



Numerical analysis of hybrid nanofluids as coolants for automotive applications

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ABSTRACT

The study the laminar convective heat transfer of hybrid nanofluids in a 3D flattened tube under constant heat flux condition was carried out. The effects of Reynolds number and concentration of hybrid nanoparticles on heat transfer characteristics of MWCNT-Fe₃O₄/water hybrid nanofluids were numerically investigated. The simulations were performed for the Reynolds number in the range 50-1000 and for two volume concentrations of hybrid nanoparticles, 0.1% and 0.3% respectively. Results showed that the heat transfer coefficient increases with increasing volume concentration of hybrid nanoparticles and increasing Reynolds number. At low Reynolds numbers, the application of MWCNT-Fe₃O₄/water hybrid nanofluids in flattened tube can enhance heat transfer up to 31% compared with water (base fluid). Numerically results were validated by comparison of simulations with results available in literature.

Keywords: Hybrid Nanofluids, Flat Tube, Heat Transfer.

1. INTRODUCTION

In past decade, extensive research was focused on applications of nanofluids in the automotive industry, especially to automotive radiator. The researches carried out so far suggest that the nanofluids could be an alternative to conventional coolants (water, ethylene glycol, water and ethylene glycol mixture) used in various thermal applications [1-3], as well in automotive radiators [4,5].

Vajjha et al. [6] carried out a numerically study concerning to heat transfer characteristics of the Al₂O₃ and CuO nanoparticle into water-ethylene glycol mixture (40:60). The two nanofluids flow through a flattened tube under laminar flow. The heat transfer coefficient ($h=50$ W/m²K) and the temperature ($T=303$ K) on walls of tube were imposed. The study was performed in following conditions: the Reynolds number, $Re=100-2000$, the inlet temperature, $T_{in} = 90$ °C, the volume concentration of nanoparticles, $\phi=0-10\%$ for the Al₂O₃ and $\phi=0-6\%$ for the CuO nanoparticles. Their results indicated that thermal performances of the flattened tube were improved due to using nanofluids. There was an increase in heat transfer coefficient with increasing of Reynolds number and also with increasing of volume concentration of nanoparticles.

Huminic and Huminic [7] numerically investigated the effect of volume concentration of nanoparticles, of Brownian motion and of Reynolds number on thermal performances of the flattened tube using CuO/ethylene glycol nanofluids under laminar flow. The heat transfer coefficient ($h=50$ W/m²K) and

the temperature ($T=303$ K) on walls of tube were imposed. The boundary conditions imposed in this study was following: the Reynolds number, $Re=10-125$, the inlet temperature, $T_{in} = 50$ °C, the volume concentration of nanoparticles, $\phi=0-4\%$ for the CuO nanoparticles. The numerical results were compared with results obtained in the case circular and elliptic tubes. The authors founded that the thermal performances of flattened tubes were significantly enhanced compared to that of the elliptic and circular tubes using CuO/ethylene glycol nanofluids as coolant.

Delavari et al. [8] numerically investigated heat transfer and flow characteristics of ethylene glycol and water based on Al₂O₃ nanoparticles flowing through a flattened tube under laminar and turbulent flow. Single and two-phase approaches were employed. The study was performed in following conditions: the Reynolds number, $Re=1220-2440$ (laminar flow) and $Re=9350-23000$ (turbulent flow), the inlet temperature, $T_{in} = 35-60$ °C, and the volume concentration of nanoparticles, $\phi=0-1\%$. They observed that the numerical results using two-phase approach were closer to the experimental data than the results obtained using single-phase method.

Also, the heat transfer and flow characteristic of the water based Al₂O₃ and CuO nanoparticle flowing through a flattened tube under laminar flow were numerically investigated by M. Elsebay et al. [9]. The study was performed in following conditions: the Reynolds number, $Re=250-1750$, the inlet temperature, $T_{in}=80$ °C, the temperature, $T_w=303$ K, the heat

transfer coefficient, $h_w=50$ W/m²K and the volume concentration of nanoparticles, $\phi=0-7\%$. They observed that although the heat transfer coefficients increase with 45 and 38% for Al₂O₃/water and CuO/water nanofluids, the increase of heat transfer coefficient was correlated with a significantly increase in the friction factor and in pressure drop of 271 and 267% for Al₂O₃/water and 266 and 226% for CuO/water nanofluids.

