE }}$ tends to 0 . It can easily show by using $P_{2}$ for $\Phi_{1}()$, utilizing [(8.352) [18]], [(3.197.3) [18]], [(8.352.1) [18]] \& [(9.131) [18]]. The opposite scenario that $P_{\gamma_{T}}^{\text {OUTAGE }}$ tends to 1 as $\rho \rightarrow 0$ can be easily confirm for (30). While checking the high SNR scenario, it can be seen that the negative exponent of $\rho$ does not depend on $c_{1}$ and $c_{0}$. Thus, for simplicity purpose, we take $c_{1}=c_{0}$ for which $\Phi_{1}()$ in (29) tends to 1 . Utilizing [(8.352.1) [18]] to (29), (30) can be simplified as,

$$
\begin{aligned}
& P_{\gamma_{T}}^{\text {OUTAGE }}= \\
& \frac{\gamma\left(M_{R} M_{D} m_{S D}, \frac{\gamma_{T}}{\rho c_{0}}\right)}{\Gamma\left(M_{R} M_{D} m_{S D}\right)} \frac{\gamma\left(M_{R}^{2} m_{S R}, \frac{\gamma_{T}}{\rho c_{2}}\right)}{\Gamma\left(M_{R}^{2} m_{S R}\right)}+ \\
& \frac{\gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}, \frac{\gamma_{T}}{\rho c_{0}}\right)}{\Gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right)} \frac{\Gamma\left(M_{R}^{2} m_{S R}, \frac{\gamma_{T}}{\rho c_{2}}\right)}{\Gamma\left(M_{R}^{2} m_{S R}\right)} .
\end{aligned}
$$

It can be easily shown that the cooperation improves the DO of the system. For high SNR scenario the outage probability expression can be expressed as,

$$
\begin{align*}
& \frac{\gamma_{T}^{M_{R} M_{D} m_{S D}+M_{R} M_{R} m_{S R}} \rho^{-M_{R} M_{D} m_{S D}-M_{R} M_{R} m_{S R}}}{c_{0}^{M_{R} M_{D} m_{D} m_{S D}} c_{2}^{M_{R} M_{R} M_{S R}} \Gamma\left(M_{R} M_{D} m_{S D}\right) \Gamma\left(M_{R} M_{R} m_{S R}\right) M_{R}^{3} M_{D}}+  \tag{31}\\
& \frac{\gamma_{T}}{c_{0}^{M_{R} M_{D} M_{D} m_{D D} M_{S D} M_{R} M_{D}+M_{R} M_{D} m_{R D} m_{R D}} \Gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right)\left(M_{R} M_{D} M_{S D} M_{D} m_{S D}+M_{R} M_{D} M_{D D} m_{R D}\right)} \\
& -\frac{\gamma_{0}^{M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}+M_{R} M_{R} m_{S R}} \rho^{-\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right)-M_{R} M_{R} m_{S R}}}{c_{0}^{M_{R} M_{D} m_{S D} M_{R} M_{D} m_{R D}} c_{2}^{M_{R} M_{R} m_{S R}} \Gamma\left(M_{R} M_{D} m_{S D}+M_{R} M_{D} m_{R D}\right) \Gamma\left(M_{R} M_{R} m_{S R}\right) 2 M_{R}^{3} M_{D}}
\end{align*}
$$

The OP expression is dominate by the first two terms of (31). The DO becomes $M_{R} M_{D} m_{S D}+M_{R} M_{R} m_{S R}$ and $M_{R} M_{D} m_{S D}+$ $M_{R} M_{D} m_{R D}$ for $M_{D}>M_{R}$ and $M_{D} \leq M_{R}$, respectively. For special case when $A_{R}=1$, the asymptotic value of OP is completely described by the second term of (31) and DO expression becomes independent of the value of $M_{R}$ and $M_{D}$, for this special case DO is expressed as $M_{R} M_{D} m_{S D}+$ $M_{R} M_{D} m_{R D}$.

## 4. SIMULATION RESULTS

Monte-Carlo (MC) simulation are given to confirm the accuracy of the theoretical OP expression given in (30). Simulation parameters are, $M_{R}=1, R_{C}=1, c_{0}=0.80, c_{1}=$ $0.90, c_{2}=0.95, \gamma_{T}=5 d B$ and $P_{T}=4 d B w$. The Alamouti STBC codeword is used with 4-PSK modulation symbols. We consider the flat fading case and it has been assumed that the $H_{S D}, H_{S R}$ and $H_{R D}$ are constant during the two consecutives symbols. The total number of symbols transmission per iteration is $10^{6}$. Figure 2 compares the OP obtained via MC simulations and analytical calculation vs. $\rho$ for cooperation system with different number of $M_{D}$. We have also shown the performance comparison between the non-cooperation system with the cooperation system. Plot shows that the relaying system outperforms the non-cooperative schemes. With increase in the value of $M_{D}$, OP performance improves. Also, it is shown that with the increasing value of $\rho$, the OP decreases. Simulated plots confirm the accuracy of the analytical results.


Figure 2. OP performance for various number of antennas at the destination node

## 5. CONCLUSION

In this paper, we analyzed the OP performance of the MIMO-OSTBC S-DF cooperative communication system over Nakagami- $m$ fading channel conditions. Based on the assumption that channel estimation is error free, i.e., perfect CSI, we derived the OP of the MIMO-OSTBC S-DF cooperative communication system. The closed form expression of OP is derived in terms of confluent hypergeometric function of two variables. The Simulation results verified the accuracy of the derived analytical results. In addition, the results showed that the distance between nodes greatly influences OP performance. However, to theoretically obtain an optimal source-relay power splitting ratio based on the the OP analysis is left as a future study.

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