It is known that nanofluids have a high thermal conductivity but also a high viscosity, which leads to limited use of nanofluids in the automotive industry. In last year's, research was focused on the development of new working fluids which combining of two or three solid materials into conventional fluids. These new fluids are called hybrid nanofluids. Thus, the main goal of this work is the study of influence of concentration of hybrid nanoparticles and Reynolds number on flattened tube.

2. SOLUTION METHODOLOGY

2.1. Physical model

In this study, the simulations were performed for a flattened tube of an automobile radiator (Fig. 1). The geometrical dimensions of the flattened tube were: the height, $H=2.56$ mm, the width, $W=16.1544$ mm, and the length, $L=500$ mm.

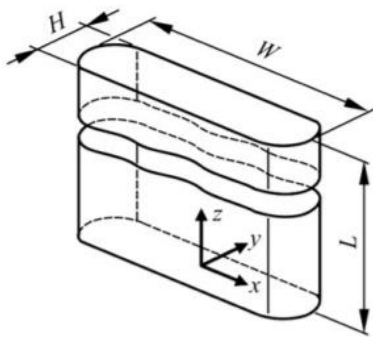


Figure 1. Physical model of flattened tube

2.2. Governing equations

The single phase model to investigate the thermal and fluid dynamic behavior of hybrid nanofluids was employed. The governing equations adopted in this study were based on the following assumptions: steady state process, fluid inside the flattened tube was Newtonian and incompressible, and radiative effect was negligible. Also, governing equations were solved in the Cartesian coordinate system using the ANSYS CFX-14.0 software.

The continuity equation:

$$\frac{\partial}{\partial x_i}(\rho U_i) = 0 \quad (1)$$

The momentum equations:

$$\frac{\partial}{\partial x_i}(\rho U_j U_i) = -\frac{\partial P}{\partial x_j} + \frac{\partial}{\partial x_i} \left(\mu \left(\frac{\partial U_j}{\partial x_i} \right) \right) \quad (2)$$

where $i, j \in \{1, 2, 3\}$.

The energy equation was solved to calculate the temperature distribution:

$$\frac{\partial}{\partial x_i}(\rho c_p U_j T) = \frac{\partial}{\partial x_i} \left(k \left(\frac{\partial T_i}{\partial x_i} \right) \right) \quad (3)$$

2.3. Grid independence test and validation

In order to grid independence test, three grid sizes were compared in terms of velocity and temperature. A multi-block meshing scheme with hexahedral elements was used for the generation of the structure grids (Fig.2).

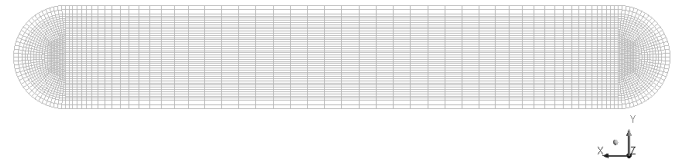


Figure 2. Grid layout used in the present analysis

Table 1 summarizes the grid independence study by comparing the velocity and temperatures profiles for water at $Re=100$, $T=313.15$ K and $Y=0$ m. After this grid independence study, grid II $90 \times 40 \times 200$ was chosen as the optimal grid size.

Table 1. Grid independence study

Grid	Velocity [m/s]	Temperature [K]
60x20x100	0.02420	309.013
90x40x200	0.02421	309.016
120x60x300	0.02422	309.016

In order to validation of the numerical model, the results were compared with the Shah and London correlation [10] and also with the numerical results carried out by Vajjha [6].

Shah and London correlations [10] for the constant wall heat flux in a circular tube under laminar flow are given below:

$$Nu = 1.953 \left(Re Pr \frac{d_h}{L} \right)^{1/3} \quad (4)$$

for $\left(Re Pr \frac{d_h}{L} \right) \geq 33.33$

$$Nu = 4.364 + 0.0722 \left(Re Pr \frac{d_h}{L} \right) \quad (5)$$

for $\left(Re Pr \frac{d_h}{L} \right) < 33.33$

In Eqs. (4) and (5), the hydraulic diameter of the flattened tube was $d_h=4.536 \cdot 10^{-3}$ m. The Reynolds and Prandtl numbers were defined as:

$$Re = \frac{U d_h}{\nu} = \frac{\rho U d_h}{\mu} \quad \text{and} \quad Pr = \frac{\mu c_p}{k} \quad (6)$$

As seen in Table 2 there a good agreement between the

calculated results and reported theoretical and numerical results.

Table 2. The validation of numerical model

Working fluid	Nusselt number, Nu	
	Shah-London correlation [10]	Numerical results
Water	Re=75	
	4.575	4.695
	Re=100	
	4.646	5.566
Ethylene glycol	Vajjha et al. [6]	
	Re=100	
	6.49	6.68

2.3. Boundary conditions

Numerical simulations were performed in a laminar flow with the Reynolds numbers in the range of 50-1000 for hybrid nanofluids based on water with volume concentrations of 0.1% and 0.3% for MWCNT+Fe₃O₄ hybrid nanoparticles.

In this study, the boundary conditions imposed were the following:

- Inlet: velocity (Re=50-1000) and temperature (T=313 K);
- Outlet: pressure (P=0);
- Wall: heat transfer coefficient (h=50 W/m²K) and temperature (T=293 K), non-slip condition;
- Interference surfaces of the domains: conservative interface flux.

2.4. Data reduction

Heat transfer rate can be expressed as

$$Q = \dot{m} c_p (T_{in} - T_{out}) \quad (7)$$

Heat transfer coefficient can be written

$$h = \frac{Q}{A_p (T_b - T_w)} = \frac{\dot{m} c_p (T_{in} - T_{out})}{A_p (T_b - T_w)} \quad (8)$$

Peripheral area is

$$A_p = 2(LH + LW) \quad (9)$$

Hydraulic diameter of tubes is given by

$$d_h = 4 \frac{A}{P} \quad (10)$$

3. THERMO-PHYSICAL PROPERTIES OF HYBRID NANOFLUIDS

The thermo-physical properties of hybrid nanofluids used in this study were chosen from the study of Sundar et al. [11]. In Table 3 were presented the thermo-physical properties of water based on MWCNT-Fe₃O₄ (26%:74%) hybrid nanoparticles.

Table 3. Thermo-physical properties of water [12] and MWCNT+Fe₃O₄ /water at 313 K [11]

Working fluid	Water	MWCNT-Fe ₃ O ₄ /water	
		φ=0.1%	φ=0.3%
Thermo-physical properties			
Thermal conductivity [W/mK]	0.633	0.720	0.7656
Viscosity [Pa s]	0.658·10 ⁻³	0.610·10 ⁻³	0.760·10 ⁻³
Density [kg/m ³]	992.20	995.85	1003.56
Specific heat [J/kg K]	4175	4179.66	4180.99

4. RESULTS AND DISCUSSIONS

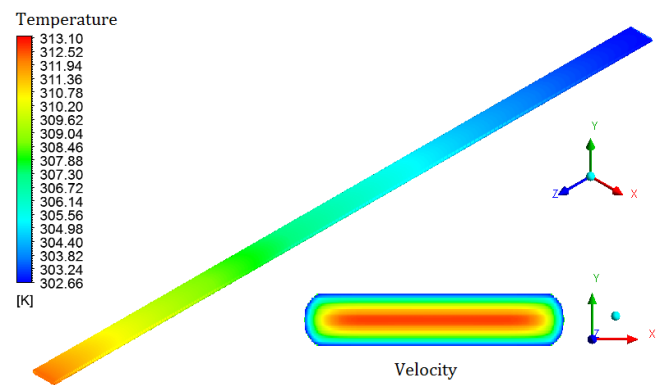


Figure 3 Temperature distribution and velocity profile for water at Re=50

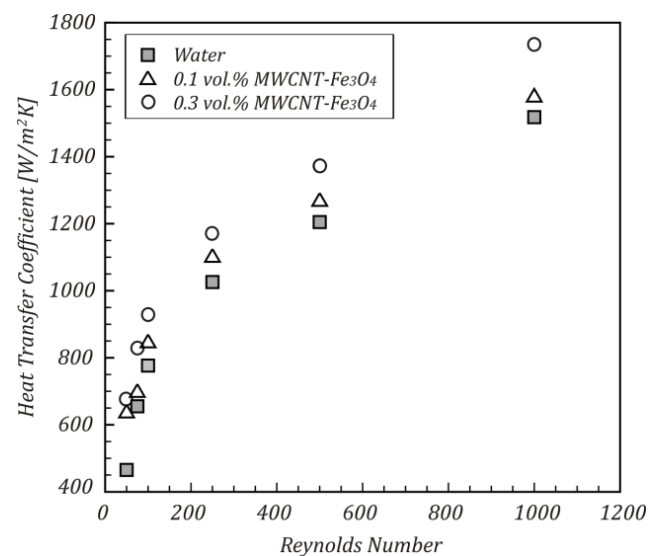


Figure 4. The variation of the heat transfer coefficient for different Reynolds number

In the present study, the heat transfer performances of flattened tube using hybrids nanofluid with volume concentrations of 0.1% and 0.3% of MWCNT-Fe₃O₄ hybrid nanoparticles in water were studied at different Reynolds numbers (Re=50-1000) and at the temperature of T=313.15 K.

The temperature and velocity profiles for water of the flattened tube at Re=50 were given in Fig. 3.

Fig. 4 shows the results of the average heat transfer coefficient for the Reynolds number within the range $Re=50-1000$, and two concentrations of MWCNT- Fe_3O_4 hybrid nanoparticles. As shown, heat transfer coefficient increases with increasing Reynolds number and increasing concentration of nanoparticles. Also, at low Reynolds numbers, the heat transfer coefficient increase was significantly higher than at high Reynolds numbers. Moreover, it is observed that heat transfer coefficient of hybrid nanofluids was considerably higher than that of water (base fluid).

Fig. 5 shows the effect of the Reynolds number on the ratio of convective heat transfer coefficient (h_{nf}/h_{bf}) defined as the ratio between the heat transfer coefficient of hybrid nanofluid (h_{nf}) and the heat transfer coefficient of base fluid (h_{bf}). From the numerical results, higher heat transfer coefficient ratio can be observed with increasing of the concentration of hybrid nanoparticles in water. The maximum heat transfer coefficient ratio was 1.45 at 0.3 vol.% MWCNT- Fe_3O_4 hybrid nanoparticles and $Re=50$. At same concentration of hybrid nanoparticles and $Re=1000$, heat transfer coefficient ratio was 1.143. Also, heat transfer coefficient ratio decreases with increasing Reynolds number for all studied concentrations of nanoparticles.

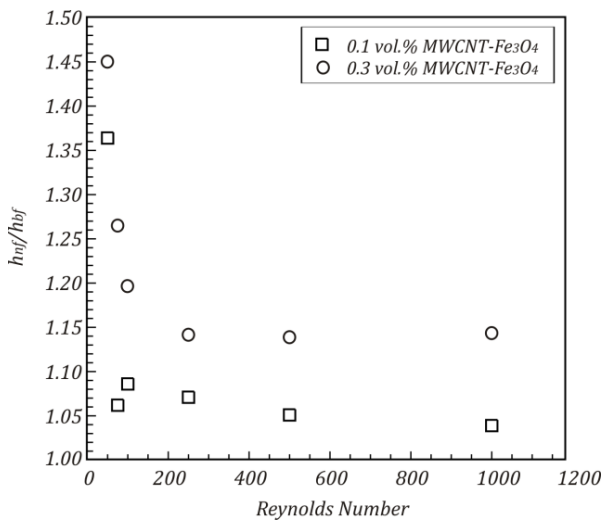


Figure 5. The heat transfer coefficient ratio versus Reynolds number

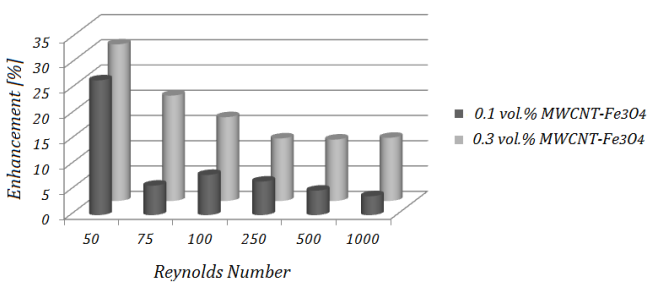


Figure 6. The heat transfer enhancement for different Reynolds number

The heat transfer enhancement for different Reynolds number and concentrations of hybrid nanoparticles is shown in Fig. 6. As shown in Fig. 6, the heat transfer enhancement increases with increasing concentration of hybrid nanoparticles and decreases with increasing Reynolds number.

The maximum enhancement ($100(h_{nf}-h_{bf})/h_{bf}$) was 31% for

a concentration of 0.3 vol.% nanoparticles and a Reynolds number of $Re=50$. At same Reynolds number, the enhancement of heat transfer coefficient for a concentration of the nanoparticles of 0.1% was 26.68%.

The pumping power required to circulate the working fluid can be expressed as:

$$W = AU(\Delta P) \quad (11)$$

The table 4 shows the pressure loss and the pumping power at different Reynolds numbers. As seen, the pressure loss increases with increasing Reynolds number in all cases. When using 0.1% MWCNT- Fe_3O_4 hybrid nanoparticles in flattened tube, the pressure loss increases up $Re=250$, after which it can be observed a decrease of it compared with the water (base fluid). Also, at a concentration of 0.3% MWCNT- Fe_3O_4 hybrid nanoparticles, the pressure loss increases compared with water and 0.1% MWCNT- Fe_3O_4 hybrid nanofluid. Furthermore, it can be seen a decrease of the pumping power at a concentration of 0.1% nanoparticles and Reynolds numbers in the range 75-1000 compared cu water, while at a concentration of 0.3% can be observed a significantly increase of the pumping power.

Table 4. Pressure loss and the pumping power in a flattened tube using hybrid nanofluids

Reynolds number	50	75	100	250	500	1000
<i>Water</i>						
Pressure loss [Pa]	18.21	23.69	28.55	50.07	85.52	157.92
Power [W]	$5.28 \cdot 10^{-6}$	$1.04 \cdot 10^{-5}$	$1.71 \cdot 10^{-5}$	$7.20 \cdot 10^{-5}$	$2.48 \cdot 10^{-4}$	$9.15 \cdot 10^{-4}$
<i>0.1% MWCNT-Fe₃O₄</i>						
Pressure loss [Pa]	20.33	25.02	29.87	50.57	84.09	151.99
Power [W]	$5.48 \cdot 10^{-6}$	$1.0 \cdot 10^{-5}$	$1.67 \cdot 10^{-5}$	$6.87 \cdot 10^{-5}$	$2.28 \cdot 10^{-4}$	$8.20 \cdot 10^{-4}$
% Power reduction	3.92	-3.97	-2.35	-4.62	-7.81	-10.4
<i>0.3% MWCNT-Fe₃O₄</i>						
Pressure loss [Pa]	27.67	34.51	39.61	67.81	122.67	207.98
Power [W]	$9.23 \cdot 10^{-6}$	$1.79 \cdot 10^{-5}$	$2.69 \cdot 10^{-5}$	$1.14 \cdot 10^{-4}$	$4.07 \cdot 10^{-4}$	$1.39 \cdot 10^{-3}$
% Power reduction	74.85	72.18	57.21	58.01	64.16	51.68

5. CONCLUSIONS

The heat transfer performances of a flattened tube were numerically investigated using water based MWCNT- Fe_3O_4 hybrid nanofluids in laminar flow. The influence of the Reynolds number and volume concentration of hybrid nanoparticles on the cooling performances of hybrid nanofluids and water were studied. The numerical results showed that the heat transfer coefficients of the MWCNT- Fe_3O_4 /water hybrid nanofluids were significantly higher than those of the base fluid (water). The increase in heat transfer coefficients was higher at low Reynolds numbers. The heat transfer enhancement of hybrid nanofluids depends of the volume concentration of hybrid nanoparticles, increasing

concentration of hybrid nanoparticles of 0.3 % showing a maximum heat transfer enhancement of 31%.

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NOMENCLATURE

A	tube surface area, m^2
A_p	peripheral area, m^2
c_p	specific heat, $J \cdot Kg^{-1} \cdot K^{-1}$
dh	hydraulic diameter of the tube, m
h	heat transfer coefficient, $W \cdot m^{-2} \cdot K^{-1}$
H	height, m
k	thermal conductivity, $W \cdot m^{-1} \cdot K^{-1}$
L	length, m
\dot{m}	mass flow rate, $kg \cdot s^{-1}$
Nu	Nusselt number
P	pressure, Pa
P	perimeter, m
Pr	Prandtl number
Q	heat transfer rate, W
Re	Reynolds number
T	temperature, K
U	velocity, $m \cdot s^{-1}$
W	width, m
W	power, W (Eq. 10)
x	cartesian coordinates, m

Greek symbols

ρ	density, $kg \cdot m^{-3}$
ν	kinematic viscosity, $m^2 \cdot s^{-1}$
μ	dynamic viscosity, Pa s

Subscripts

b	bulk
in	inlet
out	outlet
w	wall